



Andreas Krause

Discounted Cash Flows

Stock returns

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- ▶ Returns on investments consist of **capital gains** and **dividend payments**

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