

#### Existence of bubbles

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# Rationality of bubbles

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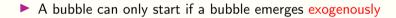
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# Starting of a bubble

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