



## *Modelling Energy Technology Diffusion on Networks*

**Nick McCullen**

*School of Mathematics*

*University of Leeds*

& the Energy-Complexity project team.

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# *Modelling Energy Technology Diffusion on Networks*

*Introduction*

*Focus of the Case-Study*

*Complex Network Models*

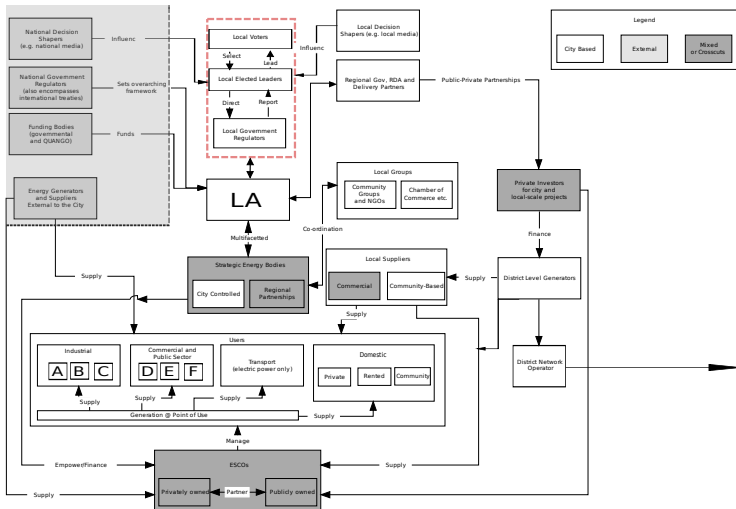
*Dynamical Models*

*Model Results*



# Introduction

## Can complexity science contribute to city energy policy?



# What is “Complexity Theory”?

## 1. Characteristics of a complex system:

- Multiple interacting individuals,
- interactions important to system level behaviour,
- macroscopic *emergent* phenomena,
  - coherence & pattern,
  - “unexpected” outcomes.
- *Universality*:
  - common behaviours in ‘unrelated’ systems,
  - identify basic underlying features.

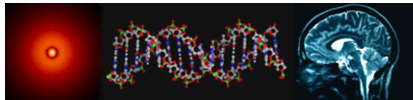
## 2. Tools include ABM, networks, dynamical systems. . .



# Measuring Complexity

*Level of Complexity*

Complex **System** or **Behaviour**?



**Complex behaviour  
from  
simple rules**



*Emergent  
behaviour*



**Order/Pattern  
from  
complexity**



# Modelling the Real World

- Would like to predict specific outcomes of *interventions*.
- Not generally possible in chaotic and complex systems,
  - can give generic behaviours,
  - test whether system conforms to expectations.
- Models include only *essential features* of system.
- Can test *sensitivity* to model details and initial conditions.



## Focus of the Case-Study

- Study interventions related to adoption of new technology or energy use strategies,
- mediated by social contacts between individuals (as well as through the media) <sup>1</sup>.
- This dissemination of technology or ideas can be studied using models of diffusion on networks.

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<sup>1</sup>e.g. see: R. Phillips and S. Rowley, *Bringing it home: Using behavioural insights to make green living policy work*, Green Alliance (2011).

## *Schemes Under Consideration*

1. Green Deal provider covers upfront costs of EE tech, paid back from the savings in energy bills;
2. Subsidy for installing EE out of LA budget;
  - word-of-mouth about savings achieved,
  - incentives such as “recommend a friend discounts”.
3. Smart meter installation;
  - effects of seeing own use compared to neighbours’.





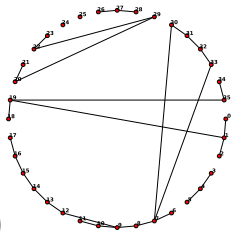
# Network Models

- Individuals, organisations, households, . . . , considered as *nodes* on a network.
  - Properties of nodes are associated with variables, e.g.:
    - ability to buy (income + subsidy),
    - willingness to buy (personal and social utility).
- *Links* ('edges') are drawn between connected individuals.
  - Information/influence passed along (weighted) edges.
- This is a *complex system* of interacting individuals.
- Dynamics of variables governed by equations (rules) based on own and neighbours' state.

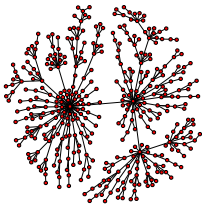


## Types of Model Network

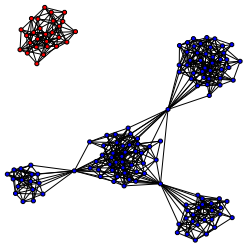
- Random networks constructed to give different qualitative features of real world interactions:



(a)



(b)



(c)

(a): *Small world* network with 20% rewiring of a regular lattice.

