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Chapter 12

Asset management

Outline

- **Problem and model assumptions**
- Clients investing directly
- Delegated investment
- Clients with equal information
- Summary

Delegated portfolio management

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