Atomic-Scale Insight into LaFeO₃ Perovskite: Defect Nanoclusters and Ion Migration

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Atomistic simulation techniques are employed to investigate the energetics of defect formation, dopant– defect association, and ion migration in orthorhombic LaFeO₃ in relation to electrochemical applications. Point defect calculations suggest that intrinsic Schottky or Frenkel disorder is not significant. The results of redox reaction calculations suggest that at high oxygen partial pressures doped LaFeO₃ will oxidize with the formation of holes, contributing to the p-type electronic conductivity that is observed experimentally. The binding energies of selected dopant-vacancy clusters are also derived. A minimum in the binding energy was found for Sr^{2+} on the La³⁺ site, which would be beneficial to oxide ion conductivity. Larger complex defect clusters within 2D and 3D configurations have also been considered as they may be important as precursors to possible short-range ordering or "nanodomain" formation. A number of different pathways for oxygen migration by a vacancy mechanism are investigated; the lowest activation energy for this process is via a curved path between oxygen sites. We also examine cation-vacancy transport in LaFeO₃ and determine the migration energies for La and Fe migration.

1. Introduction

The development of cathode materials for solid oxide fuel cells (SOFCs) has largely focused on perovskite oxide materials with chemical formula ABO₃, containing La and Sr on the A sites and transition metals on the B sites. Strontium-doped lanthanum manganate (LSM), $La_{1-x}Sr_xMnO_3$, is the most commonly used cathode material for zirconia-based SOFCs.¹ A key requirement for the development and application of SOFC technologies is to reduce the operating temperature to ≤ 700 °C². However, at lower temperatures, cell performance may be affected by reduced electrocatalytic reaction at the cathode. In order to improve cathode performance at lower temperatures a number of substituted perovskites, such as lanthanum ferrites, have been considered.^{3,4} They have the advantage of higher catalytic activity at lower temperatures, resulting in an overall superior electrochemical performance compared to LSM.⁵

Over a wide range of temperatures and pressures LaFeO₃ has been shown to be a mixed oxide ion and electron hole conductor.^{6,7} The doped system $La_{1-x}Sr_xFeO_{3-\delta}$ has been extensively studied^{8–10} and found to have good p-type electrical conductivity¹¹ (>100 Scm⁻¹); the high electronic and ionic conductivities combined with thermal stability¹² makes them candidate materials as cathodes for SOFCs. However, the defect and ion transport properties of the doped LaFeO₃ system are not fully understood.

In this study, orthorhombic LaFeO₃, the end member of the solid solution $La_{1-x}Sr_xFeO_{3-\delta}$, which is stable up to approximately 1000 °C,¹³ has been probed at the atomic level by employing advanced computer simulation techniques. In this way, the defect chemistry and the mechanism and energetics of ion migration within these perovskite-type materials have been investigated. In addition to this, the substitution of a range of dopants has been investigated together with the energetics of dopant-vacancy clusters.

2. Simulation Methods

The computational techniques used in this work, embodied in the GULP code,¹⁴ are well established and have been reviewed in detail elsewhere.^{15,16} The calculations are based upon the Born model of a solid which includes a long-range Coulombic interaction between each pair of ions *i* and *j*, and a short-range Buckingham term to model overlap repulsions and van der Waals forces. The short-range interactions are modeled with a Buckingham potential of the form

$$V_{ii}(r) = A_{ii} \exp(-r/\rho_{ii}) - C_{ii}/r^6$$
(1)

where A_{ij} , ρ_{ij} , and C_{ij} are the potential parameters and r is the interatomic separation.

The electronic polarizability of the ions is described by the shell model,¹⁷ which has been found to be effective in simulating the dielectric and lattice dynamical properties of metal oxides.¹⁶ Using this model, the deformable ion is represented as a massive core connected by a harmonic spring to a massless, but chargebearing, shell. The calculation of defect formation and migration energies utilizes the two-region Mott-Littleton methodology¹⁸ for accurate modeling of defective lattices. This is performed such that lattice relaxation occurs about the point defect, or migrating ion, so that the crystal is not considered as a rigid lattice. It employs a method in which the crystal lattice is partitioned into two main regions. Ions in the spherical inner region surrounding the defect are relaxed explicitly, with each ion allowed to relax from its ideal position in order to minimize forces. In the remainder of the crystal, where the defect forces are relatively weak, only implicit polarization of each sublattice is considered, instead of individual ions. A radius of 12 Å was used for the inner region and this typically corresponded to around 550 ions.

3. Results and Discussion

3.1. Structural Modeling. Unlike the cubic perovskite structure, which only has one distinct oxygen site, the orthor-

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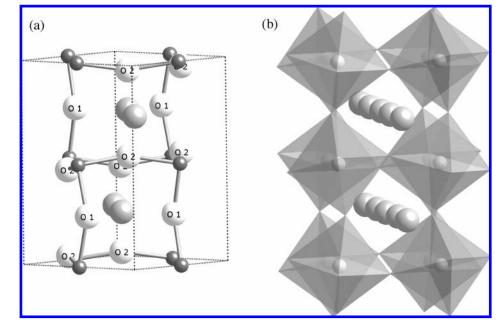


Figure 1. (a) Unit cell of orthorhombic LaFeO₃ showing the two oxygen sites, O1 and O2; (b) Structure of orthorhombic LaFeO₃ showing the tilted FeO₆ octahedra with the La ions occupying the cavities between the octahedra.

