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► Companies retain the outcome

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▶ Banks obtain the outcome if the loan cannot be repaid and are repaid for higher outcomes, up to the maximum loan rate at which companies demand loans

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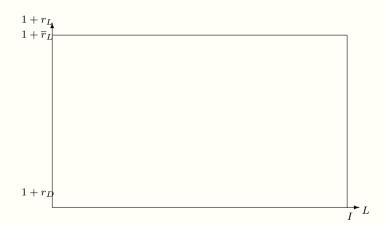
$$\Rightarrow \frac{\partial \Pi_B}{\partial L} = \frac{1 + r_L}{1 + \overline{r}_L} > 0$$

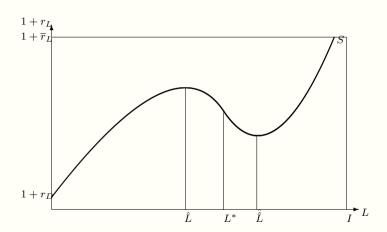
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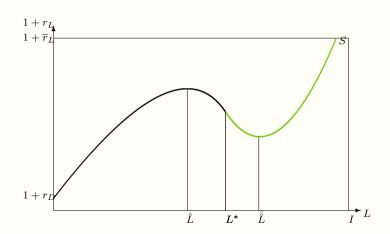


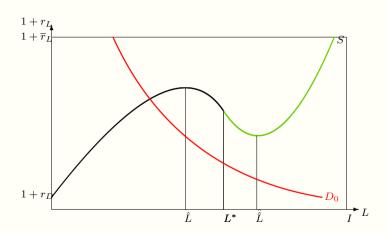
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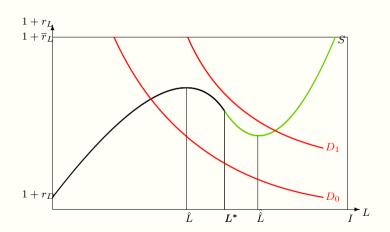


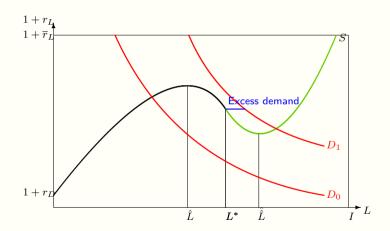


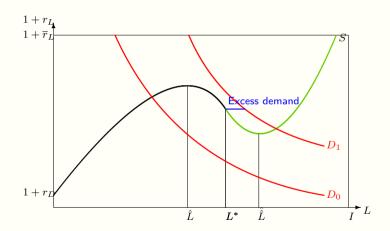












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