



Collateralised debt obligations

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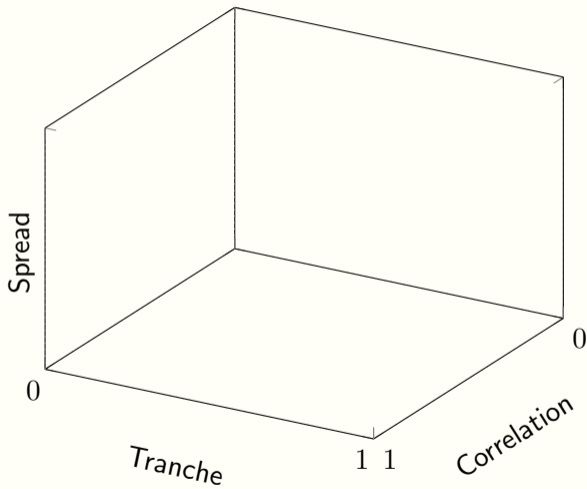
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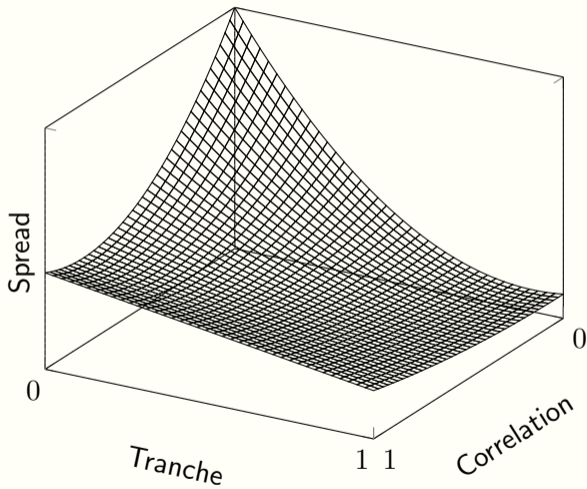
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# Spread of collateralised debt obligations

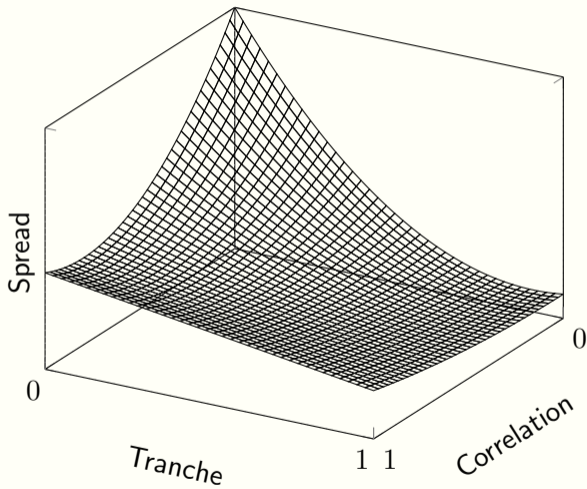
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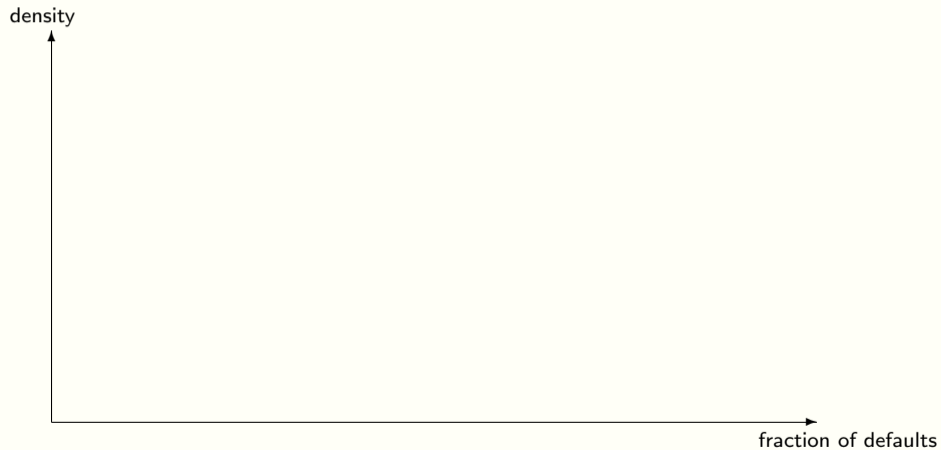
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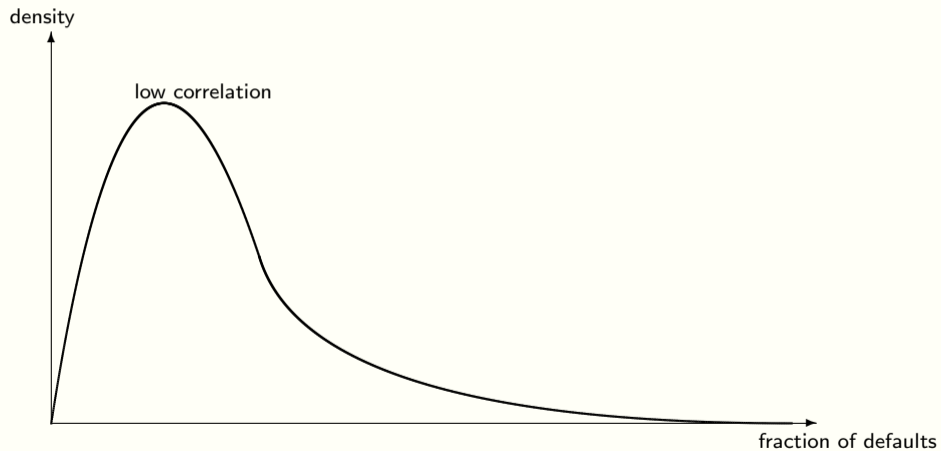


