



## Chapter 12

# Asset management

# Outline

- Problem and model assumptions
- Clients investing directly
- Delegated investment
- Clients with equal information
- Summary

## ■ Problem and model assumptions

■ Clients investing directly

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■ Summary

# Delegated portfolio management

- ▶ Investment banks also manage funds on behalf of clients
- ▶ They do not only give advice on investments, but instead make investment decisions themselves
- ▶ Clients delegate the decision-making to the investment bank
- ▶ The reason for delegation is the superior information and skills investment banks have

# Value of asset management

- ▶ Asset management provides a stable source of income to investment banks
- ▶ Can be used to maintain personal contacts to key decision-makers in companies
- ▶ The market is fiercely competitive with private banks and investment consultancies seeking access to the same investors

# Investment banking fees

- ▶ Investment banks are rewarded by a management fee  $f_0$  on the wealth invested
- ▶ They also charge a performance fee  $f_1$  on the profits above a benchmark return  $r$
- ▶ They invest a fraction  $\omega$  in a risky asset and the remainder in an asset yielding the benchmark return
- ▶ Fee income:  $F = f_0 W_0 + f_1 \omega (R - r) W_0$

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# Investment returns and risks

- ▶ The information clients have, suggests the expected return of the risky asset is  $\mu_C$  and its variance  $\sigma_C^2$
- ▶ After investing, the wealth will be the return on the amount invested in the benchmark asset and the return on the risky asset
- ▶  $W_1 = (1 - \omega) (1 + r) W_0 + \omega (1 + R) W_0$
- ▶ Expected value:  $E[W_1] = (1 + r) W_0 + \omega (\mu_C - r) W_0$
- ▶ Variance:  $Var[W_1] = \omega^2 \sigma_C^2 W_0^2$



# Optimal portfolio

- ▶ Clients maximize expected utility  $U_C = E[W_1] - \frac{1}{2}zVar[W_1]$  and the first order condition  $\frac{\partial U_C}{\partial \omega} = 0$  gives
- ▶  $\omega^* = \frac{\mu_C - r}{z\sigma_C^2} W_0$
- ▶ Utility is then  $U_C = (1 + r)W_0 + \frac{(\mu_C - r)^2}{2z\sigma_C^2}$

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# Maximizing fee income

- ▶ Investment banks have different information and assess the asset as having expected return  $\mu_B$  and variance  $\sigma_B < \sigma_C$
- ▶ Investment banks maximize fee income
- ▶ Expected fees:  $E[F] = f_0 W_0 + f_1 \omega (\mu_B - r) W_0$
- ▶ Variance:  $Var[F] = f_1^2 \omega^2 \sigma_B^2 W_0^2$

# Optimal delegated portfolio

- ▶ Investment banks maximize expected utility  $U_B = E[F] - \frac{1}{2}zVar[F]$  and the first order condition  $\frac{\partial U_B}{\partial \omega} = 0$  gives
- ▶  $\omega^{**} = \frac{\mu_B - r}{zf_1\sigma_B^2 W_0}$
- ▶ Investment bank utility:  $U_B = f_0 W_0 + \frac{(\mu_B - r)^2}{2z\sigma_B^2}$
- ▶ Perfect competition sets management fee such that  $U_B = 0$ , hence  $f_0 = -\frac{(\mu_B - r)^2}{2z\sigma_B^2 W_0} < 0$
- ▶ Investment banks charge a negative management fee

# Optimal performance fee

- ▶ Client wealth:  $W_1 = (1 + r) W_0 + \omega^{**} (R - r) W_0 - F$
- ▶ Client utility:  $\hat{U}_C = (1 + r) W_0 + 2 \frac{(\mu_B - r)^2}{2z\sigma_B^2} - \frac{(\mu_B - r)^2}{2z\sigma_B^2} \left( \frac{1 - 2f_1}{f_1} \right)^2$
- ▶ Investment banks extract all surplus from clients and set the performance fee such that  $\hat{U}_C = U_C$
- ▶  $f_1 = \frac{1}{2 + \sqrt{2 - \frac{\sigma_B^2}{\sigma_C^2} \left( \frac{\mu_C - r}{\mu_B - r} \right)^2}} < \frac{1}{2}$

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# Optimal portfolio

- ▶ To compare the optimal portfolios, assume that  $\mu_B = \mu_C$  and  $\sigma_B^2 = \sigma_C^2$ , clients and investment banks have the same information

- ▶ Client utility:

$$\hat{U}_C = (1 + r - f_0) W_0 + (1 - f_1) \omega (\mu_B - r) W_0 - \frac{1}{2} (1 - f_1)^2 \omega^2 \sigma_B^2 W_0^2$$

- ▶ First order condition for the optimal portfolio is then  $\frac{\partial \hat{U}_C}{\partial \omega} = 0$

- ▶  $\omega^{***} = \frac{\mu_B - r}{z(1 - f_1)\sigma_B^2 W_0}$

# Excess risks taken

- ▶ As  $f_1 = \frac{1}{3}$ , we have  $\omega^{**} = 2\omega^{***}$
- ▶ Investment banks invest a too high fraction into the risky asset
- ▶ The reliance on the performance fee drives this result
- ▶ As only the fee is exposed to risk, not their investment, investment banks seek higher risks



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# Distorted asset allocation

- ▶ Investment decisions being delegated to investment banks lead to more risky portfolios than is optimal
- ▶ This may seem even more risky to clients if they assess the risk based on their own information
- ▶ The informational advantage of investment banks may, however, increase the utility of clients, despite the distorted allocation into risky assets

# Consequences of biased asset allocation

- ▶ Larger exposure of clients to more risky assets makes the portfolio performance more sensitive to the assessment of the investment bank
- ▶ This makes the skills of the investment bank more apparent
- ▶ Investment banks have to invest more into these skills to remain competitive



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