

- We will provide an explanation why occasionally stock markets might crash, while on other occasions in a similar situation no crash occurs.
- We will firstly look at why investors might still invest into stocks even if they know that a crash might occur and then look a mechanism that could trigger such a crash.

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- → While many movements in asset prices can at least be explained ex-post, there are significant events, such as sudden large price drops, that cannot be explained easily, even retrospectively.
 - Stock markets are sometimes observed to loose a substantial fraction of their value
 - and this loss happens in a very short period of time. The time frame may range from a few minutes or hours to a few days. In any case, for the scale of the loss in value, the movement of price is very fast.
- ▶ Of course, if new information arrives or becomes more widely known that suggests stocks are worth less than their current price, then such movements are easily explained. It is however, events in which no information arrives that could justify the price movement we are interested in.
- ▶ We can also exclude a change in the preferences of investors that lead to a change in demand, or other changes in their behaviour.
- If there are no apparent reasons for the sudden price drop, we speak of a 'crash'.
 - Crashes are most prominently discussed in the context of stock markets,
 - but we see similar developments in real estate, although given the nature of transactions the crash usually plays out over months.
 - Exchange rates occasionally also see crashes of a currency,
 - as do some commodities.
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 - Explanations of crashes are often difficult, especially with the benefit of hindsight.
 - One explanation often used is that stocks were overvalued at the time and hence the crash a correction. While such an explanation might sound appropriate well after the event, at the time of the crash there might not have been a consensus of stocks being overvalued and even if there was a consensus to this effect, it might have been held for a long period of time prior to the crash. The reason for the crash to occur that particular moment remains undiscovered.
- Also, it other times, markets are overvalued, which seems to be common knowledge, and the stock prices either adjust slowly downwards towards the fundamental value or they remain stable until the fundamental value has increased to reach the price. In either case, no crash is observed.
- We will in the first model look at why overvaluations can be sustained for long periods of time,
 - and also how a correction is affected in that model.
- We will then in a second model explain the occurrence of crashes in some situations more carefully, avoiding the randomness of crashes in the previous model. We will look at a situation in which no(t much) information is responsible for the crash.
- → We will thus firstly looking at how overvaluations can be sustained and then will look at why sometimes the market crashes to correct these high prices.

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 - We often find that assets in financial markets are overvalued. Such overvaluations are not the result of asymmetric information between market participants or the lack of information, but they are often commonly known and openly acknowledged. Such overvaluations often persist for prolonged periods of time.
 - While overvaluations are often observed, the same cannot be said of undervaluations. In most markets, undervlautions are rarely observed and if
 they are occurring, are short-lived only.
- ▶ We will discuss a model that shows it can be rational to invest into assets that an investor knows to be overvalued.
 - The overvaluation will at some point lead to a sudden price correction, a crash.
 - The explanation given in this model is highly unsatisfactory and we will discuss the mechanism of the crash in more detail in the second model.
- We can now develop a model of bubbles, that is long periods of prices exceeding the fundamental value, that can be used to explain the willingness of investors to purchase overvalued assets.

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- We will discuss a model that shows it can be rational to invest into assets that an investor knows to be overvalued.
 - The overvaluation will at some point lead to a sudden price correction, a crash.
- The explanation given in this model is highly unsatisfactory and we will discuss the mechanism of the crash in more detail in the second model.
- → We can now develop a model of bubbles, that is long periods of prices exceeding the fundamental value, that can be used to explain the willingness of investors to purchase overvalued assets.

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- Many assets are frequently overvalued, while under-valuations are rarely found
- ▶ We will see why it is rational to invest into an overvalued asset
- Overvalued assets will eventually lead to a crash

- \rightarrow We will firstly look at overvaluations and the reasons why they might be able to persist, even if all market participants agree that assets are overvalued.
 - We often find that assets in financial markets are overvalued. Such overvaluations are not the result of asymmetric information between market participants or the lack of information, but they are often commonly known and openly acknowledged. Such overvaluations often persist for prolonged periods of time.
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Bursting bubbles

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Stochastic bursting of bubbles is unsatisfactory as an explanation of such significant events

As prices are driven by demand and supply in the market, we should investigate these factors for an explanation

Dividing investors into informed investors and uninformed investors allows us to introduce hedging by investors

We will see how hedging by uninformed investors can lead to market crashes

- ightarrow We will now focus on modelling the actual causes of crashes, a sudden change in the demand.
- It is very unsatisfactory to explain rare and significant events with the random bursting of a bubble. To aid our understanding of crashes, we would want to demonstrate mechanism that will cause such a crash and investigate the conditions required to trigger it.
- Prices are equilibrium prices, thus points at which demand and supply meet. It would therefore be appropriate to asses the demand and supply as the driving force behind these equilibrium prices. We will take the supply of assets as given, such as the number of shares issued, the number of properties available and will focus ont he demand for holding such assets.
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Copyright (C) 2024 by Andreas Krause Market crashes



If hedging is widespread after a prolonged market rise, the demand for assets in non-monotonous
 Small negative information can cause a large drop in asset prices
 Markets rise and fall over time, but not every time a crash occurs, why would markets most of times move slowly?
 We need a large amount of hedging and this hedging has to be at roughly the same strike price, only then do we observe a crash, if either conditions is not to the conditions.

- If we have a rise in the price of an asset, uninformed investors might want to hedge their demand as they cannot know if this rise is due to the fundamental value increasing or a bubble having emerged. To protect themselves against any losses they will increasingly hedge their investment and this hedging demand or causes the demand for the asset to become non-monotonous.
- Due to this non-monotonicity we can have a situation where a small piece of negative information instigates a large drop in the price of the asset. the information itself does not justify this price drop.
- [?] Markets are moving up and down a lot and crashes are a rare occurrence, for entire markets as well as individual assets. Hence most of times the prices move smoothly rather than crash. Why?
- [!] For crashes to occur hedging must be widespread and the strike prices need to be similar, otherwise the non-monotonicity of the demand does not emerge and hence we cannot observe a crash. Thus is will be that most of times either of these two conditions is not fulfilled, so either investors are not much concerned about losses from overvalued assets and therefore do not hedge, or they are concerned, but employ widely differing strike prices for their protection.
- → We see that we need quite specific conditions for crashes to occur and these conditions will not be fulfilled frequently; thus crashes are rare events.

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- ? Markets rise and fall over time, but not every time a crash occurs, why would markets most of times move slowly?

- $\,\rightarrow\,\,$ We have seen that the origin of crashes lies in the hedging of investors.
- If we have a rise in the price of an asset, uninformed investors might want to hedge their demand as they cannot know if this rise is due to the fundamental value increasing or a bubble having emerged. To protect themselves against any losses they will increasingly hedge their investment and this hedging demand causes the demand for the asset to become non-monotonus.
- Due to this non-monotonicity we can have a situation where a small piece of negative information instigates a large drop in the price of the asset. the information itself does not justify this price drop.
- [?] Markets are moving up and down a lot and crashes are a rare occurrence, for entire markets as well as individual assets. Hence most of times the prices move smoothly rather than crash. Why?
- [!] For crashes to occur hedging must be widespread and the strike prices need to be similar, otherwise the non-monotonicity of the demand does not emerge and hence we cannot observe a crash. Thus is will be that most of times either of these two conditions is not fulfilled, so either investors are not much concerned about losses from overvalued assets and therefore do not hedge, or they are concerned, but employ widely differing strike prices for their protection.
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Andreas Krause Department of Economics University of Bath Claverton Down Bath BA2 7AY United Kingdom

E-mail: mnsak@bath.ac.uk