

Chapter 17.2.1

The optimality of deposit insurance limits

Outline

- Problem and model assumptions
- No deposit insurance
- Full deposit coverage
- Partial deposit coverage
- Summary

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Dividing deposits

- ▶ The amount of deposits covered by deposit insurance is usually limited
- ▶ Depositors may divide their deposits between banks to increase their coverage
- ▶ Banks compete with deposit rates and might retain larger deposits if these are sufficiently attractive
- ▶ Banks might find it optimal to limit deposit insurance to attract parts of larger deposits

Differentiated accounts

- ▶ Depositors have deposits D or $2D$ and deposit insurance might be limited to D
- ▶ Banks offer differentiated accounts and moving deposits to another bank involves costs depending on these differences
- ▶ Banks are one unit apart and depositors are uniformly distributed on this line with distance d_i

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Switching banks

- ▶ Depositors staying with bank j are repaid deposits if the loans are repaid to the bank and lose their deposits otherwise
 - ▶ $\Pi_D^{jj} = \pi(1 + r_D^j) \hat{D} - \hat{D} - (1 - \pi) \hat{D}$
 - ▶ Depositors switching banks to bank i are repaid deposits if the loans are repaid to the bank and lose their deposits otherwise, and they face switching costs
 - ▶ $\Pi_D^{ji} = \pi(1 + r_D^i) \hat{D} - \hat{D} - (1 - \pi) \hat{D} - cd_i$
 - ▶ Depositors switch if this is profitable: $\Pi_D^{ij} \geq \Pi_D^{ii}$
- $\Rightarrow d_i \leq d_i^* = \pi \frac{(1+r_D^i)-(1+r_D^j)}{c} \hat{D}$

Bank profits

- ▶ Deposits a bank holds will consist of existing large and small deposits, plus those it attracts from the other bank

- ▶
$$D_i = \lambda \left(1 + 2\pi \frac{(1+r_D^j) - (1+r_D^i)}{c} \right) 2D + (1 - \lambda) \left(1 + \pi \frac{(1+r_D^j) - (1+r_D^i)}{c} \right) D$$

- ▶ Banks profits are generated if loans are repaid, consisting of these repaid loans after deposits are repaid

- ▶
$$\Pi_B^i = \pi \left((1 + r_L) - (1 + r_D^i) \right) D_i$$

- ▶ The optimal deposit rate is obtained if
$$\frac{\partial \Pi_B^i}{\partial (1+r_D^i)} = 0$$

$$\Rightarrow 1 + r_D^* = (1 + r_L) - \frac{1-\lambda}{\pi(1+3\lambda)} \frac{c}{D}$$

$$\Rightarrow \Pi_B^* = \frac{(1+\lambda)^2}{1+3\lambda} D$$

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Switching banks

- ▶ Deposits are always repaid and if switching, the switching costs are to be paid
 - ▶ $\Pi_D^{jj} = (1 + r_D^j) \hat{D} - \hat{D}$
 - ▶ $\Pi_D^{ji} = (1 + r_D^i) \hat{D} - \hat{D} - cd_i$
 - ▶ Depositors switch if this is profitable: $\Pi_D^{ij} \geq \Pi_D^{ii}$
- $\Rightarrow d_i \leq d_i^{**} = \frac{(1+r_D^i)-(1+r_D^j)}{c} \hat{D}$

Bank profits

- ▶ Deposits at the bank are $D_i = (1 + \lambda) D + \frac{(1+r_D^i)-(1+r_D^j)}{c} (1 + 3\lambda) D^2$
 - ▶ Maximizing bank profits gives $1 + r_D^{**} = (1 + r_L) - \frac{1+\lambda}{3+\lambda} \frac{c}{D}$
- ⇒ $\Pi_B^{**} = \pi \frac{(1+\lambda)^2}{1+3\lambda} D = \pi \Pi_B^*$
- ▶ Full deposit coverage gives banks less profits than no deposit insurance
 - ▶ Competition for deposits has increased as the profits of depositors have increased and more can switch
 - ▶ The lower deposit rate due to the absence of risk does not compensate for this sufficiently

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Switching opportunities

- ▶ Large depositors will only be covered for their deposits up to D
- ▶ They can stay with bank j and have D repaid for sure and D only repaid if the loan is repaid to the bank
- ▶ $\Pi_D^{jj} = (1 + r_D^j) D - D + \pi (1 + r_D^j) D - D - (1 - \pi) D$
- ▶ They can stay switch entirely to bank i and have D repaid for sure and D only repaid if the loan is repaid to the bank, and bear switching costs
- ▶ $\Pi_D^{ji} = (1 + r_D^i) D - D + \pi (1 + r_D^i) D - D - (1 - \pi) D - cd_j$
- ▶ They can switch D to bank i and have the full deposits insured, bearing switching costs
- ▶ $\Pi_D^{jij} = (1 + r_D^j) D - D + (1 + r_D^i) D - D - cd_j$

Switching decision

- ▶ Large depositors switch parts of their deposits if $\Pi_D^{jj} \geq \Pi_D^{ij}$

$$\Rightarrow d_i \leq d_i^{***} = \frac{(1+r_D^j) - \pi(1+r_D^i) + (1-\pi)}{c} D$$

- ▶ Large depositors are attracted from other banks seeking to increase their deposit insurance coverage
- ▶ Large depositors are lost to other banks seeking to increase their deposit insurance coverage
- ▶ Small depositors will be fully insured and behave as indicated above
- ▶
$$D_i = \lambda \left(2D - \frac{(1+r_D^j) - \pi(1+r_D^i) + (1-\pi)}{c} D^2 + \frac{(1+r_D^i) - \pi(1+r_D^j) + (1-\pi)}{c} D^2 \right) \\ + (1 - \lambda) \left(D + \frac{(1+r_D^i) - (1+r_D^j)}{c} D^2 \right)$$

Bank profits

▶ Maximizing bank profits gives $1 + r_D^{***} = (1 + r_L) - \frac{1+\lambda}{1+\pi\lambda} \frac{c}{D}$

$$\Rightarrow \Pi_B^{***} = \pi \frac{(1+\lambda)^2}{1+\pi\lambda} D$$

▶ These profits are higher than no deposit insurance if $\pi > \frac{1}{1+2\lambda}$

▶ In this case competition for large deposits is not too strong to negate the effect of the lower deposit rate due to them not being exposed to risk

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Increased competition with deposit insurance

- ▶ If banks are not too risky they prefer deposit insurance to be limited to smaller deposits
- ▶ More risky banks would prefer no deposit insurance at all
- ▶ Deposit insurance increases competition for deposits but also reduces deposit rates due to the elimination of risk
- ▶ Higher-risk banks see a stronger competition effect and will therefore prefer not to have any deposit insurance

Optimal limited coverage

- ▶ Deposit insurance is not provided to large deposits unless banks are highly risky
- ▶ If deposit insurance is not provided free, this will make the benefits of partial insurance coverage over full coverage more pronounced
- ▶ Banks are content with limits on deposit insurance as this limits competition for large deposit



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