

Andreas Krause

Properties of option prices

Influences on option values

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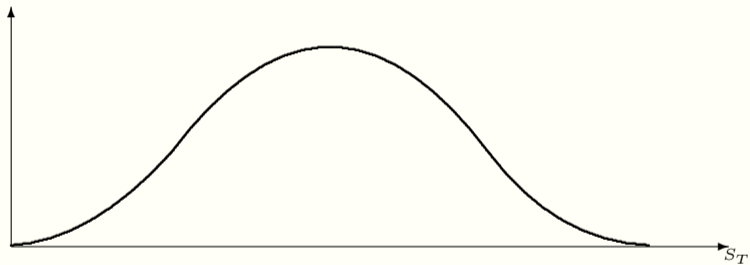
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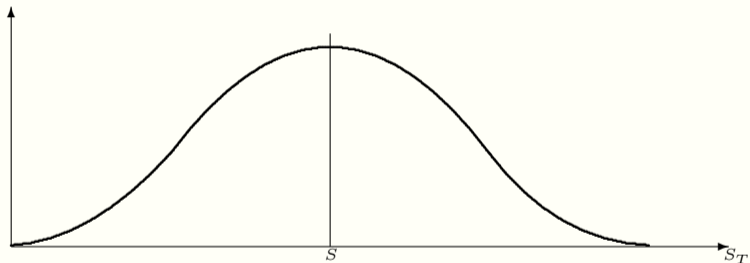
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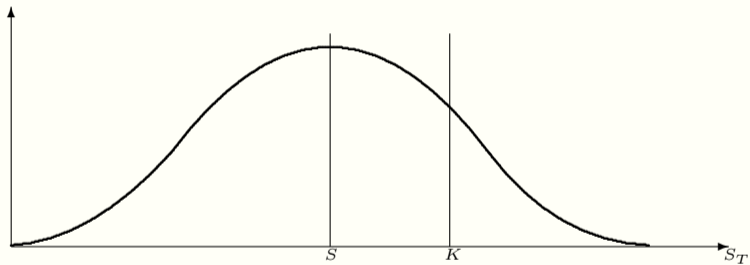
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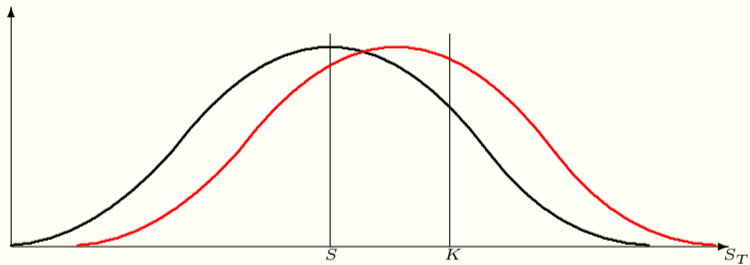
