# Second Harmonic Spectroscopy of Surface Lattice Resonances

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## Supporting Information

ABSTRACT: Because of their large figures of merit, surface lattice resonances (SLRs) in metal nanoparticle arrays are very promising for chemical and biomolecular sensing in both liquid and gas media. SLRs are sensitive to refractive index changes both near the surface of the nanoparticles (surface sensitivity) and in the volume between them (bulk sensitivity). Because of its intrinsic surface-sensitivity and a power law dependence on electric fields, second harmonic generation (SHG) spectroscopy can improve upon both the surface and volume sensitivities of SLRs. In this report on SHG spectroscopy of plasmonic nanoparticles, we show that



the SHG signal is greatly increased (up to 450 times) by the SLRs. We also demonstrate very narrow resonances in SHG intensity (~5 nm fwhm). We illustrate how the SHG resonances are highly sensitive to SLRs by varying the fundamental wavelength, angle of incidence, nanoparticle material, and lattice constant of the arrays. Finally, we identify an SHG resonance (10 nm fwhm) that is electric dipole forbidden and can be attributed to higher-order multipoles, enhanced by the strong nearfields of SLRs. Our results open up new and very promising avenues for chemical and biomolecular sensing based on SHG spectroscopy of SLRs.

**KEYWORDS:** Nonlinear optics, plasmonics, quadrupoles, surface lattice resonance

Recently, nonlinear plasmonics has attracted significant research interest.<sup>1,2</sup> The reason is that nonlinear optical effects scale as a power law of the incident light and plasmonic nanostructures strongly concentrate the incident light into optical near-field "hotspots". As a consequence, within such hotspots, nonlinear plasmonic effects are tremendously enlarged, offering prospects for new and improved applications.

Because nonlinear optical effects find applications in tuning laser light, significant research interest has been devoted to nanostructure-enhanced frequency conversion, with increasing efficiency. Various strategies have been employed for enhancing frequency conversion such as using all-dielectric nanostructures for increased damage threshold,<sup>3-5</sup> plasmonicdielectric hybrids where a plasmonic resonance enhances the frequency conversion of the dielectric,  $^{6-8}$  and plasmonic nanostructures.<sup>1,2,9</sup> Nonlinear optical effects also find applications in multiphoton microscopy, useful for biological sciences and material characterization.<sup>10</sup> Plasmonic nanoparticles have thus been the subject of numerous investigations with second harmonic generation (SHG),<sup>11–13</sup> third harmonic generation,<sup>14,15</sup> and two-photon luminescence microscopy. Because of the frequency conversion, the measured signal in all these techniques is background free (from the illumination). The

improved frequency conversion offered by plasmons can allow imaging with lower laser power and reduced photodamage to specimens (organic or inorganic).<sup>16,17</sup> The absence of signal background is also a key factor for the strong sensitivity of nonlinear optical effects, such as SHG chiral optical effects,<sup>18-21</sup> or magnetization-induced SHG<sup>22,23</sup> compared to their linear optical counterparts.<sup>24</sup> Though considerable attention has been devoted to the SHG enhancements from localized surface plasmon resonances (LSPR) and metasurfaces,<sup>25–31</sup> surface lattice resonances (SLR)<sup>32–36</sup> have received much less consideration.<sup>37,38</sup>

SLRs are more promising for sensing applications than LSPRs because of their significantly narrower resonance line width (<5 nm).<sup>34,39–41</sup> Since the resonance wavelength depends on the refractive index of the environment,<sup>42</sup> surface plasmons can be used for chemical and biological sensing in both liquid and gaseous media. Although for LSPRs the figure of merit (FoM) is typically on the order of a few units, for SLRs it is much larger<sup>43,44</sup> (by one<sup>45</sup> and even two<sup>46</sup> orders of magnitude), and the narrower resonance line width is

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Figure 1. Our large-area gold nanoparticle arrays exhibit clear surface lattice resonances. (a) Sample schematic and dimensions showing gold nanoparticles on a fused silica substrate and capped with photoresist (SU8). (b) Scanning electron micrograph of the fabricated nanoparticle array before capping with SU8. (c) Photograph of an investigated sample, the large-area nanostructured array appears green. (d) Experimental mapping of transmission spectra versus changing angle of incidence, upon illumination with vertically polarized light ( $S_{IN}$ ). The green lines show theoretical calculations of the diffraction beams that couple into surface lattice resonances. The red and blue dashed lines indicate the angles of incidence for enhancing 810 nm fundamental light.

