

Performance evaluation



Outline

- Exploiting market inefficiencies
- Sharpe ratio
- Jensen's α
- Portfolio return decomposition
- Summary

■ Exploiting market inefficiencies

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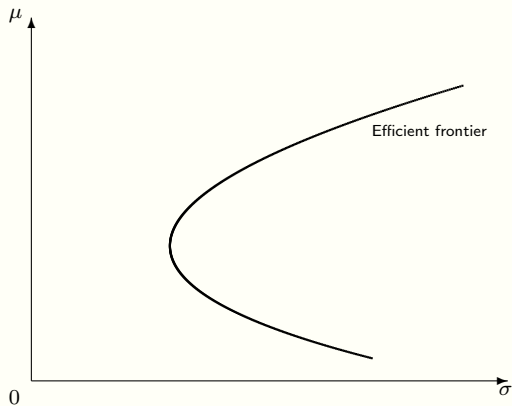
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Portfolio selection

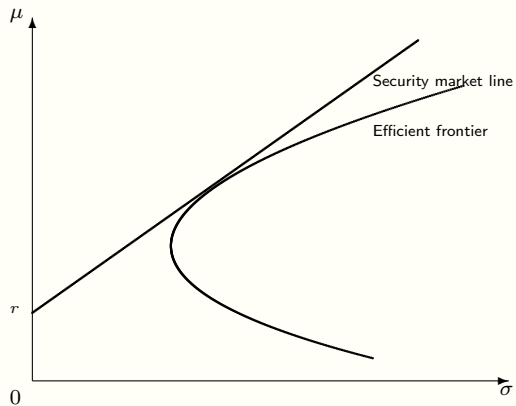
Portfolio selection



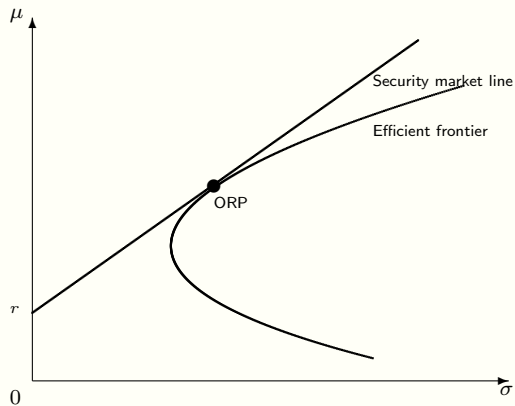
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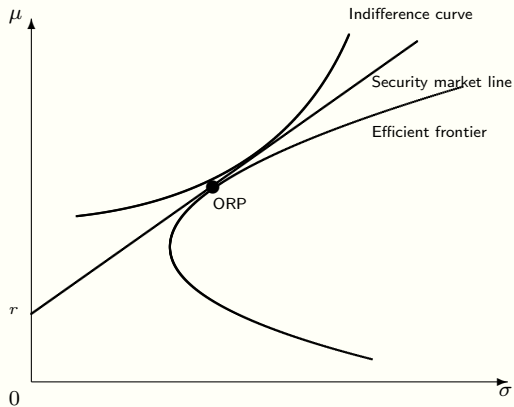