TABLE 1: Interatomic	Potential	Parameters f	or LaFeO ₃
and Dopant Species			

(i) Short-Range Potential			
interaction	A/eV	$ ho/ m \AA^6$	C/eV Å ⁶
La ³⁺ ····O ²⁻	1545.21	0.3590	0
Fe ³⁺ ····O ²⁻	1156.36	0.3299	0
$O^{2-} \cdots O^{2-}$	22764.30	0.1490	43.0
$Mg^{2+} \cdots O^{2-}$	821.60	0.3242	0
$Ca^{2+}O^{2-}$	1228.90	0.3372	0
$Sr^{2+}\cdots O^{2-}$	1400.00	0.3500	0
Ga ³⁺ ····O ²⁻	2901.12	0.2742	0
$Mn^{3+} \cdots O^{2-}$	1267.50	0.3214	0
$Co^{3+O^{2-}}$	1329.82	0.3087	0
	(ii) Shell Mo	odel ^a	
species	Y/e		$k/eV Å^{-2}$
La ³⁺	-0.25		145.0
O^{2-}	-2.24		42.0
Mg^{2+}	2.00	99999	
Ca ²⁺	1.26	34.00	
Sr^{2+}	1.33	21.53	
Ga ³⁺	3.00	99999	
Mn ³⁺	3.00		95.00
Co^{3+}	2.04		196.30

 ^{a}Y and k refer to the shell charge and harmonic force constant, respectively.

hombic phase of LaFeO₃ has two nonequivalent oxygen sites, O1 and O2, as shown in Figure 1a. The structure can be viewed as a network of tilted, corner-sharing FeO₆ octahedra with the La cations occupying the cavities between the octahedra as shown in Figure 1b.

The short-range potential parameters and the shell-model parameters for O^{2-} and La^{3+} used in this study (listed in Table 1) were those derived by Cherry et al.¹⁹ in a study of LaBO₃ perovskites (B = Cr, Mn, Fe, and Co) by empirical fitting to observed structural properties. The same potential parameters were used for the Fe³⁺ species, but it was assumed to be nonpolarizable and treated simply as a rigid ion. Using this set of interatomic potentials it was possible to reproduce the orthorhombic structure of LaFeO₃. The calculated bond distances, lattice parameters, and their comparison with experi-

TABLE 2: Calculated and Experimental Properties of Orthorhombic LaFeO3

	(i) Unit-C	ell Parameters		
parameter	calculated/Å	experimentalª/Å	difference/%	
а	5.600	5.565	0.63	
b	7.862	7.855	0.08	
С	5.557	5.556	0.01	
(ii) Bond Lengths				
distance				
bond separation	n calculated/Å	experimental ^a /Å	difference/Å	
La-O1	2.555	2.593	-0.038	
La-O2	2.438	2.651	-0.213	
Fe-O1 2.007 2.002 0.0			0.005	
Fe-O2	2.013	2.008	0.005	
01-01	3.447	3.433	0.014	
02-02	3.363	3.315	0.048	

a Falcon et al.20

mental values²⁰ are listed in Table 2. It can be seen that there is good agreement between experimental and simulated structures, thus supporting the validity of the potentials used for the subsequent defect and migration calculations.

The interatomic potentials for the dopant species (Table 1) were those of the corresponding binary metal oxides,²¹ as they are consistent with the above derived potentials and have successfully been applied to similar studies of dopant substitution in other perovskites.^{19,22,23}

3.2. Intrinsic Atomic Defects. The energies of isolated intrinsic defects (interstitials and vacancies) in orthorhombic LaFeO₃ were first evaluated. It is found that the difference in energy between an O1 and O2 oxygen vacancy is only 0.04 eV. This is not surprising as they occupy similar environments within the orthorhombic LaFeO₃ structure as can be seen in Figure 1a.

Frenkel disorder, full Schottky disorder and partial Schottky disorder energies were calculated by combining the individual defect energies and the lattice energies where appropriate. These defect reactions are given below (eqs 2–7) and the corresponding energies listed in Table 3.

J. Phys. Chem. C, Vol. 112, No. 12, 2008 4457

TABLE 3: Calculated Energies for Frenkel- and Schottky-Type Disorder in Orthorhombic LaFeO₃

disorder	total energy/eV	energy/eV per defect
La Frenkel	19.57	9.79
Fe Frenkel	17.13	8.57
O Frenkel	8.49	4.25
LaFeO3 full Schottky	17.49	3.60
La ₂ O ₃ partial Schottky	15.15	3.03
Fe ₂ O ₃ partial Schottky	18.50	3.70

Lanthanum Frenkel disorder:

$$La_{La}^{X} \leftrightarrow V_{La}^{\prime\prime\prime\prime} + La_{i}^{\bullet\bullet\bullet}$$
 (2)

Iron Frenkel disorder:

$$Fe_{Fe}^{X} \leftrightarrow V_{Fe}^{\prime\prime\prime\prime} + Fe_{i}^{\bullet\bullet\bullet}$$
 (3)

Oxygen Frenkel disorder:

$$O_0^X \leftrightarrow V_0^{\bullet \bullet} + O_i^{\prime\prime}$$
 (4)