attributed to a Fano-type effect.<sup>47</sup> SLRs occur on plasmonic nanoparticles, arranged periodically, with a lattice constant of the order of the wavelength of incident light. The two determining factors for the SLR are the LSPR and the Rayleigh anomaly (where light is diffracted in the plane of the array).<sup>47–49</sup> Specifically, the SLRs result from the coupling of the broad LSPR with the narrow frequency of the Rayleigh anomaly and hence exhibit a dual sensitivity—surface (on the nanoparticles) and bulk (between the nanoparticles).<sup>50</sup>

Here, we demonstrate SHG spectroscopy of SLRs, where the SHG signal is enhanced up to 450-times by SLRs, much above the previous reports of 10- and 30-times increase.<sup>37,38</sup> The measured SHG resonances can be as sharp as 5 nm in fwhm, which is promising for sensing. Indeed, we show that the SHG signal is very sensitive to the factors determining SLRs; we successfully tuned the SHG by varying the fundamental wavelength, the angle of incidence, the lattice parameter, and the nanoparticle material. Importantly, we discover SHG spectroscopy resonances (10 nm fwhm) that are not associated with electric dipoles. We attribute these resonances to higher-order contributions, enhanced by the SLRs. For individual nanoparticles with diameter >100 nm, retardation effects lead to higher-order terms (quadrupoles,<sup>51</sup> octupoles, etc.<sup>52–55</sup>) at the second harmonic frequency.<sup>56,57</sup> Although in previous decades such higher-order contributions did not play a major role in material properties, recent progress in nanofabrication has pushed them to the forefront of nonlinear plasmonics.<sup>58,59</sup>

We study four samples, where gold and silver plasmonic nanoparticles are arranged into two square lattices each, with periodicities of 580 and 600 nm. Further specifications of the samples can be found in Section S.1 of the Supporting Information. The sample geometry is shown in Figure 1a. The nanoparticle arrays are fabricated using PEEL (a combination of photolithography, e-beam deposition, etching, and lift-off). A scanning electron micrograph (SEM) of a 600 nm period array is shown in Figure 1b. An advantage of this fabrication technique is the ability to create large-area (cm<sup>2</sup>) uniform arrays, as demonstrated in Figure 1c, where the nanoparticle array appears green due to its diffractive properties. The linear transmission spectra as a function of the angle of incidence for the 600 nm period gold array are shown in Figure 1d, revealing the location of the SLR band edges. The Rayleigh anomaly dispersion, denoted by the green lines in Figure 1d, is calculated using<sup>37</sup>

$$\lambda_{(i,0)} = a_0 \left( \frac{n}{|i|} - \frac{\sin(\theta)}{i} \right) \tag{1}$$

where  $a_0$  is the lattice periodicity, *n* is the refractive index of the surrounding environment,  $\theta$  is the angle of incidence, and *i* is an integer denoting the diffraction order. At the wavelength of the Rayleigh anomaly, the diffracted wave travels across the sample surface interacting with multiple nanoparticles. When the wavelength undergoing a Rayleigh anomaly interferes with the broad LSPR of individual nanoparticles, a Fano-type SLR occurs (Figure 2a).



Figure 2. Numerical simulations illustrating the surface lattice resonance (SLR) enhancement of near-fields. (a) For the 600 nm period gold array, the transmission at normal incidence clearly displays an SLR, at 872 nm. (b) Electric near-field at the surface of the nanoparticle, away from resonance at 780 nm. (c) Electric near-field at the surface of the nanoparticle, at 872 nm, the wavelength of SLR. A distinctive radiative dipole can be seen, illustrating the nature of the SLR.