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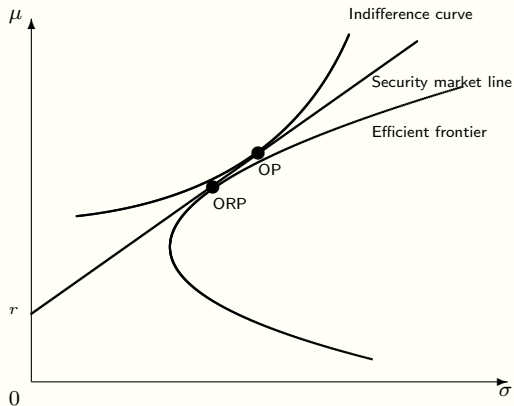
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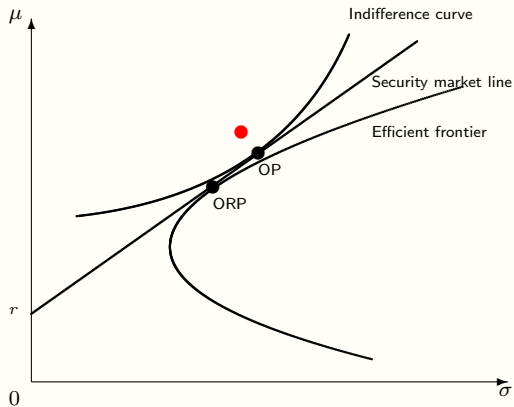
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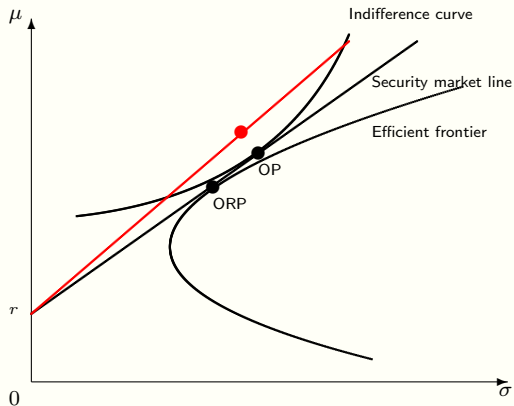
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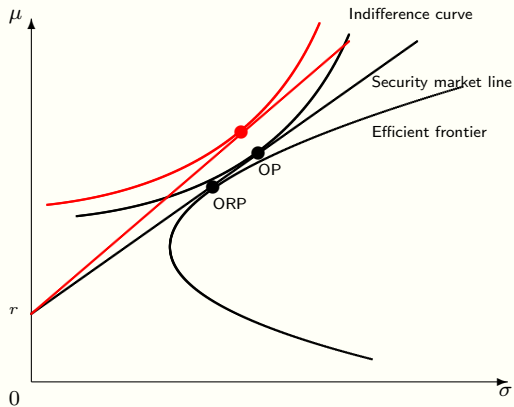
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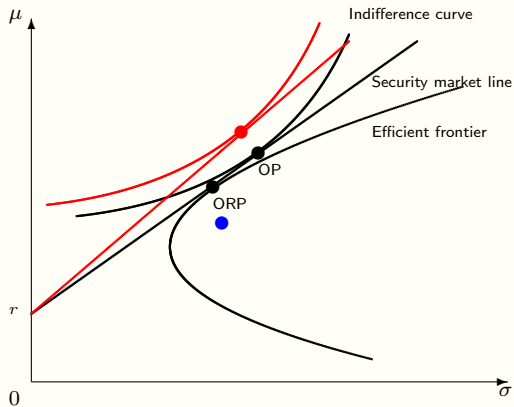
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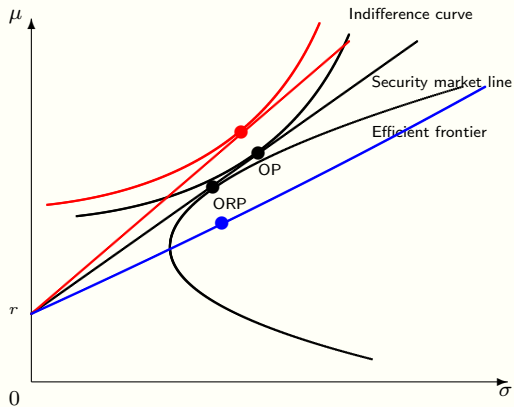
