



Parities

Outline

- Arbitrage with goods and investment
- Purchasing power parity
- Interest rate parity
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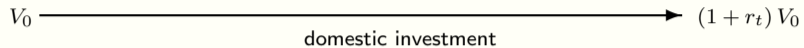
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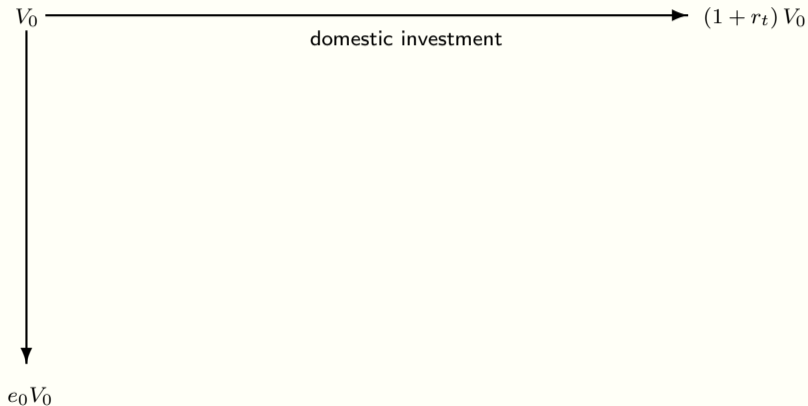
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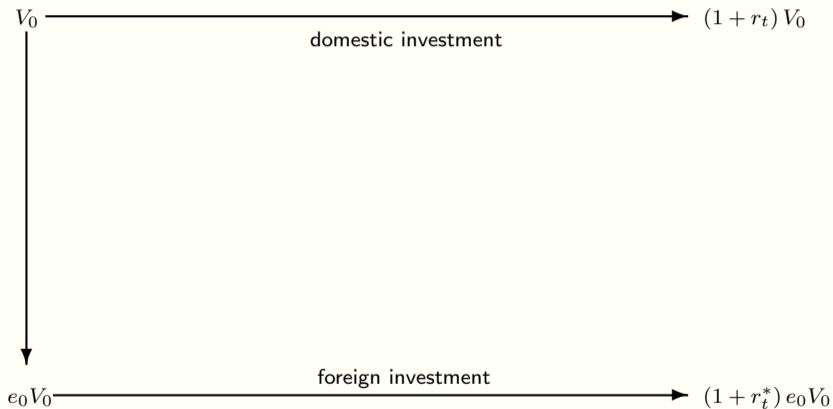
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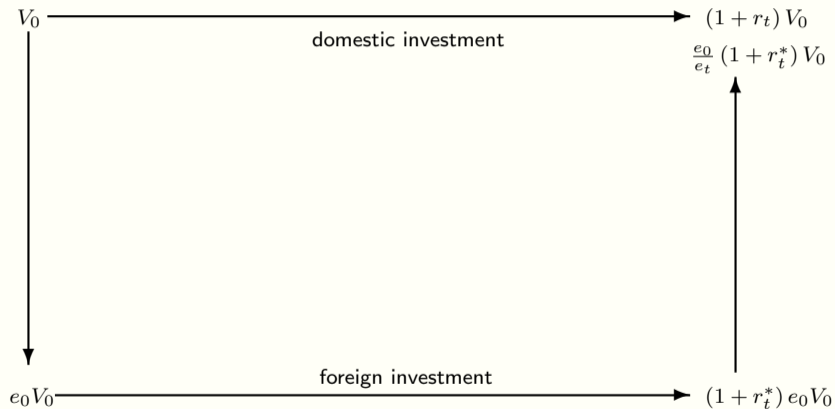
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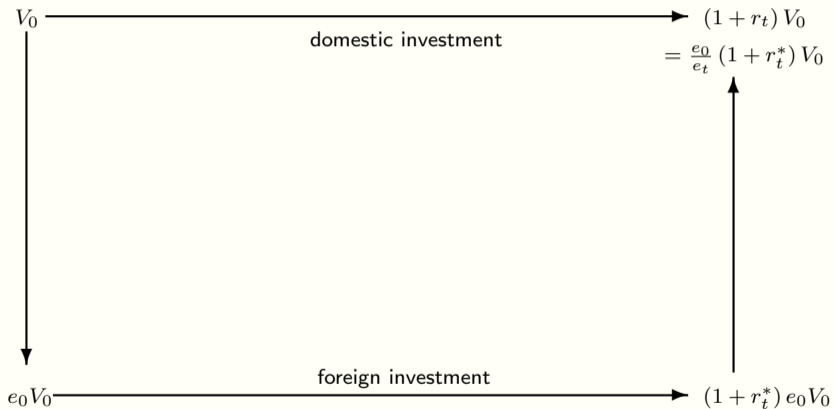
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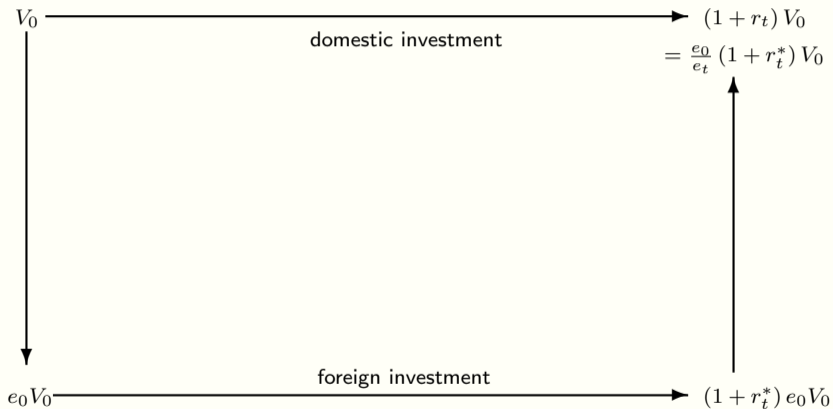
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