



## Chapter 15.2

# Remuneration of traders

# Outline

- Problem and model assumptions
- Independent traders
- Fixed wages
- Performance wages
- Optimal trader remuneration
- Summary

## ■ Problem and model assumptions

### ■ Independent traders

### ■ Fixed wages

### ■ Performance wages

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# Traders as employees

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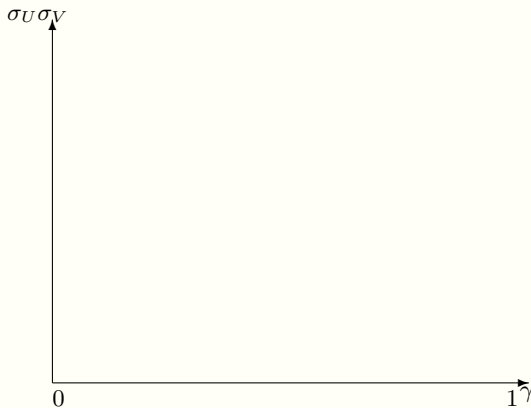
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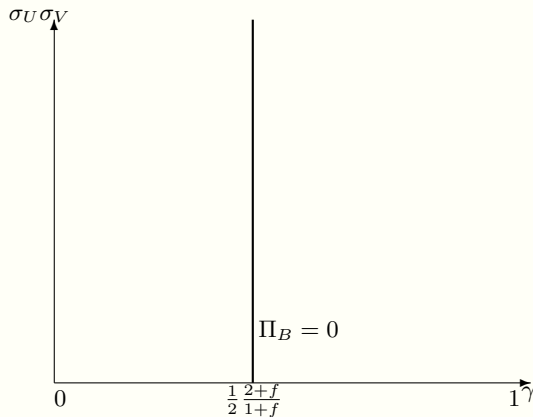
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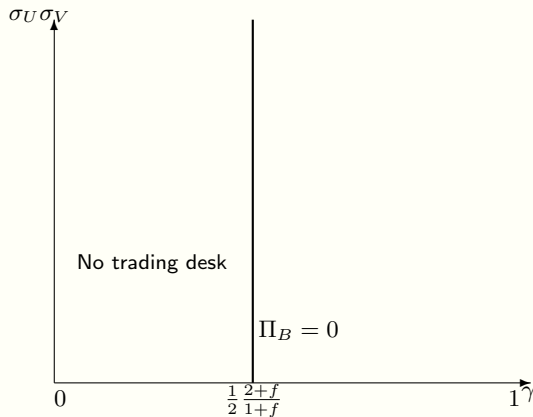
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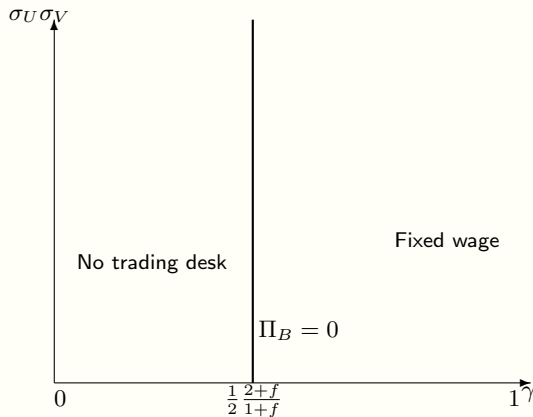
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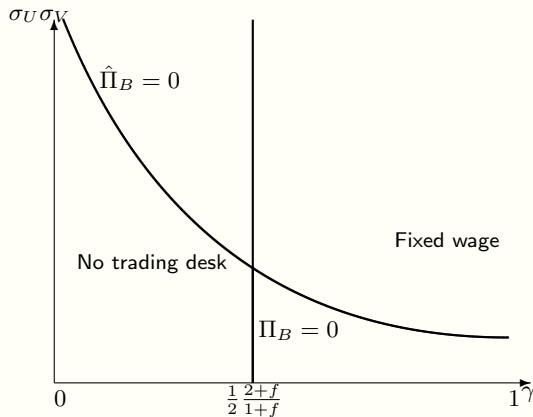