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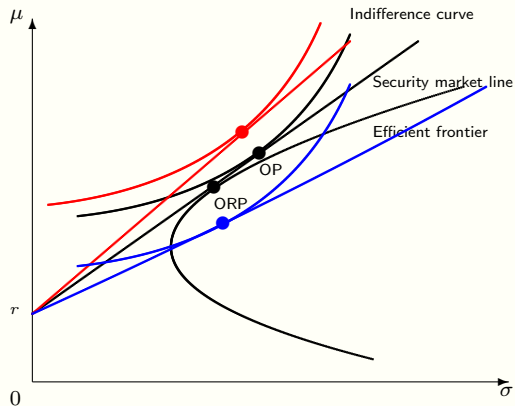
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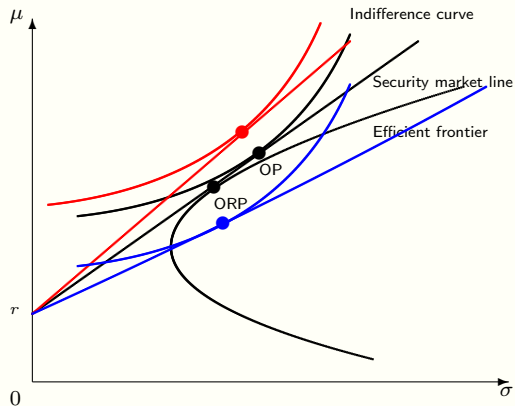
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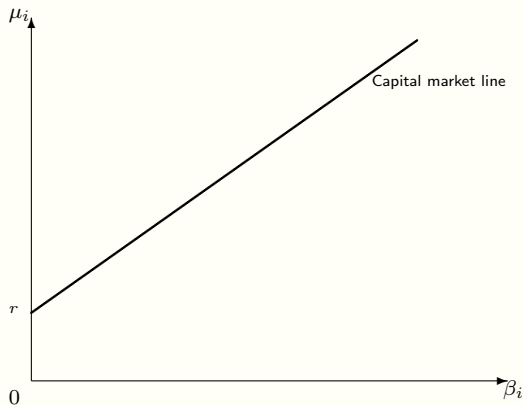
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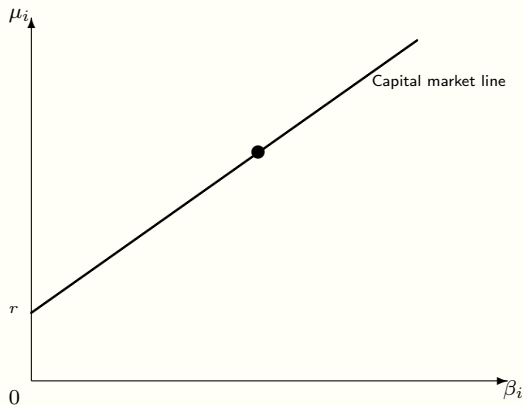
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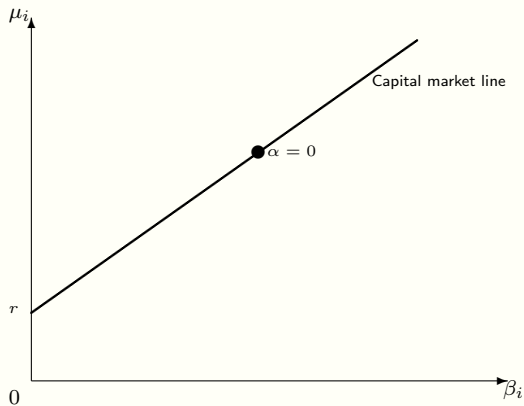