Figure 2a shows a numerically calculated transmission spectrum (performed using Lumerical<sup>60</sup>) of the 600 nm period gold nanoparticle array for normal incident light. The dip in transmission at 675 nm is attributable to the LSPR. The Rayleigh anomaly is at 870 nm, and the SLR is at 872 nm. To illustrate the specific electromagnetic behavior of the SLR, we plot the results of numerical simulations at two different

wavelengths: at the SLR and away from it. Specifically, these are electric field simulations, at the surface of a single nanoparticle, with periodic boundary conditions. In Figure 2b, at 780 nm, that is, away from the SLR, the electric field is concentrated around the nanoparticle. By contrast, in Figure 2c, at 872 nm, that is, at the wavelength of SLR, the electric field radiated by the nanoparticle extends to neighboring nanoparticles. This is evidenced by the electromagnetic radiation from the dipole reaching beyond a single unit cell. The enhancement of the electric near-field at the SLR leads to an increased SHG signal.

Second harmonic generation is caused by a part of the material polarization that occurs and radiates at  $2\omega$ , that is, twice the fundamental driving frequency  $\omega$ . The total effective second order nonlinear polarization can be expressed as

$$\mathbf{P}(2\omega) = \mathbf{P}^{D}(2\omega) + \mathbf{P}^{Q}(2\omega)$$
(2)

where  $\mathbf{P}^{D}(2\omega)$  is the dipole contribution to the second harmonic polarization, and  $\mathbf{P}^{Q}(2\omega)$  represents the contribution from quadrupoles. These two terms can then be written in full as<sup>61</sup>

$$P_i^D(2\omega) = \chi_{ijk}^{(2,D)} E_j(\omega) E_k(\omega),$$
  

$$P_i^Q(2\omega) = \chi_{ijkl}^{(2,Q)} E_j(\omega) \nabla_k E_l(\omega)$$
(3)

where summation over repeated indices is implied. The indices i, j, and k take the Cartesian directions, and  $E(\omega)$  is the electric field of the incident light. Here,  $\chi_{ijk}^{(2,D)}$  is a rank three tensor denoting the electric dipole susceptibility at the second harmonic, the first index designates the direction of the polarization, and the final two indices are the directions of the input fields. The quadrupolar contribution is represented by the rank four tensor  $\chi_{ijk}^{(2,Q)}$ . The expression for  $P_i^Q(2\omega)$  in eq 3 is obtained by a Taylor expansion and represents the quadrupolar contribution to the second order polarization, see Section S.2 in the Supporting Information for further details. Electric dipole contributions to SHG are forbidden in systems with inversion symmetry. Our arrays of gold nanoparticles possess  $C_{4\nu}$  symmetry, and the corresponding  $\chi_{ijk}^{(2,D)}$  tensor is<sup>62</sup>

$$\chi_{ijk}^{(2,D)} = \begin{pmatrix} 0 & 0 & 0 & 0 & \chi_{XXZ} & 0 \\ 0 & 0 & 0 & \chi_{XXZ} & 0 & 0 \\ \chi_{ZYY} & \chi_{ZYY} & \chi_{ZZZ} & 0 & 0 & 0 \end{pmatrix}$$
(4)

This  $C_{4v}$  tensor is mathematically identical to the rotationally isotropic surface tensor. Eq 2 shows that the dipolar contribution to SHG scales as a power law of the electric field of incident light and that the quadrupolar contribution is proportional to gradients of that electric field. Notably, in SLRs, the bulk and surface sensitivities are characterized by a long-range radiative dipole coupling (which scales as  $e^{ikr}/r$ ) and by a short-range electric near-field (which scales as  $1/r^3$  and contains strong electric field gradients), respectively. In other terms, SLRs are surface-sensitive: a spectral shift is induced in response to the refractive index change in the local environment. On the other hand, they are bulk-sensitive: the electromagnetic field of SLR modes is not confined to the plane of the array, it extends over a volume, tens of hundreds of nm across.<sup>63,64</sup> Consequently, combining SLRs and SHG presents obvious advantages, and SHG spectroscopy of SLRs is currently of increasing interest.<sup>37,38,65</sup>

Our experiments demonstrate two types of SHG enhancement mechanism: one dominated by dipolar contribution (sensitive to the amplitude of SLR enhanced near-fields) and one dominated by higher-order contributions (additionally sensitive to the gradients of SLR enhanced near-fields). The SHG experimental setup is shown in Figure 3a. A tunable