LaFeO₃ full Schottky disorder:

$$La_{La}^{X} + Fe_{Fe}^{X} + 3O_{O}^{X} \leftrightarrow V_{La}^{\prime\prime\prime\prime} + V_{Fe}^{\prime\prime\prime\prime} + 3V_{O}^{\bullet} + LaFeO_{3}$$
(5)

La₂O₃ partial Schottky disorder:

$$2\mathrm{La}_{\mathrm{La}}^{\mathrm{X}} + 3\mathrm{O}_{\mathrm{O}}^{\mathrm{X}} \leftrightarrow 2\mathrm{V}_{\mathrm{La}}^{\prime\prime\prime} + 3\mathrm{V}_{\mathrm{O}}^{\bullet\bullet} + \mathrm{La}_{2}\mathrm{O}_{3}$$
(6)

Fe₂O₃ partial Schottky disorder:

$$2Fe_{Fe}^{X} + 3O_{O}^{X} \leftrightarrow 2V_{Fe}^{\prime\prime\prime} + 3V_{O}^{\bullet\bullet} + Fe_{2}O_{3}$$
(7)

where, in Kröger–Vink notation,²⁴ $O_i^{//}$, La^{•••}, and Fe^{•••} represent oxygen, lanthanum, and iron interstitials, respectively, V_O^{\bullet} , $V_{La}^{///}$, and $V_{Fe}^{///}$ represent oxygen, lanthanum, and iron vacancies, respectively, and the superscripts • (positive), / (negative), and x (neutral) indicate the charge of the defect relative to the normal site.

The Frenkel disorder energies are much higher than the other disorder energies. The results suggest that interstitials would be unlikely intrinsic defects (as would be expected in a closepacked perovskite structure). The lowest energy is for the La₂O₃ Schottky-type disorder. However, the Schottky energies are still relatively high, suggesting that we would not expect intrinsic Schottky or Frenkel disorder to dominate the defect chemistry of undoped stoichiometric LaFeO3 except at very high temperatures. This is consistent with the defect models proposed by Mizusaki et al.¹¹ in a study of $La_{1-x}Sr_xFeO_{3-\delta}$ (x = 0.0, 0.1, and 0.5). It is interesting to note that Wærnhus et al.^{7,25} have investigated the non-stoichiometric system $La_{1-v}FeO_{3-\delta}$; they proposed that the *p*-type conductivity at high oxygen partial pressures is due to the formation of Schottky defects at high annealing temperatures (>1000 °C) and that the number of cation vacancies, which act as electron acceptors and introduce p-type conductivity, will increase with the oxygen partial pressure; this issue warrants further investigation.

3.3. Redox Reactions. An understanding of the redox behavior of these materials is critical for defining the conditions in which various conductivity regimes may be exploited. Mizusaki et al.¹¹ have described the electronic conductivity as localized electrons and holes hopping between the Fe ions of different valence states. Studies on the electronic properties of LaFeO₃ suggest that the *n*-type conductivity at low oxygen

partial pressures is due to reduction of Fe^{3+} to Fe^{2+} and the formation of oxygen vacancies.

Experimental determination and interpretation of the defect equilibria are complicated due to the number of possible conducting species (oxide ion, electron or hole). Atomistic simulation is therefore a useful tool in assisting the interpretation of experimental data, as has been shown previously.²²

Using an approach that has been successfully applied to other transition metal oxides,²⁶ the electronic defects, electrons (e') and holes (h[•]), were treated as localized species (small polarons). The hole species was assumed to reside on either an oxide ion $(O^{2-} \rightarrow O^{-})$ or iron ion $(Fe^{3+} \rightarrow Fe^{4+})$. Oxidation and reduction in undoped LaFeO₃ were considered (eqs 8–11), and the energies of these processes compared with that of the doped system in order to determine the most likely oxidation and reduction mechanisms. For the undoped system, the following reactions were considered:

(i) Oxidation to give a metal deficient material:

$$\frac{1}{2}O_2(g) + \frac{2}{3}Fe_{Fe}^x \rightarrow \frac{2}{3}V_{Fe}^{\prime\prime\prime} + 2h^{\bullet} + \frac{1}{3}Fe_2O_3 \qquad (8)$$

or

$$\frac{1}{2}O_2(g) + \frac{2}{3}La_{La}^x \rightarrow \frac{2}{3}V_{La}^{\prime\prime\prime} + 2h^{\bullet} + \frac{1}{3}La_2O_3 \qquad (9)$$

With regard to the hole species, our calculations found that the formation of an O^- species is more favorable than Fe⁴⁺ formation by about 3 eV, suggesting that holes are more likely to be centered on oxygen sites, although we recognize that there will be some degree of Fe(3d)–O(2p) mixing.²⁷

(ii) Reduction to give an oxygen deficient material was the only one considered, as introduction of cation interstitials has been shown to be an energetically unfavorable process:

$$\mathbf{O}_{\mathbf{O}}^{\mathbf{x}} \rightarrow \mathbf{V}_{\mathbf{O}}^{\bullet\bullet} + \frac{1}{2} \,\mathbf{O}_{2} \,(\mathbf{g}) + 2\mathbf{e}^{\prime} \tag{10}$$