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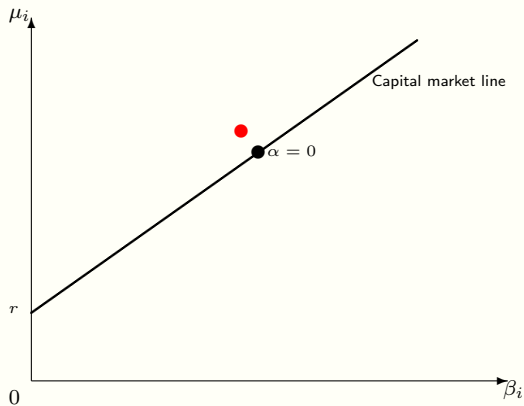
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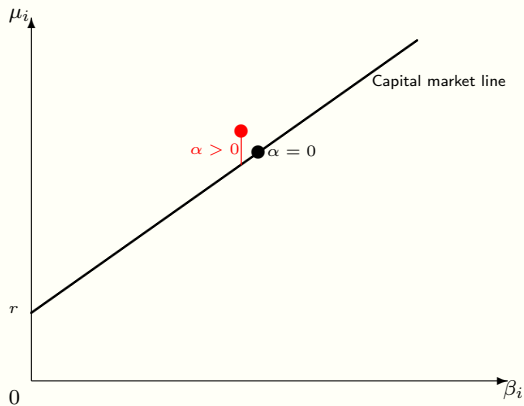
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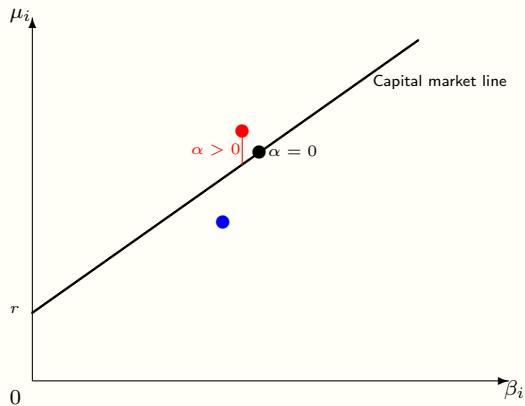
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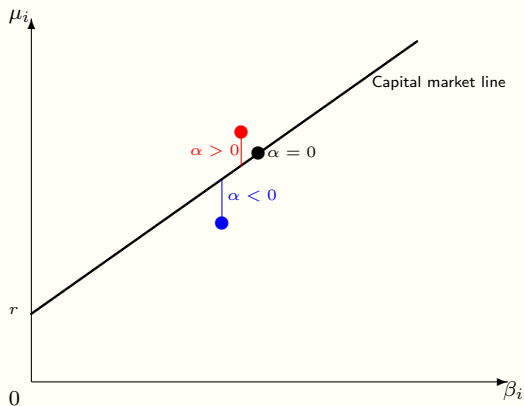
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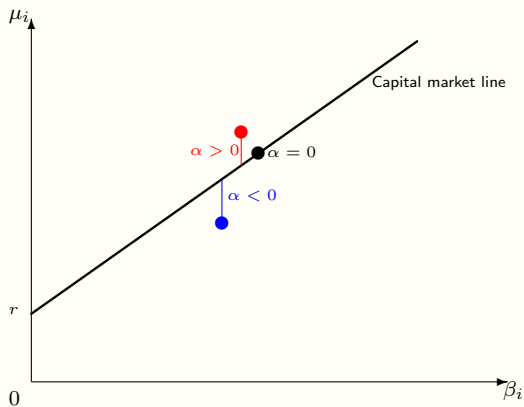
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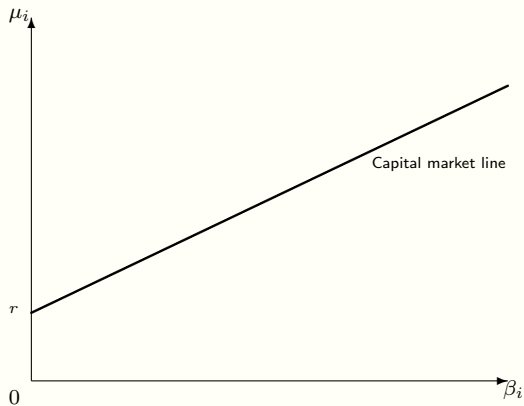