**Figure 3.** Second harmonic generation signal clearly stands out from the multiphoton background. (a) Experimental configuration for the SHG measurements, where  $\theta$  is the angle of incidence, RG is an RG665 Schott glass filter, BP is bandpass filter, and PMT is a photomultiplier tube. (b) For illumination with 780 nm fundamental light, the multiphoton emission is plotted versus wavelength. A 10 nm fwhm bandpass filter was used for each detection wavelength, as indicated by the inset. The dashed vertical line shows the SHG signal, and the shaded region shows the fwhm of the bandpass filter.

femtosecond pulsed laser provides the incident fundamental wavelength, which is adjusted to a power of 0.5 mW, the sample is mounted on an automated rotation stage to control the angle of optical incidence, and an analyzing polarizer is used to decompose the SHG signal into its vertically (S) and horizontally (P) polarized components. See Section S.3 in the Supporting Information for further experimental details.

First, it is important to establish that the measurements clearly correspond to SHG; for instance, three-photon luminescence could spectrally overlap with the detected SHG signal. Previous studies did not report such a check.<sup>37,38</sup> To characterize the respective contributions from multiphoton luminescence and SHG, a series of bandpass filters are used, see Figure 3b, inset. The filters are centered at 10 nm intervals, with 10 nm fwhm. In this experiment, the fundamental

wavelength and the angle of incidence are kept constant at 780 nm and  $9.2^{\circ}$ , respectively. These values are close to an SLR in the 600 nm period sample. As Figure 3b illustrates, the strongest signal occurs at 390 nm, which is the SHG. For wavelengths 380 nm and below, as well as for wavelengths 400 nm and above, there is negligible signal, which establishes that there is no contribution from multiphoton luminescence. The results unambiguously demonstrate that the signals we measure correspond to pure SHG.

The SHG signal is greatly enhanced by the SLRs. We begin with the 600 nm period array of gold nanoparticles, illuminated at 810 nm. In Figure 4a, the SHG intensity is plotted as a function of the angle of incidence, for the S<sub>IN</sub>-P<sub>OUT</sub> polarizeranalyzer configuration (i.e., vertical-in horizontal-out). Two strong SHG enhancements are observed at around  $\pm 6^{\circ}$  angle of incidence. The red and blue dashed lines in Figure 1d correspond to the calculated Rayleigh anomalies at  $\pm 5.7^{\circ}$ , which are shown by the black dashed lines in Figure 4a. For angles of incidence in between the peaks, there is no enhancement of SHG, and the signal is below 0.2 counts per second. From these data, the SHG enhancement in the SLR peaks is over 150-times due to the strong electric near-fields around the nanoparticles provided by the SLR. Notably, this enhancement is already much greater compared to the previous reports of 10- and 30-times,<sup>37,38</sup> but it can be even greater.

Next, we examine how the SLR enhancement of SHG is affected by fundamental wavelength, angle of incidence, array periodicity, and nanoparticle material, see Figure 4b-d. Specifically, nanoparticle arrays with periodicities of 600 and 580 nm are investigated, and four fundamental wavelengths are used, throughout various angles of incidence. For each fundamental wavelength and each sample periodicity, there is a corresponding peak in SHG versus angle of incidence. The figures show that as the fundamental wavelength is decreased, the corresponding SHG enhancement shifts to greater angles of incidence. The SHG peaks track the angle of incidence at which a corresponding SLR occurs. Between Figure 4b and c, the peaks are offset in angle of incidence. This offset is due to the change in array periodicity, which affects the position of the SLRs. It should be noted that all our sample arrays are covered with SU8 and that the difference in their behavior is therefore not due to differences in their refractive index environment. Moreover, because the azimuthal angle orientation of the arrays affects the dispersion of the Rayleigh anomalies, all samples were orientated with their lattice vectors parallel to the incident polarization.

