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Chapter 3

Selling information

Outline

- Problem and model assumptions
- Uninformed investment banks
- Informed investment banks
- Purchase of information
- Summary

Opportunity to sell information

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- We need $s < r$ to have information being offered, this means

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