Andreas Krause

Chapter 14.1.2

Coordination of deposit withdrawals

Losses from withdrawing deposits

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Loan sales to finance deposit withdrawals

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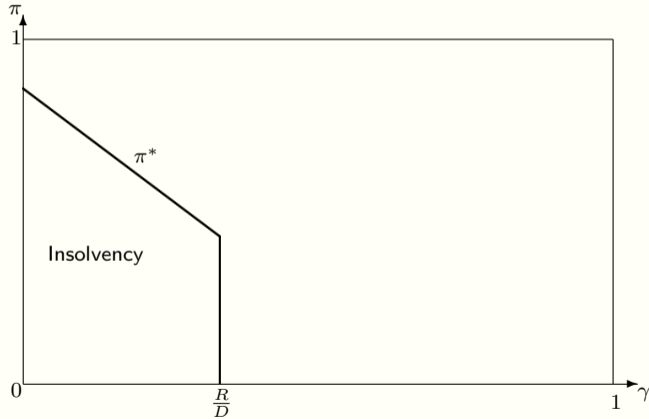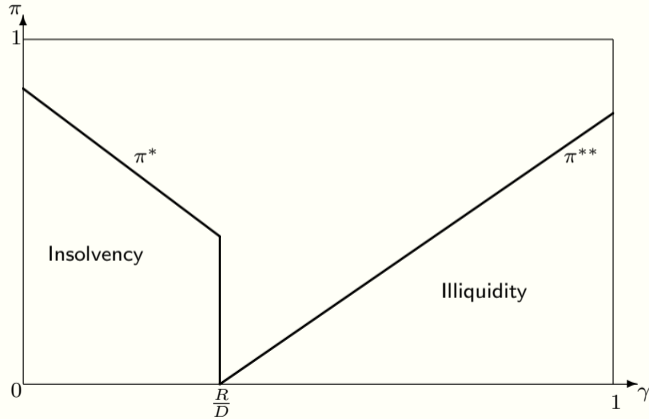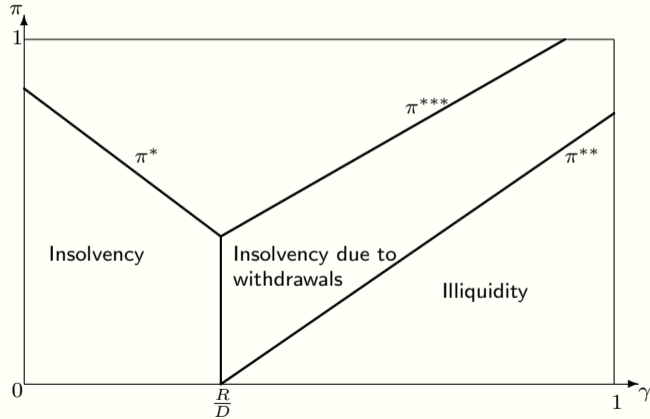
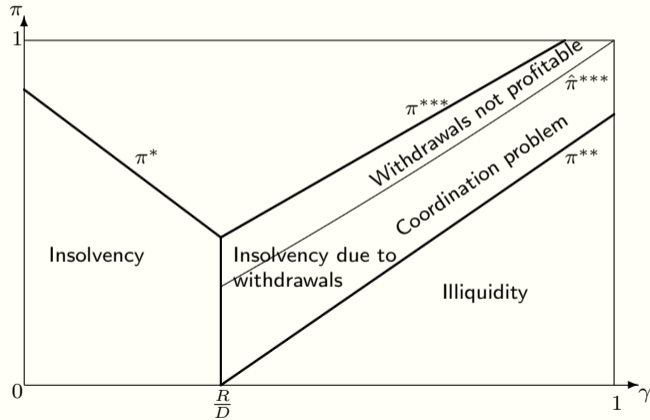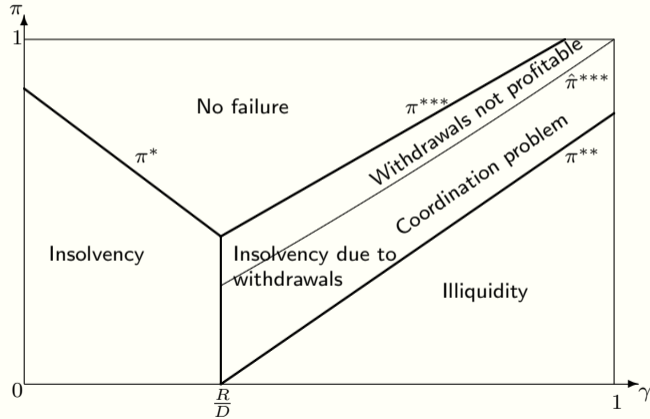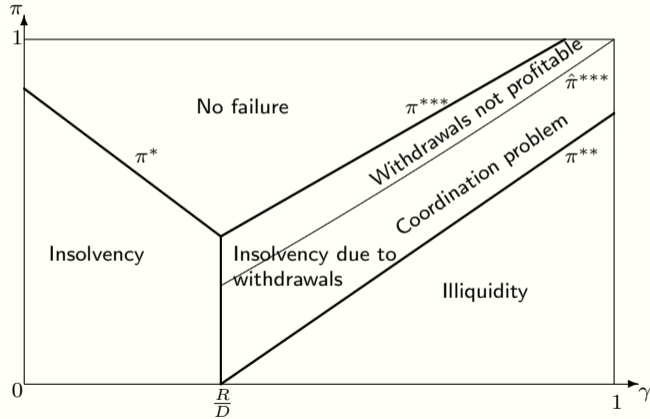# Bank failures due to deposit withdrawals

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This presentation is based on
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