(iii) We also examined the energetics of disproportionation of two Fe^{3+} ions to Fe^{2+} and Fe^{4+} ions according to the equation:

$$2\mathrm{Fe}_{\mathrm{Fe}}^{\mathrm{x}} \rightarrow \mathrm{Fe}_{\mathrm{Fe}}^{\bullet} + \mathrm{Fe}_{\mathrm{Fe}}^{/} \tag{11}$$

 M^{2+} dopants may be substituted into the LaFeO₃ structure in order to introduce vacancies at oxygen sites. At high oxygen partial pressures, doping can also be used to affect electronic conductivity by "filling" of the oxygen vacancies to create holes (h•). The energetics of hole formation in doped LaFeO₃ were examined via the following reaction:

$$\frac{1}{2}O_2 + V_0^{\bullet\bullet} \to O_o^x + 2h^{\bullet}$$
(12)

The energies of the various redox processes, summarized in Table 4, were calculated using the appropriate free ion terms together with the point defect energies and the relevant lattice energies.

The results indicate that the most favorable redox process is oxidation of doped LaFeO₃ with the formation of holes (eq 12). The calculations therefore suggest that p-type conduction would be exhibited in the doped LaFeO₃ system at high oxygen partial pressures, as found experimentally.^{4,11} This process is important for mixed ionic-electronic conductivity in doped LaFeO₃ and its potential use in SOFC cathodes or ceramic membranes. In the undoped stoichiometric system, however, both oxidation and

TABLE 4: Calculated Energies of Redox Reactions

process	eq	energy/eV per electronic defect ^a
oxidation	8	5.94
oxidation	9	5.38
reduction	10	4.69
disproportionation	11	5.23
oxidation	12	2.86

^{*a*} Calculated using $\Delta E = 9.87 \text{ eV}$ for $1/2O_2 \rightarrow O^{2-}$; O hole (h[•]) term = 7.65 eV; Fe hole (h[•]) term = 10.56 eV; Fe electron (e') term = -0.11 eV.

reduction energies indicate relatively unfavorable processes. The calculated energy for disproportionation suggests that this too is an unlikely process in LaFeO₃, in contrast to some Co-based perovskites.²⁸

3.4. Dopant-Vacancy Association. The oxygen vacancies which are formed as a result of acceptor-doping of ABO₃ perovskites have been shown to be crucial to high oxygen conductivity in perovskite materials.²⁹ Misuzaki et al.³⁰ have pointed out that the diffusivity of oxygen in La perovskites is controlled by the oxygen vacancy concentration. Interactions between dopant ions and their charge compensating defects can lead to the formation of distinct clusters which can trap the migrating species. A recent review of fast oxygen transport in acceptor-doped oxides³¹ concluded that there is a dopant concentration dependence in the conductivity and the activation enthalpy of doped oxides. It has also been noted that there is a minimum in the activation.

In fluorite-structured oxides (e.g., doped CeO₂ and ZrO₂), interactions between dopant ions and their oppositely charged compensating defects lead to the formation of defect clusters or associates.^{31,32} This adds a binding (association) energy term to the conduction activation energy. Dielectric relaxation measurements of acceptor-doped KTaO₃ and CaTiO₃ perovskites by Nowick et al.³³ also provide evidence of dopant-vacancy pairs.

A series of calculations on defect clusters in orthorhombic $LaFeO_3$ were carried out to investigate interactions between oxygen vacancies and dopant cations, which are not fully understood in this material. For this task, the simulation methods used here are well suited as they model accurately Coulomb and polarization energies, which are the predominant terms in any local association process.

Work on the LaGaO₃ perovskite³⁴ suggests that in addition to the electrostatic attraction, the elastic energy term due to distortion of the crystal lattice upon introduction of differentsized cations contributes to cluster formation, as found in fluorite oxides.

In this study, a number of different dopant-vacancy configurations (pairs and trimers) were simulated to ascertain whether any degree of "trapping" of the oxygen vacancies by the dopant species might occur. At higher dopant concentrations, there is the possibility that an oxygen vacancy may be associated with one or more dopant cations; therefore, the association of both charged dimers ($M'V_o^{\bullet}$) and neutral trimers ($M'V_o^{\bullet}M'$) has been studied. The configurations that were considered for the pair clusters are comprised of an M^{2+} or M^{3+} dopant substitutional and either an O1 or O2 oxygen vacancy at nearest neighbor sites. For the neutral trimer clusters, two M^{2+} dopant substitutionals and the nearest neighbor O1 or O2 vacancy were considered.

