

- We will now explore the implications of portfolio theory for the expected return of assets.
- The result will be one of the best-known and most-widely used models in finance, the Capital Asset Pricing Model (CAPM)

- → We start from the ideas of portfolio selection theory and develop these further to derive the expected returns of assets.
 - From portfolio theory we know that all investors hold the same portfolio of risky assets, which is independent of their preferences.
 - This portfolio was called the optimal risky portfolio (ORP).
 - This ORP is then combined with the risk-free asset, and it is only this combination that depends on the preferences of investors.
- ▶ Using these investment decisions, we will derive how the expected returns must be such that all assets available to investors are actually held.
 - If the returns were higher than this equilibrium, the assets would be attractive and the demand by investors would be higher than the supply.
 - If the returns were lower than this equilibrium, the assets would not be attractive and the demand by investors would be lower than
 the supply.
- ightarrow We can now derive this equilibrium in a very simple way.

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- The capital market line has a slope which is given by the height difference the optimal risky portfolio and the risk-free asset given by the differences in returns, $\mu_P r$, and the difference in risk of σ_p .
- This slope is also known as the Sharpe ratio and can be used as a performance measure when assessing investment strategies.
- We know that the optimal portfolio consist of the optimal risky portfolio, which has weight ω of the risky assets in the total portfolio.
 - This is combined with the risk-free asset.
- The expected return will consist of the expected return from the risky asset comprising the optimal risky portfolio, and the remainder being invested into the risk-free asset. ι denotes a vector of 1s and hence $\omega^T \iota$ would be the sum of all the weights of the risky assets, leaving $1 \omega^T \iota$ as the weight of the risk-free asset.
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- We can now obtain the equilibrium returns of the risky assets.
- We know that the Capital Market Line is touching the efficient frontier.
 - · This implies that the Capital Market Line has the highest possible slope that touches a portfolio, the optimal risky portfolio.
- ▶ [⇒] We will therefore seek a portfolio that maximizes this slope, which implies maximizing the Sharpe ratio over the optimal portfolio weights.
- ightharpoonup [\Rightarrow] Inserting for the expected return and variance and solving the first order condition gives us this formula
- We can now define a vector $\boldsymbol{\beta}$ for convenience.
- ▶ [⇒] This allows us the require the expected return of the risky assets in the more common form.
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- ightarrow The CAPM states that the expected excess returns of an asset, μ_i-r are proportional to the excess return of the market μ_M-r . β_i serves as a risk measure here where for $\beta_i=0$ the expected return is the risk free rate and it increases the higher beta is. The market itself has $\beta_M=1$ as $\sigma_{MM}=\sigma_M^2$.

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- ightharpoonup We can now write the CAPM in the more common form for an individual asset, using β_i for that asset and the portfolio return having been replaced by the market return.
- ightharpoonup The β_i are now the ratio of the covariance of the asset with the market and the market variance.
- ightarrow The CAPM states that the expected excess returns of an asset, μ_i-r are proportional to the excess return of the market μ_M-r . β_i serves as a risk measure here where for $\beta_i=0$ the expected return is the risk free rate and it increases the higher beta is. The market itself has $\beta_M=1$ as $\sigma_{MM}=\sigma_M^2$.

Capital Asset Pricing Model Slide 5 of 7

- ightharpoonup The term $\Sigma \omega$ represents the covariance of the assets with the optimal risky portfolio
- ► The optimal risky portfolio is identical for all investors, it must be the market portfolio

$$\Rightarrow \mu_i = r + \beta_i (\mu_M - r)$$
$$\beta_i = \frac{\sigma_{iM}}{\sigma_M^2}$$

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Capital Asset Pricing Model Slide 6 of 7

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Capital Asset Pricing Model Slide 6 of 7

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Capital Asset Pricing Model Slide 6 of 7

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- → The derivation of the CAPM did depend on the optimal risky portfolio being the market portfolio; we than have to asses the properties of the market portfolio, the expected return and variance, as well as the covariance of each asset with the market portfolio.
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 - It will also have to include all bonds, whether corporate bonds or non-risk-free government bonds.
 - Investors can also purchase real estate, commercial and residential property.
 - Investors will in general also have access to non-listed companies through private equity funds or investing directly.
 - Another investment possibility are hedge funds, who often have very different investment strategies.
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