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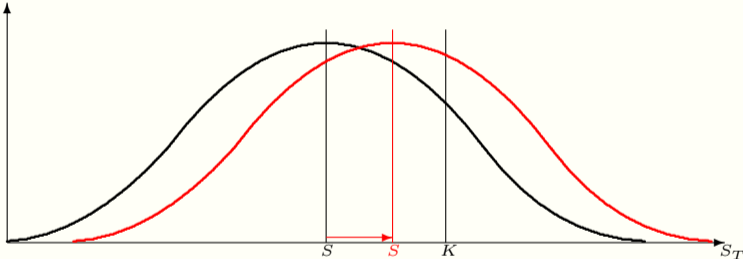
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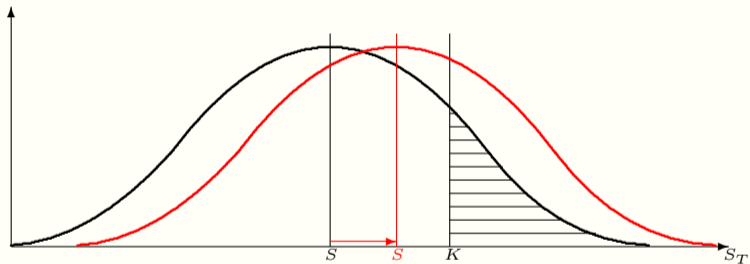
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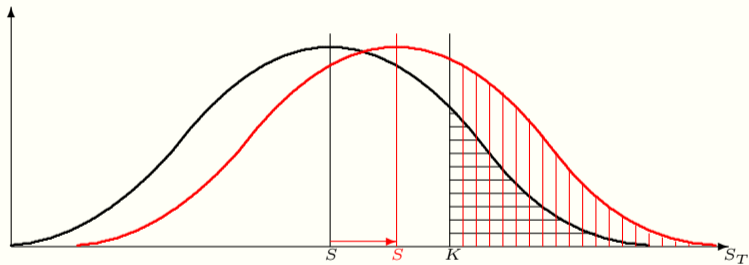
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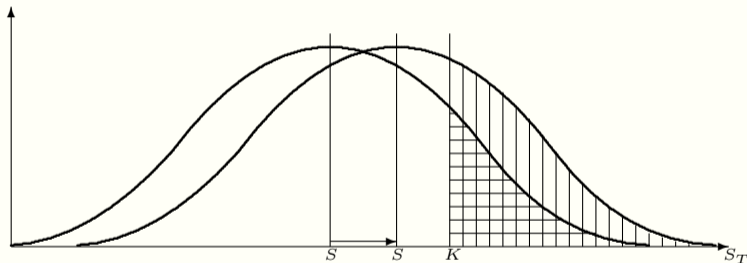
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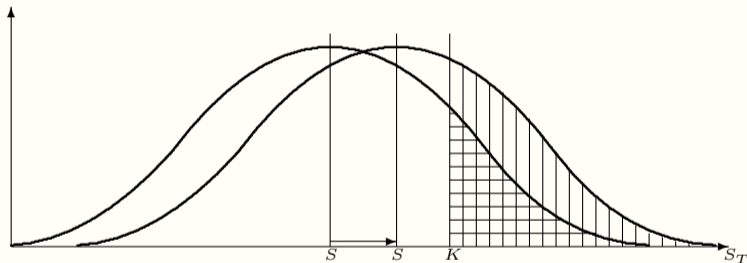