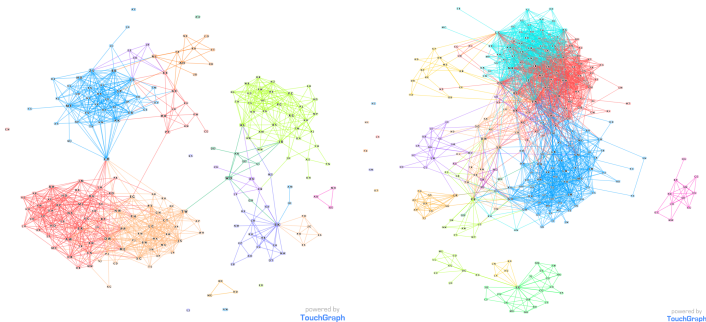
(b): Preferential attachment graph with a *scale-free* degree distribution.

(c): Simple model of weakly-connected communities.



## Real-World Social Networks

- Different types of social connection exist; these include:
  - geographical neighbours, distant friendships, family trees, *communities*.



*Figure:* Inter-friend contacts on the *Facebook* website.



# Community-Structured Networks

- **Communities** are sets of individuals which are more well connected internally than to the rest of the network <sup>2</sup>.
  - a distribution over a range of sizes exists,
- Most individuals will be connected to more than one group (work, leisure, children's school etc.).
- Varying degrees of overlap exist <sup>3</sup>.
- This creates the cobweb of highly inter-connected groups.

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<sup>2</sup>S. Fortunato and C. Castellano, *Community structure in graphs* (2007).

<sup>3</sup>G. Palla, I. Derényi, I. Farkas, and T. Vicsek. *Uncovering the overlapping community structure of complex networks in nature and society* (2005).



# *Dynamical Models*

Internal Dynamics could include the following factors:

- Rational cost-benefit analysis;
  - dynamical system on nodes,
  - defined decision criteria.
- Decisions based on influence crossing some threshold:
  - fixed number of friends or proportion of contacts.
- Could be probabilistic.
- Would likely have multiple parameters.



# *Social Dynamics and Diffusion Models*

- Many models exist for social dynamics <sup>4</sup>.
- We are more interested in technology adoption models:
  - Threshold models are often used:
    - individuals use the technology if a certain number or proportion of the neighbours are using it.
- Can quantify system “effectiveness” counting either:
  - number of individuals who have technology,
  - average opinion of technology.

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<sup>4</sup>C. Castellano, S. Fortunato, and V. Loreto. *Statistical physics of social dynamics* (2009).



## Models of Social Influences

Models weight individual's own preference relative to social influence <sup>5</sup>:

- *Utility* (benefit) of product to individual:

$$U = \alpha p + (1 - \alpha)s$$

*p*: personal utility: value of product to individual,

*s*: social utility: fraction of other individuals with technology,

*α*: relative weighting of personal to social value.

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<sup>5</sup>S.A. Delre, W. Jager, T.H.A. Bijmolt, and M.A. Janssen. *Will it spread or not? The effects of social influences and network topology on innovation diffusion* (2010)



## Personal Utility

Intrinsic to product and individual, could depend on:

- potential savings,
  - relative or absolute,
  - pay-back time;
- environmental credentials (may change),
- negative effects of barriers to adoption.

## Social Utility

- Data suggests individuals assign different relative value to personal contacts and society <sup>6</sup>.
  - someone buys when adoption within society and contact network are above respective thresholds,
  - individuals classed as early, majority or late adopters,

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<sup>6</sup>T.W. Valente. *Social network thresholds in the diffusion of innovations* (1996).





## Aspects to Include in Models

1. Use community-structured networks with wide degree-distribution,
2. Weight links of different types,
  - strength of influence of different individuals.
3. Use distributions of behaviour archetypes:
  - thresholds for personal and social utility, as well as prevalence in society in general (via media).
4. Market feedback effects such as *learning-curves*, whereby the unit price reduces with market penetration <sup>7</sup>.

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<sup>7</sup>S. Cantono and G. Silverberg. *A percolation model of eco-innovation diffusion: the relationship between diffusion, learning economies and subsidies*. (2009)



## Model Specifications

1. The individual households are nodes on the network.
2. Associated state variable  $x_i = 0, 1$ :  
0: not purchased, 1: purchased,
  - can also include continuous “opinion” region.
3. Weighted “value” of an EE product to individual is bundled into a *utility* variable,  $U_i$
4. Threshold for adoption  $\theta_i = C_i - I_i$ ,  
 $C$ : *perceived* “costs”,  $I$ : incentives.