TABLE 5: Calculated Binding Energies for M^{2+} Dopant-Oxygen Pair-Clusters and M^{2+} Neutral Trimer Clusters $(M'V_0^{\circ}M')$ at (a) the La Site and (b) the Fe Site, and (c) M^{3+} Dopant-Oxygen Pair-Clusters at the Fe Site in LaFeO₃

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(a) M ²⁺ on La Site				
dopant	mean binding e	mean binding energy/eV per defect		
M ²⁺ and O1 vacancy	$(M_{La}^{/}V_{o}^{\bullet \bullet})$ pair	$(M_{La}^{\prime}V_{o}^{\bullet\bullet}M_{La}^{\prime})$ trimer		
Ca^{2+} Sr ²⁺ M ²⁺ and O2 vacancy	-0.22 -0.17	-0.35 -0.33		
${Ca^{2+} \over Sr^{2+}}$	-0.33 -0.31	-0.34 -0.32		
(b) M ²⁺ on Fe Site			
dopant	mean binding	energy/eV per defect		
M ²⁺ and O1/O2 vacancy	$(M_{Fe}^{\prime}V_{o}^{\bullet \bullet})$ pair	$(M_{Fe}^{\prime}V_{o}^{\bullet \bullet}M_{Fe}^{\prime})$ trimer		
Mg ²⁺	-0.54	-0.69		
(c) M^{3+} on Fe site				
dopant	mean binding	energy/eV per defect		
M ³⁺ and O1/O2 vacancy	$(M_{Fe}^{x}V_{O}^{\bullet \bullet})$ p	air		
Ga^{3+} Mn ³⁺ Co ³⁺	$0.17 \\ 0.00 \\ -0.10$			

The cluster binding energies (E_{bind}) were calculated using the general relation:

$$E_{\text{bind}} = E_{\text{cluster}} - \left(\sum_{\text{component}} E_{\text{isolated defect}}\right)$$
(13)

where E_{cluster} is the energy of the cluster and E_{isolated} is the energy of the individual component defects. For example, the binding energy for the $(Mg'_{\text{Fe}}V_0^{\bullet})$ pair cluster is derived as follows:

$$E_{\text{bind}} = E(\mathrm{Mg}_{\mathrm{Fe}}^{\prime} \mathrm{V}_{\mathrm{o}}^{\bullet \bullet}) - [E(\mathrm{Mg}_{\mathrm{Fe}}^{\prime}) + E(\mathrm{V}_{\mathrm{o}}^{\bullet \bullet})] \qquad (14)$$

A negative value indicates that the cluster is stable with respect to the isolated defects.

In this study we focused on dopants typically used in these systems, namely Ca^{2+} and Sr^{2+} on the La^{3+} site, and Mg^{2+} , Ga^{3+} , Mn^{3+} , and Co^{3+} on the Fe³⁺ site. The results of the calculations for these selected dopants are summarized in Table 5.

It can be seen from Table 5 that the calculated binding energies for M^{2+} dopant pair and trimer clusters all indicate a degree of association at the La or the Fe sites, ranging from -0.17 to -0.69 eV. The smallest binding energies for M^{2+} dopant pair clusters are calculated for Sr^{2+} and Ca^{2+} at the La site and an O1 vacancy. Incorporation of Sr into LaFeO₃ would be expected to increase the conductivity owing to the increase in vacancy concentration, and a low binding energy would be a major factor in promoting the free oxygen vacancy population. High oxygen diffusivity with increasing levels of Sr^{2+} substitution is reported by Ishigaki,¹⁰ and other workers have found that the oxygen diffusivity in La_{1-x}Sr_xFeO_{3- δ} reaches a maximum at $x = 0.3^9$ or $0.5.^{35}$

The results of these calculations also suggest that Mg has a stronger tendency to "trap" migrating oxygen vacancies than the Sr dopant and that at high Mg doping levels the conduction activation energy is likely to increase. This has been shown to be the case by Haavik et al. for LaGaO₃.³⁶ Their defect model has been used to rationalize the temperature-dependent con-

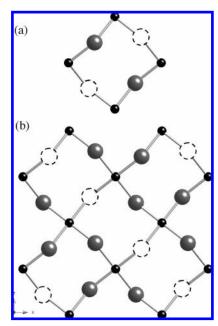


Figure 2. Views down [010] of 2D arrays of neutral Mg^{2+} -vacancy clusters: (a) $4Mg'_{Fe}2V_{o}^{\bullet\bullet}$ (b) $12Mg'_{Fe}6V_{o}^{\bullet\bullet}$ (black spheres and open dashed circles represent Mg dopant ions and oxygen vacancies, respectively).

ductivity of LaGaO₃ and derive a defect association enthalpy ($\approx 0.8 \text{ eV}$) of the same order as our calculated binding energy for LaFeO₃.

The calculated binding energies for selected M3+ dopant pair clusters $(M_{Fe}^{x}V_{O}^{\bullet\bullet})$ on the Fe site are also presented in Table 5. These isovalent substitutionals have no effective charge (i.e., relative to the host Fe³⁺ lattice ions). With respect to acceptor dopants, the population of oxygen vacancies would be dependent upon the M²⁺ dopants, e.g., Sr²⁺, already introduced into the lattice. The results indicate a very small degree of association for Co^{3+} . Since the binding energy is dependent on the ion size mis-match between host and dopant,³¹ these results are not unexpected as the ionic radii of Mn³⁺, Ga³⁺, and Co³⁺ are very close to that of Fe³⁺. It is worth noting that the ionic radius of Mn³⁺ is almost identical to that of Fe³⁺, and the calculated binding energy for the $(Mn_{Fe}^{x}V_{O}^{\bullet \bullet})$ cluster is zero. We should note that similar small binding energies are found for Gd³⁺ and Nd³⁺ on the La site, again indicating the importance of elastic strain effects.