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If the current asset value increases, call options become **more valuable**

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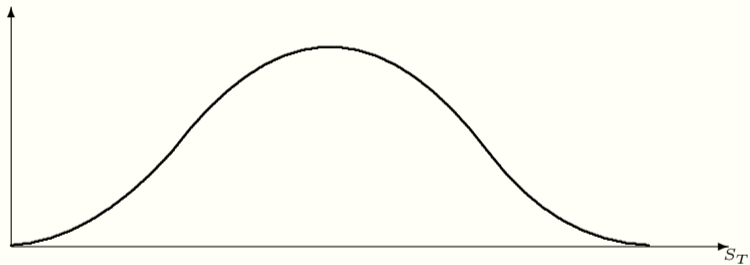
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Strike price

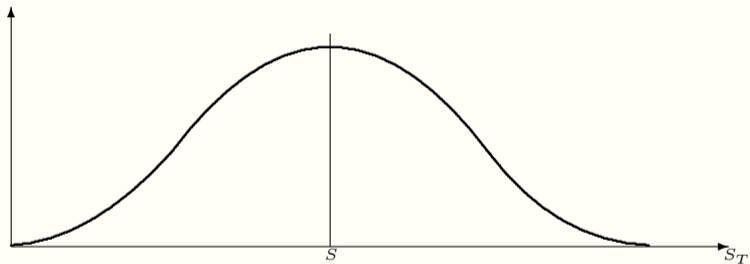
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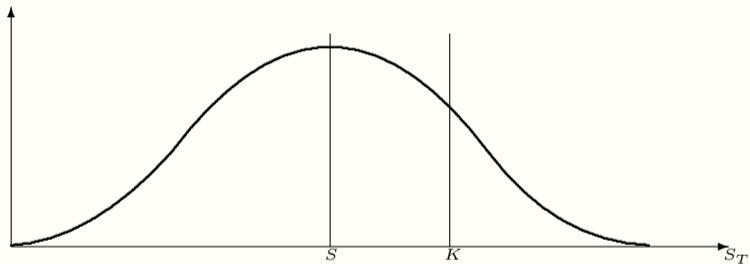
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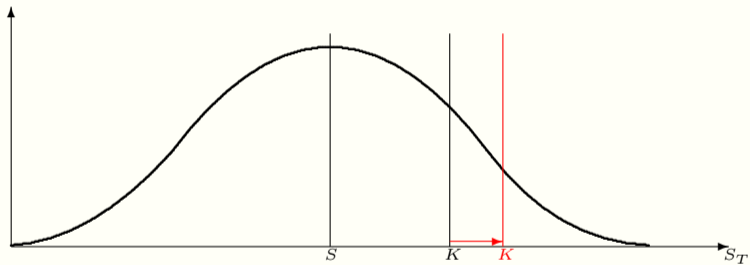
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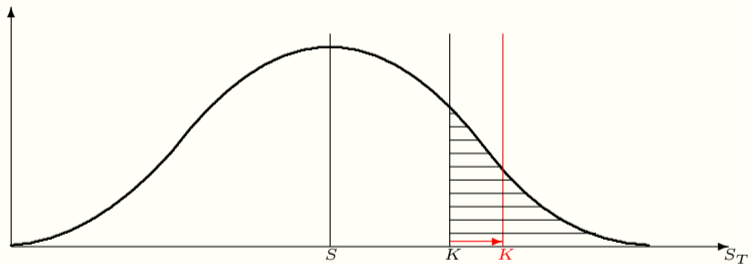
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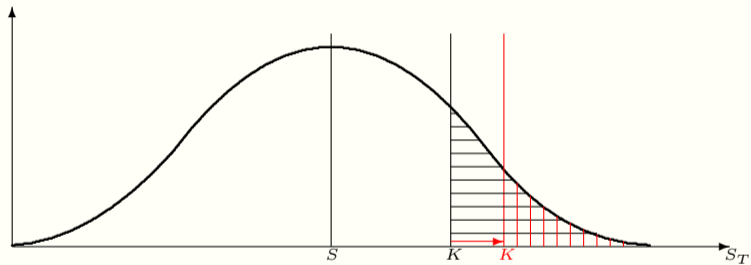
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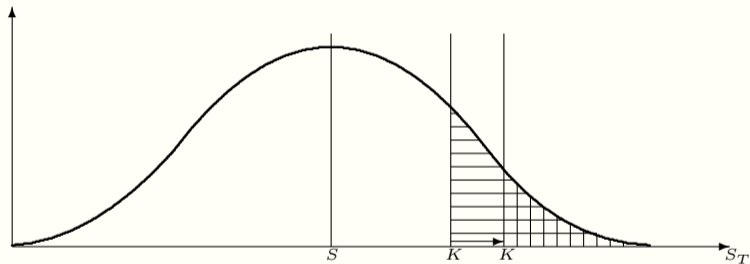
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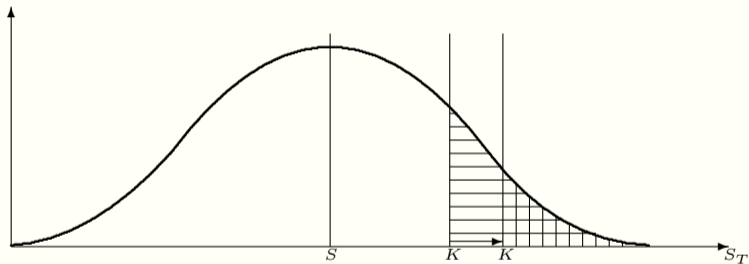