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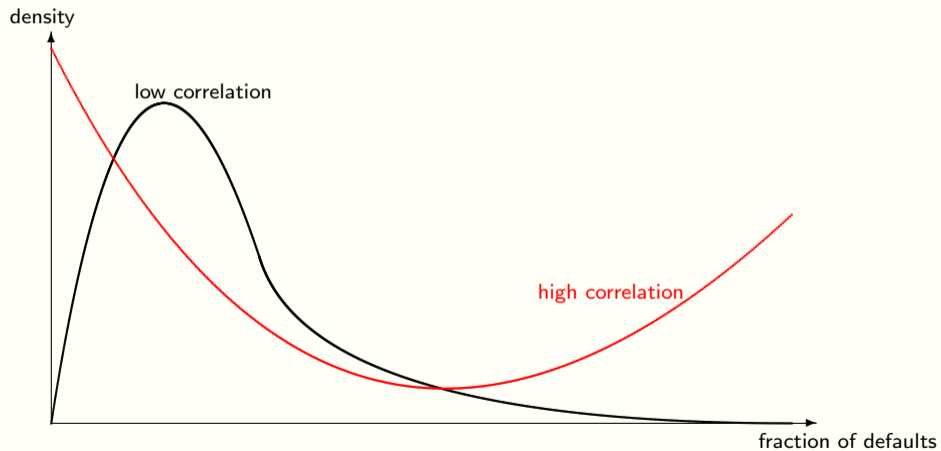
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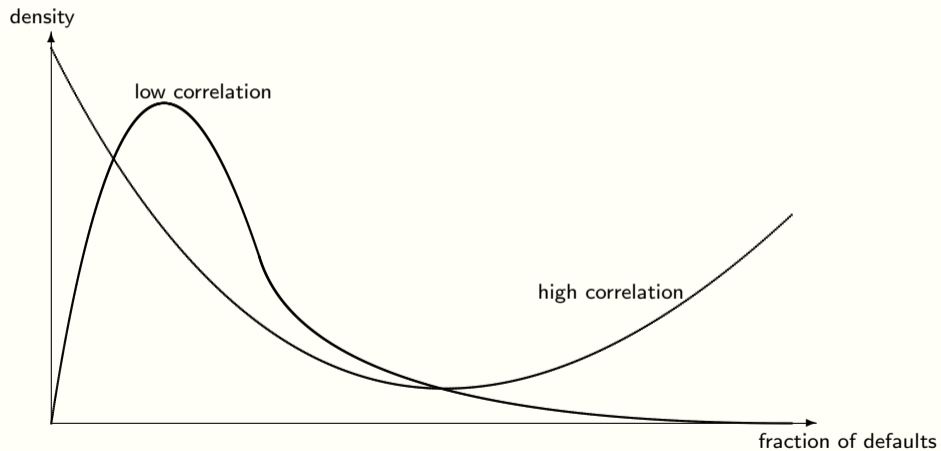
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Andreas Krause  
Department of Economics  
University of Bath  
Claverton Down  
Bath BA2 7AY  
United Kingdom

E-mail: [mnsak@bath.ac.uk](mailto:mnsak@bath.ac.uk)