3.5. Complex Mg²⁺-Vacancy Clusters. Our results for Mg²⁺ dopant pair and trimer clusters suggest the importance of defect-dopant association in relation to conductivity studies. Although simple pair clusters may dominate in the low concentration regime, it is thought that at higher dopant levels more complex defect clusters come into play and may be related to possible short-range ordering.³⁷

We have examined the energetics of larger clusters, focusing on Mg on the Fe site with oxygen vacancies at nearest neighbor sites. Neutral configurations based on $(nMg'_{Fe} n/2V_{o}^{\bullet\bullet})$ were considered, both for two-dimensional (2D) and three-dimensional (3D) clusters with the number of Mg²⁺ dopant ions (*n*) ranging from 2 to 16. Examples of selected 2D and 3D clusters are shown in Figures 2 and 3, respectively. The binding energies are derived by the same methodology described in eqs 13 and 14. The calculated binding energies for all of the configurations examined are presented in Figure 4 as a function of the number of Mg²⁺ ions in the cluster.

All of the clusters show relatively favorable binding energies with the magnitude varying for the different configurations. The

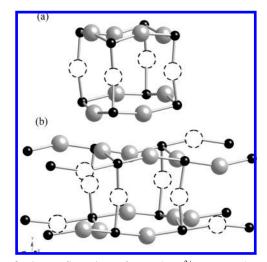


Figure 3. 3D configurations of neutral Mg²⁺-vacancy clusters: (a) $8Mg'_{Fe}4V^{\bullet}_{o}$ (b) $16Mg'_{Fe}8V^{\bullet}_{o}$ (black spheres and open dashed circles represent Mg dopant ions and oxygen vacancies, respectively).

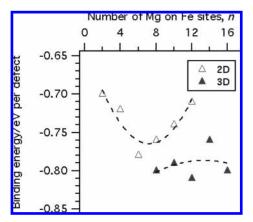


Figure 4. Calculated binding energies for 2D and 3D configurations of neutral $Mg_{2^+}^{2+}$ -vacancy clusters $(nMg_{Fe}^{\prime}n/2V_o^{*})$ as a function of the number of Mg^{2+} ions, *n*. Lines are a guide to the eye only.

strongest binding energy is found for the $(12Mg'_{Fe}6V_o^{\bullet})$ 3D configuration and in general the 3D structures show greater stability than the 2D arrays. The results suggest that complex nanoscale clusters such as $(12Mg'_{Fe}6V_o^{\bullet})$ or $(16Mg'_{Fe}8V_o^{\bullet})$ may form at high dopant concentrations and possibly be important as precursors to possible short-range ordering or "nanodomain" formation. In this context, in a study of LaGaO₃, Huang et al.³⁸ have suggested that dopant ions such as Mg²⁺ may act not only as traps for isolated oxygen vacancies, but also as nucleating centers for the formation of ordered vacancy clusters. Such defect clusters in doped LaFeO₃ warrant further structural study.

3.6. Oxide-Ion Migration. The presence of the two nonequivalent O1 and O2 oxygen sites in orthorhombic LaFeO₃ means that three possible vacancy migration pathways can be identified. The energy profiles for oxide ion migration were mapped out by calculating the defect energy of the migrating ion at intermediate sites between adjacent oxygen vacancies, allowing relaxation of the lattice ions at each position. In the saddlepoint configuration, the migrating oxide ion must pass through the opening of a triangle defined by two La³⁺ ions and one Fe³⁺ ion (Figure 5). Significant outward relaxation of these cations away from the migrating oxide ion is found. The simulations indicate the importance of local lattice relaxation effects and that the saddlepoint cannot be treated purely as a structural gap of hard-sphere ions.

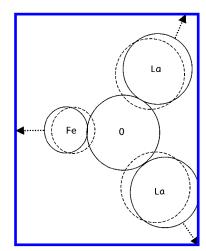


Figure 5. Saddlepoint configuration for oxide ion migration indicating the relaxation of the surrounding cations (solid lines). Dashed circles represent the unrelaxed positions of the cations.

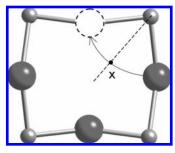


Figure 6. Schematic representation of the calculated pathway (curved line) of oxide ion migration between occupied and vacant O2 sites. The position of the saddlepoint is shown with a cross. Small gray spheres represent Fe ions.

TABLE 6: Calculated Migration Energy (E_m) for Oxide Ion Migration in LaFeO₃ and Total Calculated Activation (E_a) in Sr-Doped LaFeO₃

migration pathway	separation/ Å	calculated E _m /eV	Sr binding energy term/ eV	total calculated E_{a}/eV
01-01	3.43	2.13	0.17	2.30
01-02	2.80	0.44	0.26	0.70
02-02	2.80	0.50	0.34	0.84

For oxygen migration between two O2 sites or between an O1 and O2 site, it was found that the lowest energy pathway was a curved path, as shown in Figure 6, away from the octahedral edge, as has been found previously for oxygen migration in cubic LaGaO₃ and other perovskite oxides.^{15,22,39} Subsequent neutron scattering and diffraction studies⁴⁰ have provided evidence for our predicted curved path. However, for oxygen migration between two O1 vacancies, the lowest energy migration pathway was found to be a direct linear route between the two sites. The results (Table 6) clearly show that migration between O1 sites is extremely unlikely, but a pathway linking O2 sites or between O2 and O1 sites with a migration energy, $\Delta E_{\rm m}$, of 0.5 eV is energetically very favorable.