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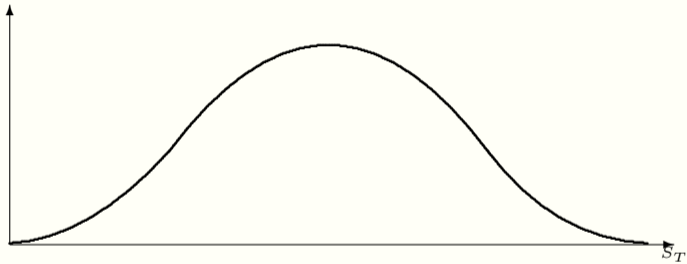
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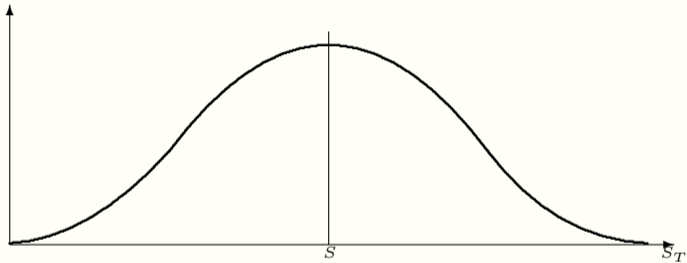
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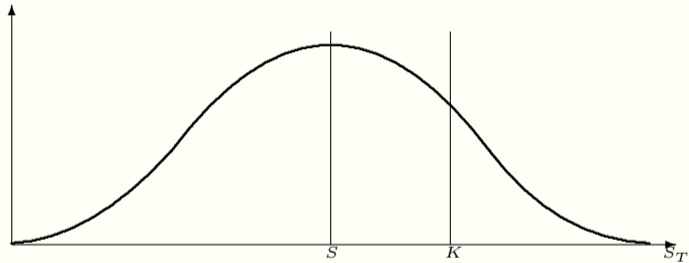
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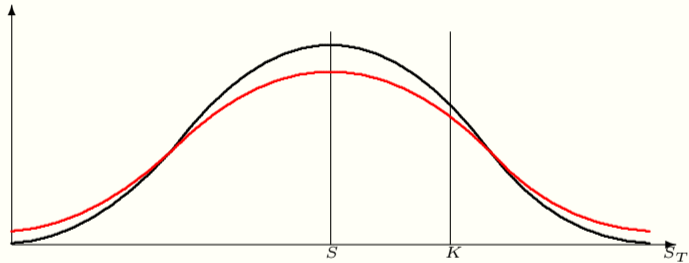
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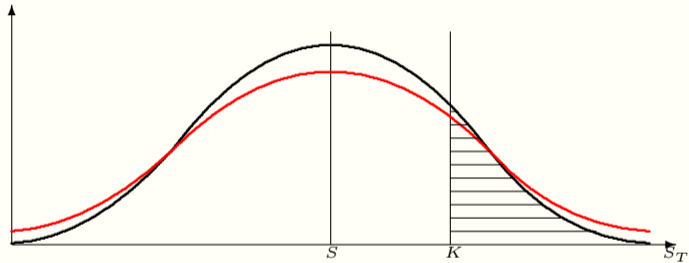
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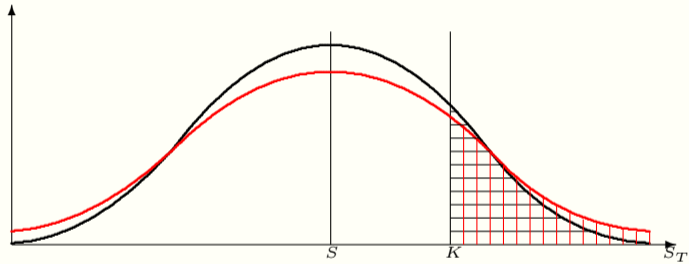
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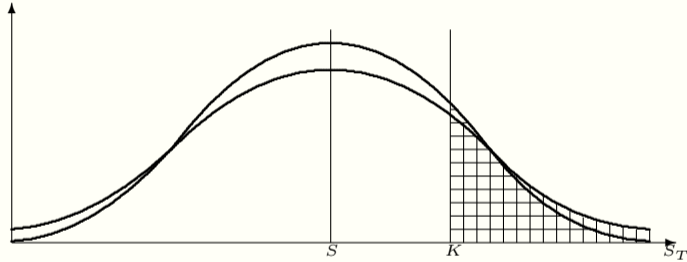
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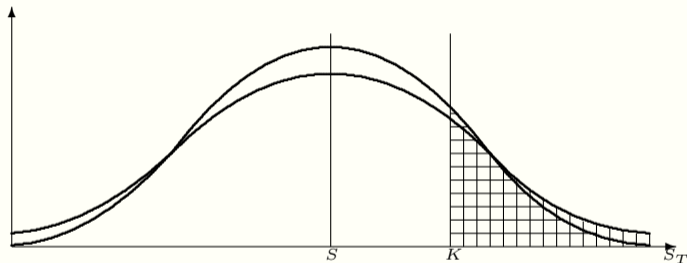


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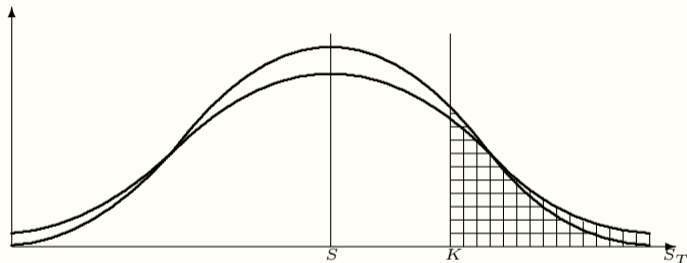
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Vega	$\nu_C = \frac{\partial C}{\partial \sigma} = Sn(d_1)\sqrt{T} = \frac{\partial P}{\partial \sigma} = \nu_P$	
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