## Model Specifications

5. At each time-step evaluate *utility* of product:

$$U_i = \alpha p_i + \beta s_i + \gamma m$$

$$s_i = \sum_j^{K_i} \rho_{ij} x_j / \sum_j^{K_i} \rho_{ij}, \quad m = \sum_{k=1}^N \sigma_k x_k / \sum_k^N \sigma_k.$$

6. If  $U_i \geq \theta_i$  :  $x_i \rightarrow 1$ .

- Time-scales for updating opinion ( $\tau_1$ ) and making purchases ( $\tau_2$ ) may be different:

- $\tau_1$  opinion updated after interacting with friends and taking in media (e.g. weekly),
- $\tau_2$  purchase decisions made less frequently (motivated by monthly pay-day, weather, prices, breakages etc.).



## *Modelling Interventions*

- Measure diffusion with and without a given intervention.
- Compare possible interventions, e.g.:
  1. street-by street targeting for installation;
  2. targeting communities and opinion leaders,
  3. 'random' installation,
    - e.g. via advertising campaign;
  4. 'word-of-mouth' propagated installation,
    - strengthening network ties to improve communication.
    - e.g. incentive to "recommend to a friend".

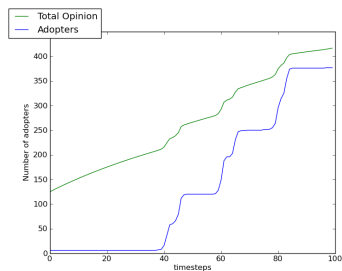
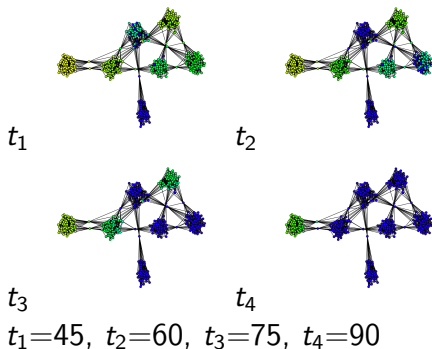


## *Results of Models*

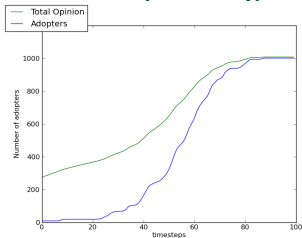
- Vary parameters to study sensitivity of uptake:
  - network types and parameters,
  - weights and thresholds.
- Simulate many randomisations to investigate stability of results.
- Study various “interventions”:
  - initial conditions,
  - “incentives” to reduce thresholds etc.



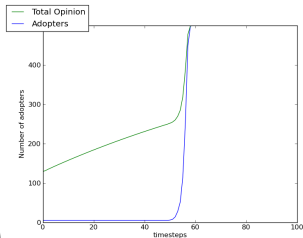
# Example: Weighted “opinion” Model on Community Network



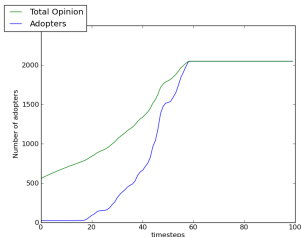
# Comparing Different Transitions



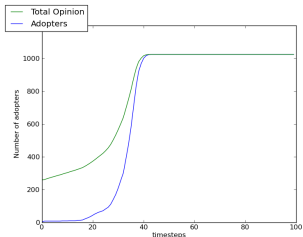
(a)



(b)



(c)



(d)

- (a): Weakly connected communities. (b): Inter-community *bridges*.  
 (c): Large, weakly bound groups. (d): Distributions of thresholds.



## *Possible Conclusions*

In this simple example:

- Fast transitions are seen wherever tightly bound communities interact with more than a few others.
- Transition to technology adoption can be slowed when:
  - communities are not tightly bound,
  - communities do not interact strongly,
  - a lot of individuals have high resistance to uptake.
- To ensure a fast transition increase:
  - strength of links,
  - inter-community ties,
  - information about whole system.





## Potential Recommendations

- Increase network ties for swift transition:
  - incentivise people to spread the word, e.g. by:
    - money back for recommending a friend,
    - money off for groups investing together.
- Make energy more visible to consumers, e.g.:
  - smart meters, showing neighbourhood averages, time-averaged individual (monthly/weekly) spend,
  - potential savings from EE measures,
  - show prevalence of EE measures in society to encourage people into the 'trend',
  - attract *early adopters* by predicting future trends.