It is important to stress that the calculated migration energies relate purely to migration of an oxygen vacancy and do not include a binding term. The values calculated here do not take into account the dopant-vacancy association which may contribute to the observed activation energies. Inclusion of the binding energy term in the calculated energy for oxygen migration in Sr-doped LaFeO₃ results in a calculated activation energy of between 0.70 and 0.84 eV (Table 6).

TABLE 7: Reported Experimental Activation Energies for Oxide Ion Conduction in $La_{1-x}Sr_xFeO_{3-\delta}$

x	$E_{\rm a}/{ m eV}$	temp. range/°C	ref
0.0	0.77	900-1100	41
0.1	0.88	900-1100	10
0.1	1.17	850-1050	9
0.2	1.67	850-1050	9
0.3	1.80	850-1050	9
0.4	1.56	850-1050	9
0.2	0.67	750-950	35
0.4	0.67	750-950	35
0.5	0.70	750-950	35

Activation energies for oxide ion transport via vacancy migration determined experimentally at low oxygen partial pressures and 950 °C range from 0.67 eV in La_{1-x}Sr_xFeO_{3- δ} for 0.2 $\leq x \leq 0.5^{35}$ to 0.77 eV for LaFeO₃.⁴¹These results are consistent with a model proposed by Haavik et al.³⁶ for LaGaO₃ in which they rationalize the temperature dependence of conductivity in terms of dopant-oxygen vacancy clusters.

Patrakeev et al.³⁵ have reported that at low oxygen partial pressures the oxide ion conductivity increases to a maximum value at x = 0.5 but that the activation energy for ion conductivity does not depend on the Sr content until x > 0.5, after which it increases with increasing Sr content. This increase in activation energy was explained in terms of vacancy ordering, which decreases the population of oxygen vacancies available for oxygen transport.

We recognize that direct comparison between the migration energies calculated here and the experimental activation energies (E_a) is not straightforward since the E_a values (listed in Table 7) from a range of conductivity studies on both LaFeO₃ and La_{1-x}Sr_xFeO_{3- δ} show significant variation. This may reflect differences in the synthesis conditions and phase purity or the method of determination and analysis of conductivity data.

Finally, we investigated the possibility of association between oppositely charged lanthanum and oxygen vacancies which could occur in A-site deficient compositions. Our calculated binding energy for the $(V_{La}^{\prime\prime\prime}V_{O}^{\bullet\bullet})$ pair cluster is found to be -1.02 eV per defect. This strong binding energy suggests that this could be a factor inhibiting the mobility of oxygen vacancies. As it has been proposed that the dominant compensation mechanism for A-site deficiency in lanthanum ferrites and cuprates is *via* the formation of oxygen vacancies,^{4,42,43} such a defect association would be expected to have a detrimental effect on the conductivity of these materials. However, it has been shown that La deficiency in the related LaMnO₃ system has no effect on oxygen diffusion compared to the cation stoichiometric compound.44 This was attributed to the fact that the formation of negatively charged La vacancies, $V_{\text{La}}^{\prime\prime\prime}\!$ is compensated by the oxidation of Mn³⁺ ions rather than the formation of oxygen vacancies, V₀^{••}. It has also been shown that A-site deficiency plays an important role in enhancing the performance of LSCF cathode materials;⁴³ therefore, the formation of holes may be the compensating mechanism for La-deficiency in LaFeO₃.

3.7. Cation Migration. The diffusion of cations is known to be slow compared to that of oxide ions. Cation diffusion may cause chemical creep, demixing, or decomposition and plays a key role in sintering, grain growth, and interactions at the electrode–electrolyte interface.^{45,46} The rate at which some of these processes occur is determined by the slowest moving species.⁴⁶ If the cations exhibit different diffusivities, kinetic demixing of cations⁴⁷ may contribute to the long-term degradation of oxide ion conductors in SOFCs. The energetics of cation migration were therefore investigated by atomic-scale simula-

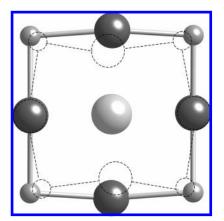


Figure 7. View down [010] showing a migrating La ion at the saddle point and the consequent local relaxation of the surrounding ions. The dashed line represents the migration aperture before relaxation.

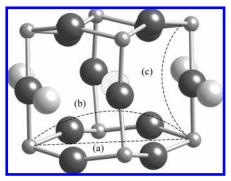


Figure 8. Possible pathways for Fe vacancy migration in $LaFeO_3$: (a) linear pathway along [100], (b) curved pathway along [100] with nearest La site vacant (shown as striped sphere) and (c) curved pathway between two Fe sites separated by an oxygen in the [010] direction with the same vacant La site. Small gray spheres represent Fe, large dark spheres O and large gray spheres La.

 TABLE 8: Calculated Activation Energies for Migration of

 La and Fe Ions in Orthorhombic LaFeO3

cation	migration pathway	migration energy/eV
La ³⁺	linear along [010]	4.00
La ³⁺	linear along [101]	4.21
Fe ³⁺	linear along [100] (a) ^{a}	13.18
Fe ³⁺	curved pathway with	6.16
Fe ³⁺	adjacent La vacancy (b) ^{<i>a</i>} curved pathway in [010] direction with adjacent La vacancy (c) ^{<i>a</i>}	3.25

^a See Figure 8

tions of vacancy migration between cation sites for both La^{3+} and Fe^{3+} ions.