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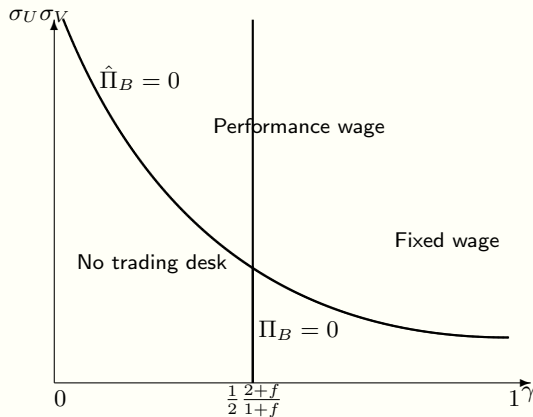




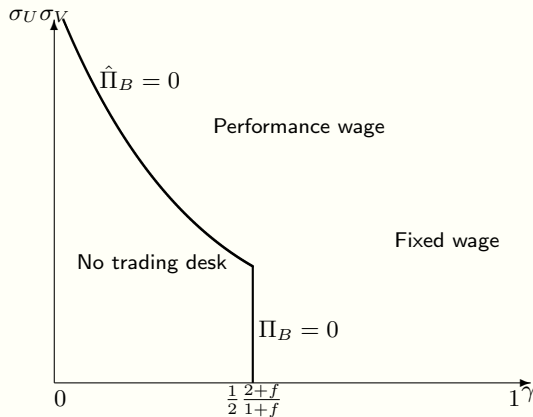
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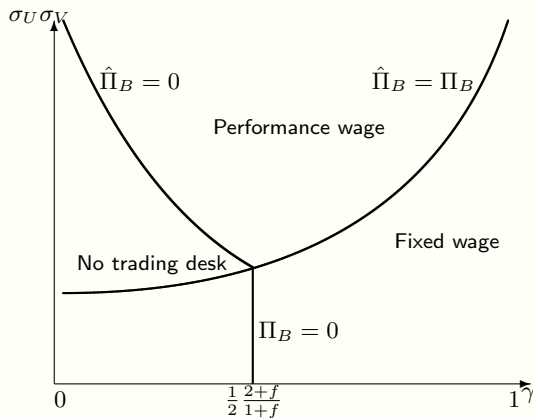
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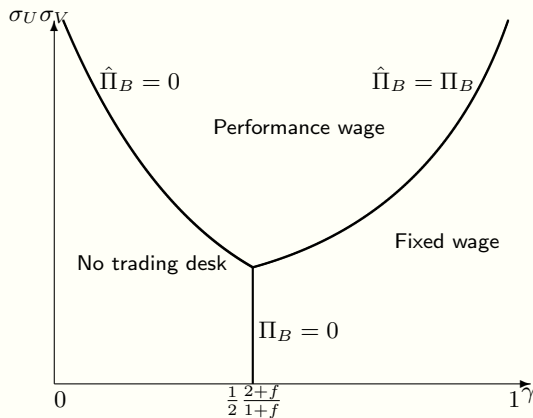
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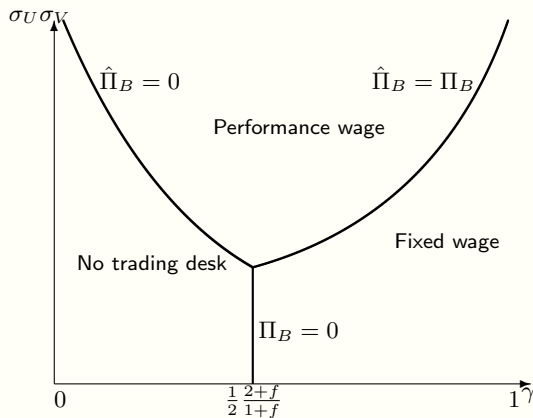
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■ Problem and model assumptions

■ Independent traders

■ Fixed wages

■ Performance wages

■ Optimal trader remuneration

■ Summary

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