Andreas Krause



Chapter 15.1 Investment in expertise

Problem and assumptions	Low price	High price	Optimal expertise	Summary
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Outline				

- Problem and model assumptions
 - Buyer setting low price
- Buyer setting high price
- Optimal expertise



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Outline

- For traders to generate profits, they rely on the access to information and their ability to interpret this information. This is referred to here as
 expertise.
- Expertise is obtained from knowledge of the trader about the asset they seek to purchase or sell, but also inferences about the behaviour of other traders. This knowledge will be based on experience, training, and depend on the information that can be accessed.
- Expertise will be costly to traders as they need to built up the knowledge through training and practice, but also will require access to databases and other information sources.
- We will here look into the optimal level of expertise of traders.

Outline

• We will first of all look at how expertise manifests itself in our model and then explore the behaviour of the buyers of securities, before combining their behaviour with that of sellers to determine the optimal level of expertise.



Problem and assumptions	Low price	High price	Optimal expertise	Summary
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Problem and model assumptions

Buyer setting low price

Buyer setting high price

Optimal expertise



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• We will now see how expertise by traders can be modelled.



Problem and assumptions	Low price	High price	Optimal expertise	Summary
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 \rightarrow The success in trading will depend on the level of expertise a trader has.

- Trading requires information and knowledge about the interpretation of this information; this is jointly referred to as 'expertise'. Such expertise would encompass the qualities of the asset traded, but also how other traders behave and the impact both factors have jointly on future prices.
- Trading is a zero sum game. A profit can be made by a trader if he buys an asset below its (future) value. As a trade involves a buyer and a seller, there must be another trader that sells the asset below its (future) value, making a loss. This loss is identical to the profits of the buyer, thus on aggregate there are no profits or losses from trading. The traders might not be aware of the losses they are making as the true (future) values are not known, so both traders might believe to make a profit, based on their expertise.
- A trader having better information is more likely to make a profit than a loss, hence traders will be competing to make profits of other traders by increasing their expertise. We will here look specifically at traders in investment banks, but this would in principle apply to any trader.
- $\rightarrow~$ We can now look at how we nodel expertise here.

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Trading expertise				

In order to make profits from trading, investment banks need to invest into the expertise of their traders

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Benefits of trading \Delta V can be positive if diversification and hedging are considered, in addition of trading profits

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Problem and model assumptions

Buyer setting low price

Buyer setting high price

Optimal expertise

Summary

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- We first consider the case where the buyer of the asset is only willing to pay a low price for the security.
- This low price might indicate that the buyer has received a signal indicating a low value, although the precision of this information will be low.



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- \rightarrow Regardless of the willingness of the buyer to purchase the asset, a trade is only completed if a seller agrees to it.
 - We now assume that a buyer is willing to pay what he beliefs to be the price if the low signal were received.
 - The buyer has no expertise and hence will not necessarily base this price on information; instead we assume that this decision is taken for arbitrary reasons.
- A seller will be willing to sell the asset at this price only if he has received the low signal. Having received a high signal would imply that the value of the asset is higher and he would not be willing to sell it below its value and incur a loss.
- The low signal is received if the true value is high, but they receive the wrong signal, or the true value is low and the signal received is correct.
- ightarrow We can now determine the profits of the buyer from this transaction.

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Assume a buyer *i* is only willing to pay $P^* = E[V|L]$

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 - We now assume that a buyer is willing to pay what he beliefs to be the price if the low signal were received.
 - The buyer has no expertise and hence will not necessarily base this price on information; instead we assume that this decision is taken for arbitrary reasons.
- A seller will be willing to sell the asset at this price only if he has received the low signal. Having received a high signal would imply that the value of the asset is higher and he would not be willing to sell it below its value and incur a loss.
- The low signal is received if the true value is high, but they receive the wrong signal, or the true value is low and the signal received is correct.
- ightarrow We can now determine the profits of the buyer from this transaction.