Examination of the orthorhombic LaFeO₃ structure suggests that the most likely migration route for lanthanum diffusion is a linear pathway between La sites along either [010] or [101] passing through an aperture defined by four oxygen and four Fe ions as shown in Figure 7. As the radius of the La³⁺ ion is larger than the radius of this aperture, the surrounding lattice relaxes substantially in order to allow the migrating La³⁺ ion to pass through when it is at the saddle point. The degree of relaxation is shown in Figure 7 and the channel widens by 0.85 Å as the oxide ions move away from the migrating cation.

The calculated activation energies for La vacancy migration are listed in Table 8. As expected, the migration energy along [101] is greater as the bottleneck width is slightly smaller (3.32 Å versus 3.51 Å for [010]).

Simulation studies of cation migration in LaGaO₃⁴⁸ and LaMnO₃⁴⁹ have examined possible migration pathways for the B-site cation in cubic perovskite structures. These are a linear jump in the <110> direction or a more complex <100> jump along a curved pathway between B-cation sites along the <100>_{cubic} direction.

Three pathways were examined for migration of Fe³⁺ in orthorhombic LaFeO3. The results of these calculations are listed in Table 8 and the approximate migration pathways are shown in Figure 8. The first of these (a) was the linear jump between two Fe sites along [100] (the equivalent jump pathway to <110> in the cubic structure). A high migration energy of 13.18 eV was obtained; this is similar to that obtained for the B-site cation migration calculated for LaGaO₃ and LaMnO₃. The second pathway examined, (b), was also along the [100] direction, but mediated by the presence of a La vacancy on the nearest or next-nearest La site above the migration plane. The Fe ion moved in a curved pathway out of the (010) plane so that it was further from the surrounding oxide ions. Third, in (c), the migrating ion moved up and around the oxide ion located between two Fe sites adjacent along the [010] direction. This is similar to the calculated pathway described for Mn³⁺ migration in LaMnO₃.⁴⁹ As the migrating ion must pass between an oxide ion and a lanthanum ion at the saddlepoint, a La vacancy was created on the adjacent site. Our calculations find a relatively low energy of 3.25 eV for the third mechanism (c). De Souza and Maier48 also found that the migration energy for Ga^{3+} in LaGaO₃ dropped to 3.84 eV for this type of $V_{La}^{///}$ -mediated migration.

From recent studies of cation self-diffusion in close-tostoichiometric LaFeO₃, Smith and Norby⁵⁰ have suggested that the predominant diffusing species is Fe^{3+} with an activation energy of 3.3 eV, and that this represents the sum of the diffusion activation enthalpy and the formation enthalpy of the defect. Our results suggest that this observed activation energy may be purely a diffusion or migration enthalpy, although we recognize that further detailed experimental work on conductivity and computational studies using molecular dynamics (MD) are required. An MD study of doped LaGaO₃⁵¹ has suggested that cation diffusion is governed by diffusion via lattice vacancies in a mechanism similar to (b) and (c) above. It was suggested that the diffusion of cations is correlated to the formation and migration of a binary vacancy complex of two neighboring vacancies on the A and B sites of the perovskite lattice.

4. Conclusions

Atomistic simulation techniques have been used to probe the energetics of defects, dopants, nanoclustering and ion migration in the lanthanum ferrite LaFeO₃. The results have provided information at the atomic level which is relevant to the electrochemical behavior of LaFeO₃ and the doped system $La_{1-x}Sr_xFeO_{3-\delta}$ for potential SOFC applications. The main points are summarized as follows:

1. The calculated defect energies suggest that intrinsic disorder of the Frenkel or Schottky type is unlikely except at extremely high temperatures. The lowest energy redox process is oxidation of acceptor-doped LaFeO₃ with the formation of electronic holes. This result suggests p-type conduction in doped LaFeO₃ will occur at high oxygen partial pressures, as observed experimentally.

2. The binding energies for dopant-oxygen vacancy clusters indicate that Sr doping should enhance oxide-ion conductivity because of the low binding energy and the increase in vacancy concentration. However, as the Mg²⁺ substitutional has a strong tendency to "trap" the migrating oxygen vacancy, this would be detrimental to oxide-ion conductivity. Large complex clusters $(nMg'_{Fe} n/2V_o^{\bullet})$ with *n* up to 12 or 16 in 2D and 3D configurations, respectively, have been considered. These clusters may be important as precursors to possible short-range ordering or "nanodomain" formation at higher dopant concentrations, and warrants further structural study.

3. The pathway for oxide-ion migration is predicted to be a curved trajectory for O2–O2 or O2–O1 pathways. Inclusion of the binding energy term in the calculated energy for oxygen migration in Sr-doped LaFeO₃ results in calculated activation energies of between 0.70 and 0.84 eV. As expected, cation diffusion has high migration energies for both La³⁺ and Fe³⁺ vacancies. The lowest calculated energy (3.25 eV) is for Fe migration involving a La vacancy-mediated mechanism.

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