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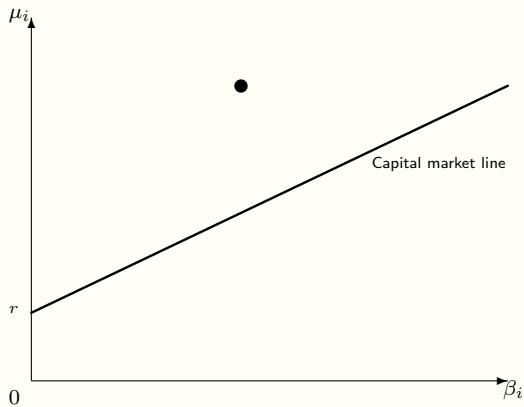
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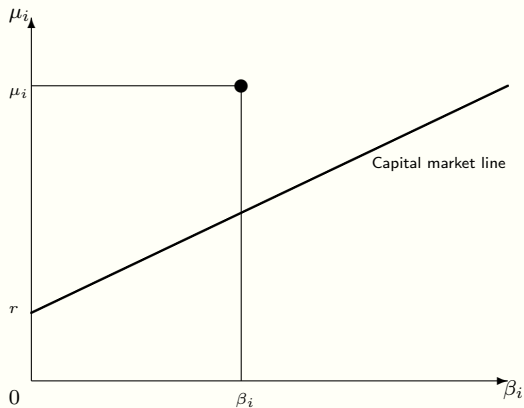
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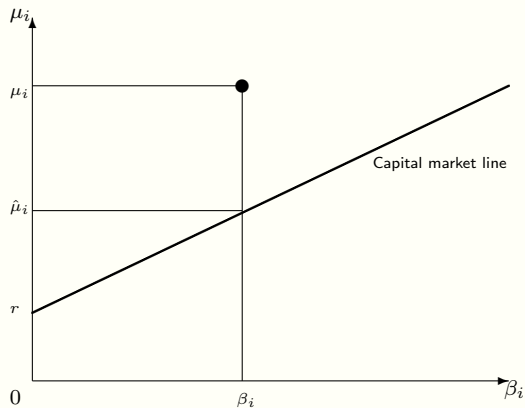
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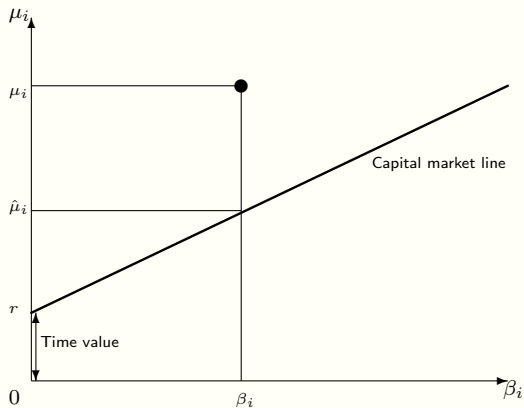
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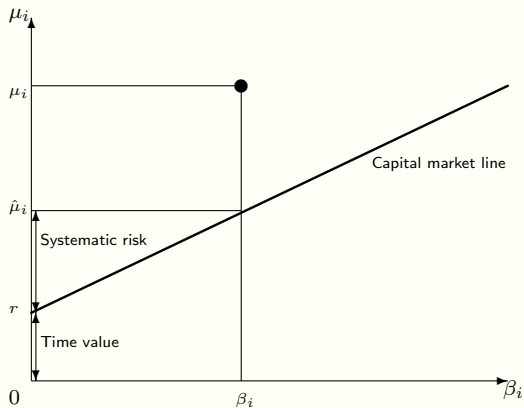
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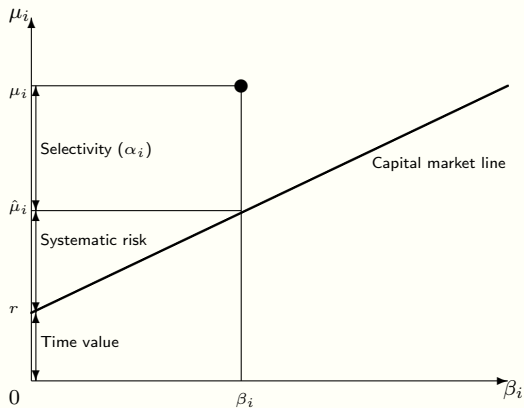
