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Chapter 12 Asset management

Problem and assumptions	Direct investment	Delegated investment 0000	Clients with equal information	Summary 0000
Outline				

- Problem and model assumptions
 - Clients investing directly
 - Delegated investment
- Clients with equal information



Problem and assumptions	Direct investment	Delegated investment	Clients with equal information	Summary
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Clients investing directly

Delegated investment

Clients with equal information



Delegated portfolio management

- Investment banks also manage funds on behalf of clients
- They do not only give advice on investments, but instead make investment decisions themselves
- Clients delegate the decision-making to the investment bank
- The reason for delegation is the superior information and skills investment banks have

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Value of asset management

- Asset management provides a stable source of income to investment banks
- > Can be used to maintain personal contacts to key decision-makers in companies
- The market is fiercely competitive with private banks and investment consultancies seeking access to the same investors

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Investment banking fees

- \blacktriangleright Investment banks are rewarded by a management fee f_0 on the wealth invested
- \blacktriangleright They also charge a performance fee f_1 on the profits above a benchmark return r
- \blacktriangleright They invest a fraction ω in a risky asset and the remainder in an asset yielding the benchmark return

Fee income:
$$F = f_0 W_0 + f_1 \omega (R - r) W_0$$

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- ► The information clients have, suggests the expected return of the risky asset is μ_C and its variance σ_C^2
- After investing, the wealth will be the return on the amount invested in the benchmark asset and the return on the risky asset

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$$W_1 = (1 - \omega) (1 + r) W_0 + \omega (1 + R) W_0$$

- Expected value: $E[W_1] = (1+r) W_0 + \omega (\mu_C r) W_0$
- Variance: $Var[W_1] = \omega^2 \sigma_C^2 W_0^2$

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Optimal portfolio

► Clients maximize expected utility U_C = E [W₁] - ¹/₂zVar [W₁] and the first order condition ^{∂U_C}/_{∂ω} = 0 gives

$$\blacktriangleright \ \omega^* = \frac{\mu_C - r}{z \sigma_C^2 W_0}$$

• Utility is then
$$U_C = (1+r) W_0 + \frac{(\mu_C - r)^2}{2z\sigma_C^2}$$

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Problem and assumptions	Direct investment 000	Delegated investment ○●○○	Clients with equal information	Summary 0000
Maximizing fee	income			

- Investment banks have different information and assess the asset as having expected return μ_B and variance σ_B < σ_C
- Investment banks maximize fee income
- Expected fees: $E[F] = f_0 W_0 + f_1 \omega (\mu_B r) W_0$

► Variance:
$$Var[F] = f_1^2 \omega^2 \sigma_B^2 W_0^2$$

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Optimal delegated portfolio

▶ Investment banks maximize expected utility $U_B = E[F] - \frac{1}{2}zVar[F]$ and the first order condition $\frac{\partial U_B}{\partial \omega} = 0$ gives

$$\blacktriangleright \ \omega^{**} = \frac{\mu_B - r}{z f_1 \sigma_B^2 W_0}$$

- Investment bank utility: $U_B = f_0 W_0 + \frac{(\mu_B r)^2}{2z\sigma_B^2}$
- ▶ Perfect competition sets management fee such that $U_B = 0$, hence $f_0 = -\frac{(\mu_B r)^2}{2z\sigma_B^2 W_0} < 0$
- Investment banks charge a negative management fee

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Optimal performance fee

- ► Client wealth: $W_1 = (1+r) W_0 + \omega^{**} (R-r) W_0 F$
- Client utility: $\hat{U}_C = (1+r) W_0 + 2 \frac{(\mu_B r)^2}{2z\sigma_B^2} \frac{(\mu_B r)^2}{2z\sigma_B^2} \left(\frac{1-2f_1}{f_1}\right)^2$
- ▶ Investment banks extract all surplus from clients and set the performance fee such that $\hat{U}_C = U_C$

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$$f_1 = \frac{1}{2 + \sqrt{2 - \frac{\sigma_B^2}{\sigma_C^2} \left(\frac{\mu_C - r}{\mu_B - r}\right)^2}} < \frac{1}{2}$$

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- To compare the optimal portfolios, assume that $\mu_B = \mu_C$ and $\sigma_B^2 = \sigma_C^2$, clients and investment banks have the same information
- Client utility: $\hat{U}_C = (1 + r - f_0) W_0 + (1 - f_1) \omega (\mu_B - r) W_0 - \frac{1}{2} (1 - f_1)^2 \omega^2 \sigma_B^2 W_0^2$
- First order condition for the optimal portfolio is then $\frac{\partial \hat{U}_C}{\partial \omega} = 0$

•
$$\omega^{***} = \frac{\mu_B - r}{z(1 - f_1)\sigma_B^2 W_0}$$

Optimal portfolio

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Excess risks taken

- As $f_1 = \frac{1}{3}$, we have $\omega^{**} = 2\omega^{***}$
- Investment banks invest a too high fraction into the risky asset
- ▶ The reliance on the performance fee drives this result
- As only the fee is exposed to risk, not their investment, investment banks seek higher risks

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Distorted asset allocation

- Investment decisions being delegated to investment banks lead to more risky portfolios than is optimal
- This may seem even more risky to clients if they assess the risk based on their own information
- The informational advantage of investment banks may, however, increase the utility of clients, despite the distorted allocation into risky assets

Consequences of biased asset allocation

- Larger exposure of clients to more risky assets makes the portfolio performance more sensitive to the assessment of the investment bank
- This makes the skills of the investment bank more apparent
- Investment banks have to invest more into these skills to remain competitive



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