Problem and assumptions	Low price	High price	Optimal expertise	Summary
	○●○	000	0000	0000

Assume a buyer i is only willing to pay $P^* = E[V|L]$ and has no expertise itself

►

- \rightarrow Regardless of the willingness of the buyer to purchase the asset, a trade is only completed if a seller agrees to it.
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Problem and assumptions	Low price	High price	Optimal expertise	Summary
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Trades occurring				

- Assume a buyer i is only willing to pay $P^* = E[V|L]$ and has no expertise itself
- \blacktriangleright A transaction only occurs if the seller j obtains a low signal

►

- \rightarrow Regardless of the willingness of the buyer to purchase the asset, a trade is only completed if a seller agrees to it.
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Problem and assumptions	Low price	High price	Optimal expertise	Summary
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- Assume a buyer i is only willing to pay $P^* = E[V|L]$ and has no expertise itself
- \blacktriangleright A transaction only occurs if the seller j obtains a low signal
- ► This happens if the value is high, but the signal is wrong or the value low and the signal correct: $\pi (1 \rho_j) + (1 \pi) \rho_j$

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Problem and assumptions	Low price	High price	Optimal expertise	Summary
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- \rightarrow $\,$ We can now determine the profits of buyers willing to pay the low price.
 - When purchasing the security the buyer obtains the security with its value and the benefits of trading in general, such as diversification or hedging.
 - These benefits are reduced by the price at which the asset is purchased.
 - These profits are only realised if a trade occurs in the first place.
- Formula
 - The value of the security the buyer obtain must be the value given a low signal as assigned to it by the informed seller.
 - If the value would be higher, the seller would not be willing to trade. Thus acceptance of the trade by the seller reveals the value of the security.
- \rightarrow Of course, the value equals the price and these two terms will eliminate each other, leaving us only with the trading benefits.



Problem and assumptions	Low price ○○●	High price 000	Optimal expertise	Summary 0000
Buyer profits				

Trading profits are the value of the security and the trading benefits

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Problem and assumptions	Low price ○○●	High price 000	Optimal expertise	Summary 0000
Buyer profits				

Trading profits are the value of the security and the trading benefits, less the price paid

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Problem and assumptions	Low price	High price	Optimal expertise	Summary
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Buyer profits				

Trading profits are the value of the security and the trading benefits, less the price paid, if the trade happens

- $\rightarrow~$ We can now determine the profits of buyers willing to pay the low price.
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Problem and assumptions	Low price	High price	Optimal expertise	Summary
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- Trading profits are the value of the security and the trading benefits, less the price paid, if the trade happens
- $\Pi_B^i = (\pi (1 \rho_j) (1 \pi) \rho_j) (E[V|L] + \Delta V P^*)$

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Problem and assumptions	Low price	High price	Optimal expertise	Summary
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Problem and model assumptions

Buyer setting low price

Buyer setting high price

Optimal expertise



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Chapter 15.1: Investment in expertise Theoretical Foundations of Investment Banking • We can now explore the case where the buyer is willing to pay a high price for the asset.

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Problem and assumptions	Low price	High price	Optimal expertise	Summary
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- \rightarrow Having determined the profits of a buyer offering the low price, we will now look at a buyer offering a high price.
 - If the buyer offers to pay the high value, that is the value the informed seller assigns if he receives the high signal, a trade will always occur.
 - That is because the value the seller assigns to the asset is either below the price offered (low signal) or equal to it (high signal) and thus the seller will always want to sell the asset.
- The price offered can be rewritten as the high value, provided the high signal is correct, or the low value of the asset if the signal is incorrect. We can insert the signal precision as defined above and obtain the formula.
 - The fact that a trade occurs does not reveal any information on the value of the asset to the buyer. This is in contract to the case where the buyer offers a low price only; there the seller accepting the offer indicated that the value of the asset was low.
 - As the trade always occurs, regardless of the information the informed seller holds, it can reveal no information.
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- → We can now determine whether the buyer will offer a high or a low price.

Problem and assumptions	Low price	High price	Optimal expertise	Summary
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Buver profits				

▶ If the buyer is willing to pay $P^{**} = E[V|H]$, trade will always happen

- \rightarrow Having determined the profits of a buyer offering the low price, we will now look at a buyer offering a high price.
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Problem and assump		Low price 000	High price ○●○	Optimal expertise 0000	Summary 0000
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- ▶ If the buyer is willing to pay $P^{**} = E[V|H]$, trade will always happen as the value of the seller is never above this amount
- ► $P^{**} = Prob(V_H|H)V_H + (1 Prob(V_H|H))V_L = \rho_j V_H + (1 \rho_j)V_L$

- \rightarrow Having determined the profits of a buyer offering the low price, we will now look at a buyer offering a high price.
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Problem and assumptions	Low price	High price	Optimal expertise	Summary
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Buyer profits				

►
$$P^{**} = Prob(V_H|H)V_H + (1 - Prob(V_H|H))V_L = \rho_j V_H + (1 - \rho_j)V_L$$

Trade does not indicate the value of the security

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Trade does not indicate the value of the security as it happens regardless of the signal the seller obtains

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Problem and assumptions	Low price	High price	Optimal expertise	Summary
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Buyer profits				