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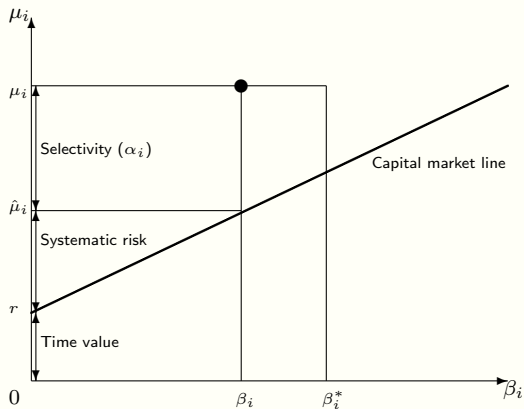
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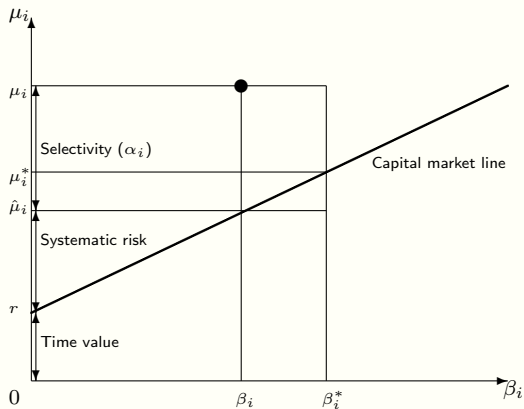
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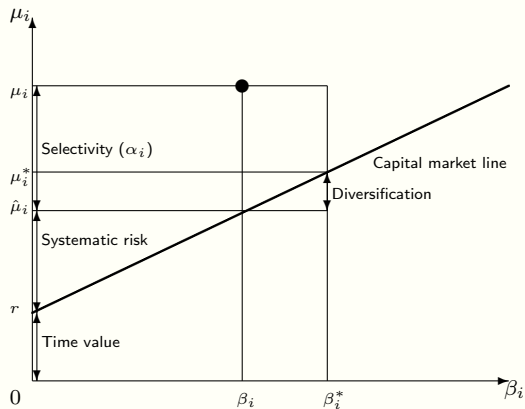
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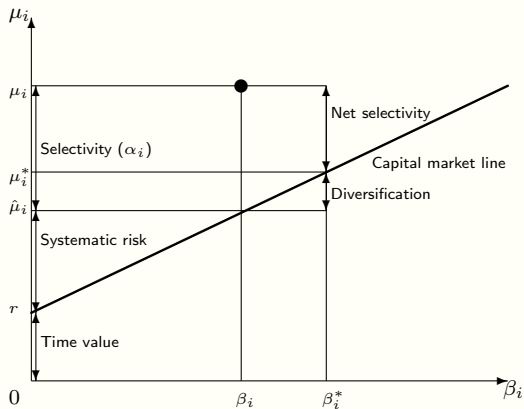
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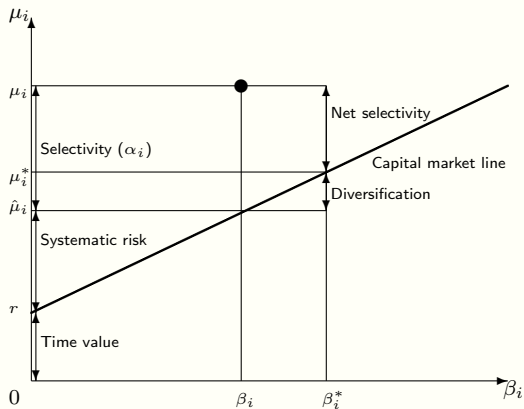
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