Furthermore, we investigate silver nanoparticle arrays with identical periodicities to those of the gold nanoarrays: 600 and 580 nm. In the case of silver, an SHG enhancement of up to 450-times is observed, for the 600 nm period array, as shown in Figure 4d. This enhancement occurs for a fundamental wavelength of 760 nm, at 11.2° angle of incidence (indicated with blue lines in Figure S1 of the Supporting Information). The strength of this SHG enhancement can be attributed to a strong SLR. Indeed, the SHG intensity scales as the fourth power of the electric near-fields, which are enhanced at the SLR. In Figure S1, the deep black color near the intersection of the blue lines clearly indicates very low transmission through the arrays, that is, a strong SLR.

At maximum enhancement an SHG conversion efficiency of  $\eta_{\text{SHG}} = 1.5 \times 10^{-9}$  is obtained, where  $\eta_{\text{SHG}} = P(2\omega)/P(\omega)$  with  $P(2\omega)$  and  $P(\omega)$  being the power of the SHG and fundamental,



**Figure 4.** Because of the strong near-fields of SLRs, SHG enhancements (up to 450-times) occur by tuning fundamental wavelength, angle of incidence, and lattice constant of the arrays. (a) SHG enhancement from an SLR occurs near the Rayleigh anomaly corresponding to the fundamental wavelength of 810 nm for the 600 nm period array. Enhancement occurs symmetrically for positive and negative angles of incidence. The 810 nm wavelength corresponds to the red and blue lines in Figure 1d. (b, c) Enhanced SHG at different fundamental wavelengths for the 600 nm period silver nanoparticle array. The strong enhancements follow the angles of incidence that correspond to a Rayleigh anomaly induced SLR at the fundamental wavelength. The insets in panels c and d show the SHG intensity for different fundamental wavelengths at a single angle of incidence. All data acquired in the vertical–horizontal polarizer–analyzer configuration.

respectively. Here, SHG enhanced by SLRs results in conversion efficiencies comparable to previous studies on plasmonic nanostructures.<sup>66–68</sup> Structures explicitly designed for efficient SHG can achieve much higher conversion efficiencies.<sup>69</sup> However, for sensing applications, the conversion efficiency is not the most crucial factor. Rather, it is the relative contrast in SHG that is important. Therefore, SLRs provide an appealing platform for sensing given the dramatic variation in SHG between on and off resonance demonstrated in this work.

In both Figure 3 and Figure 4, the SHG signal is electric dipole allowed. The experimental geometries (polarizer-analyzer combinations and angles of optical incidence) address the nonzero tensor elements in eq 4. To evidence the higher-order contributions to SHG, we must select an experimental geometry that is electric dipole forbidden, specifically, one that addresses a zero tensor component in eq 4.

In Figure 5, we demonstrate the SLR enhancement of the higher-order contributions to SHG. Here, the experimental geometry of interest is the  $S_{IN}-S_{OUT}$  (vertical-vertical) polarizer-analyzer configuration at normal incidence. Under these conditions, within the electric dipole tensor, only the  $\chi_{YYY}$  tensor component is addressed. As we can see in eq 4, this component is zero, for our samples, that is, SHG from electric dipoles is forbidden. Figure 5a shows the SHG signal versus the angle of incidence for a fundamental wavelength of 870 nm

incident on the 600 nm period gold nanoparticle array. For the  $S_{IN}-S_{OUT}$  (vertical–vertical) polarizer–analyzer configuration, a distinct SHG peak can be seen (orange diamonds), centered at normal incidence, that is, precisely in the electric dipole forbidden configuration. This enhancement is attributable to the SLR near normal incidence. Indeed, 870 nm is very close to the normal incidence SLR, as demonstrated by both theory and experiment. Numerically, we calculate the SLR position at 872 nm, see Figure 2c. Experimentally, in the  $S_{IN}-P_{OUT}$  (vertical–horizontal) polarizer–analyzer configuration, which is electric dipole allowed, we observe two peaks (blue dots) that are similar to the data in Figure 4a and are only 2° apart in angle of incidence.

Additionally, Figure 5b unambiguously demonstrates that the SHG enhancement in the electric dipole forbidden configuration is due to the normal incidence SLR. The data were recorded for both gold nanoparticle samples, in the  $S_{IN}$ - $S_{OUT}$  (vertical-vertical) polarizer-analyzer configuration and at normal incidence, see Section S.2 of the Supporting Information for further details. For each sample, the SHG spectra peak (10 nm fwhm) is at the wavelengths of the SLRs, red-shifted with respect to the wavelength of Rayleigh anomaly.