►
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Problem and assumptions	Low price 000	High price ○●○	Optimal expertise	Summary 0000

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- ► Trader profits: $\hat{\Pi}_B^i = E[V] + \Delta V P^{**} = \Delta V (V_H V_L) e_j$

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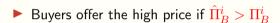
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Problem and assumptions	Low price	High price	Optimal expertise	Summary
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- \rightarrow We will now derive the condition under which the buyer is willing to offer a high price for the asset.
- The buyer will offer a high price if the profits of doing so are higher than offering the lower price. Offering the higher price brings certainty in obtaining the asset and the trading benefits, while offering a lower price may not result in a trade and the trading benefits do not materialise; this is traded off against the lower price the buyer pays.
- Inserting for all variables we obtain that the signal precision must not exceed a level as given in the formula.
- The seller is better informed and will only trade if it is profitable, implying that the buyer will make a loss. This loss is more likely the more precise the signal is as the seller will trade less and less on a wrong signal. Thus the trading losses of the buyer are increasing and need to be compensated for by the trading benefits (ΔV)
- ightarrow We can now use these results to determine the optimal level of expertise, and hence signal precision, for sellers.

Problem and assumptions	Low price	High price	Optimal expertise	Summary
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Maximum signal pr	ecision			



- ightarrow We will now derive the condition under which the buyer is willing to offer a high price for the asset.
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Problem and assumptions	Low price	High price	Optimal expertise	Summary
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▶ Buyers offer the high price if $\hat{\Pi}^i_B > \Pi^i_B$

Signal precision must not be too high: $\rho_j \leq \rho^* = \frac{\pi + (1-\pi) \frac{\Delta V}{V_H - V_L}}{1 + (1-2\pi) \frac{\Delta V}{V_H - V_L}}$

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Problem and assumptions	Low price	High price	Optimal expertise	Summary
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• Buyers offer the high price if $\hat{\Pi}_B^i > \Pi_B^i$

- Signal precision must not be too high: $\rho_j \leq \rho^* = \frac{\pi + (1-\pi) \frac{\Delta V}{V_H V_L}}{1 + (1-2\pi) \frac{\Delta V}{V_H V_L}}$
- Low signal precision is required as else adverse selection costs are too high for the buyer to offer the high price

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Problem and assumptions	Low price 000	High price	Optimal expertise ●000	Summary 0000

Problem and model assumptions

Buyer setting low price

Buyer setting high price

Optimal expertise

Summary

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• We now derive the optimal level of expertise by traders.

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Problem and assumptions	Low price	High price	Optimal expertise	Summary
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Chapter 15.1: Investment in expertise Theoretical Foundations of Investment Banking Slide 13 of 18

- \rightarrow First we determine the profits sellers make from trading.
- Trading in itself is a zero-sum game as argued above, hence the trading profits of sellers will be equal to the trading looses of buyers. As buyers here are assumed to have additional trading benefits ΔV, the net benefits of both traders combined will be those additional benefits.
- Inserting from the profits of buyers above, we get that the seller has trading profits as indicated in the formula.
- Let us now assume that over time buying and selling is balanced, thus half the time a trader is a seller and the other half a buyer.
- The profits of traders will then consist of the profits from buying and selling.
- We need to take into account the costs of gaining the expertise in the first place.
- \rightarrow These trader profits can now be maximized.

Problem and assumptions	Low price 000	High price	Optimal expertise ○●○○	Summary 0000
Seller profits				

• Total trading benefits of buyers and sellers are $\hat{\Pi}_{S}^{j} + \Pi_{B}^{i} = \Delta V$

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- Total trading benefits of buyers and sellers are $\hat{\Pi}_{S}^{j} + \Pi_{B}^{i} = \Delta V$
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Problem and assumptions	Low price	High price 000	Optimal expertise 0●00	Summary 0000

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Problem and assumptions	Low price	High price	Optimal expertise	Summary
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- \rightarrow We will now explore the optimal level of expertise that traders obtain to maximize their profits.
- The first order condition for the profit maximum of a trader is that the first derivative of their profits with respect to the level of expertise is zero.
- This condition solves for the formula.
- We assume that this result will allow buyers to offer high prices, thus $\rho_i < \rho^*$.
 - If the costs of all traders, buyers and sellers, are identical, then the optimal expertise will be identical as the solution to the first order condition
 is identical across traders.
 - Formula
- Inserting this result, we obtain the total profits as in the formula.
- ightarrow We can now compare this optimal result with the Pareto optimum for traders.

Problem and assumptions	Low price	High price	Optimal expertise	Summary
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- First order condition for optima expertise is $\frac{\partial \hat{\Pi}^i}{\partial e_i} = 0$
- This gives $\frac{\partial C_i}{\partial e_i} = \frac{1}{2} \left(V_H V_L \right) > 0$

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Problem and assumptions	Low price	High price	Optimal expertise	Summary
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- \rightarrow We see that the profits of traders are higher, the lower the costs of investing into expertise are. We will explore the implications of this observation further.
- Let us assume that traders have no expertise at all, which implies that they have no costs of acquiring such expertise.
- Having no costs will increase the profits of traders.
- Thus, not investing into expertise increases profits, but we maximized profits and had positive marginal costs, implying that traders acquire expertise at costs.
- The reason for this result is that if the other traders do not invest into expertise, then as a buyer the trader would make less losses (there is less adverse selection) and as a seller would make high profits as he is informed. This gives an incentive to invest into expertise. The result is that all traders invest into expertise.
- While having no expertise would give higher profits for all traders, they engage in an arms race by acquiring expertise and obtain the ability to generate trading profits at the expense of other traders.
- \rightarrow We thus see that, compared to the social optimum, traders over0invest into their expertise.

Problem and assumptions	Low price	High price	Optimal expertise	Summary
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• If traders have no expertise, $e_i = e_j = 0$ and $C_i = 0$

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- Not investing into expertise is more profitable
- If a trader does not invest into expertise, it is profitable for the other trader to do so
- This leads to an arms race in the level of expertise

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- Not investing into expertise is more profitable
- If a trader does not invest into expertise, it is profitable for the other trader to do so
- This leads to an arms race in the level of expertise

- \rightarrow We see that the profits of traders are higher, the lower the costs of investing into expertise are. We will explore the implications of this observation further.
- Let us assume that traders have no expertise at all, which implies that they have no costs of acquiring such expertise.
- Having no costs will increase the profits of traders.
- Thus, not investing into expertise increases profits, but we maximized profits and had positive marginal costs, implying that traders acquire expertise at costs.
- The reason for this result is that if the other traders do not invest into expertise, then as a buyer the trader would make less losses (there is less adverse selection) and as a seller would make high profits as he is informed. This gives an incentive to invest into expertise. The result is that all traders invest into expertise.
- While having no expertise would give higher profits for all traders, they engage in an arms race by acquiring expertise and obtain the ability to generate trading profits at the expense of other traders.
- \rightarrow We thus see that, compared to the social optimum, traders over0invest into their expertise.

Problem and assumptions	Low price	High price	Optimal expertise	Summary
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Problem and model assumptions

Buyer setting low price

Buyer setting high price

Optimal expertise



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• We can now summarize the key findings of this model.

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Problem and assumptions Low price High price Optimal expertise	Summary 0●00
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- \rightarrow We have seen that traders invest too much into their expertise, exceeding the Pareto optimal level of expertise.
- The reason for investors to over-invest into their expertise is that they seek to extract profits from other traders, who attempt the same, leading to an arms race.
 - In order to extract more profits from other traders, they invest into their expertise.
 - However, every trader does the same, leading to a situation where the trading profits remain the same, regardless of the level of expertise. Thus
 there are no benefits from investing into expertise, the costs even reduce the profits for each trader. However, no trader can afford to invest less
 into expertise as they would make a loss due to other traders having a higher level of expertise.
- ▶ All traders would prefer to invest less into their expertise and reduce costs, but this is not an equilibrium.
- \rightarrow We can now look briefly at some implications of this key result.

Problem and assumptions	Low price	High price	Optimal expertise	Summary
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With trading a (mostly) zero sum game, traders seek to extract profits from other traders

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Problem and assumptions	Low price	High price	Optimal expertise	Summary
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- To extract more profits, they invest into expertise, but as everyone does, no benefits are gained

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Problem and assumptions	Low price	High price	Optimal expertise	Summary
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- \rightarrow We have a disconnect between the rational decisions of individual traders and the social optimum.
- Traders invest too much into their expertise and are thus over-qualified, compared to the social optimum.
- A consequence is also that the investment bank, which bears the cost of acquiring this expertise, invests too much resources into proprietary trading and
 - The decision to invest into expertise is rational for each individual trader and it maximizes their profits, given the behaviour of all other traders.
 - The outcome is, however, socially suboptimal and could be improved by investing less into their expertise.
- → We have thus seen that investment banks invests too much resources into proprietary trading, but this is driven by the competition between investment banks to extract profits from other investment banks' trading desks.

Problem and assumptions	Low price 000	High price 000	Optimal expertise	Summary 0000

Traders are over-qualified

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