Physically, there is a direct link between SLRs and the higher-order contributions to SHG. First, to avoid confusion, we point out that we do not discuss plasmonic quadrupolar



**Figure 5.** SLR causes an enhancement of the SHG quadrupolar contributions for the gold arrays. (a) For  $S_{IN}-P_{OUT}$  (dots), the SHG signal is attributable to electric dipolar contributions. The fundamental light is at 870 nm (at the Rayleigh anomaly) and the peaks correspond to the SLRs. For  $S_{IN}-S_{OUT}$  (diamonds), the signal peaks at normal incidence, where the higher-order contributions to SHG appear. (b) Measuring SHG spectra, for  $S_{IN}-S_{OUT}$  and at normal incidence SLR wavelength, for both the 600 and 580 nm period arrays. The blue and green solid lines indicate the Rayleigh anomalies for the 580 and 600 nm periodicities, respectively. Error bars represent the standard deviation from the mean average counts.

modes in the nanoparticle. As can be seen from eq 3, the quadrupolar contribution to the second harmonic polarization is proportional to gradients of the local electric field. At the SLR, such gradients of the local electric fields are very strongly pronounced, see Figure 2c. It should be pointed out that quadrupolar SHG can originate from the surface of the nanoparticles.<sup>70</sup>

Our analysis of the SHG results in Figure 5 is based on the assumption that we address the zero tensor component in eq 4, which implies four-fold (or isotropic) symmetry. However, small shape imperfections of the nanostructures can break the isotropy leading to the appearance of electric dipole allowed SHG at normal incidence. 71,72 Moreover, lattice defects could also lead to electric dipole allowed SHG. These hypothetical electric dipole contributions would usually be very small, but, in our experiments, they could be enhanced by the SLRs and become measurable. However, as can be seen in Figure 5a, the SHG signal for S<sub>IN</sub>-S<sub>OUT</sub> peaks at normal incidence and not at the angles corresponding to the SRLs, where electric dipole SHG attributable to surface lattice resonantly enhanced imperfections should have appeared  $(\pm 1^{\circ})$ . Therefore, the S<sub>IN</sub>-S<sub>OUT</sub> signal cannot be attributed to an SLR enhanced electric dipolar contribution to SHG.

In conclusion, we demonstrate SHG spectroscopy from SLRs, where the signal can be enhanced up to 450-times. We present both electric-dipole allowed (in Figure 4) and electric-dipole forbidden (in Figure 5) SHG resonances. We observe

SHG resonances as narrow as 5 nm fwhm, which indicates that a high FoM can be achieved, opening new avenues for chemical and biosensing applications. Moreover, the SHG technique is intrinsically surface-sensitive, which can lead to improved near-field surface sensing, especially using higherorder resonances that originate from gradients in plasmonic near-fields, see eq 2. Eq 2 also demonstrates how SHG can improve upon the bulk sensitivity of SLRs. This bulk sensitivity originates from far-field coupling between nanoparticles, and for electric dipole allowed SHG resonances, the sensitivity would additionally benefit from a power law dependence on the far-fields. It should also be pointed out that the SHG process occurs via virtual energy levels at ultrafast time scales.<sup>62</sup> This process could therefore enable ultrafast probes of the refractive index and could be useful for monitoring chemical reactions, for example, catalysis by the nanoparticles. To explore the limits of these applications, future work should focus on the importance of the environment surrounding the nanoparticle arrays.<sup>73,7</sup>

# ASSOCIATED CONTENT

## **Supporting Information**

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.nano-lett.8b03574.

Sample specifications, higher order contributions to SHG, experimental details, results for silver nanoparticle arrays, power dependence measurement (PDF)

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#### **Author Contributions**

T.O. and V.K.V. designed the research. D.W., J.G., and W.W. prepared the samples. D.C.H. performed the SHG experiments. C.K. and D.W. conducted numerical simulations. D.C.H. and V.K.V. analyzed the results. D.C.H. and V.K.V. wrote the first draft of the paper, and all authors contributed to the final text.

#### Notes

The authors declare no competing financial interest.

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