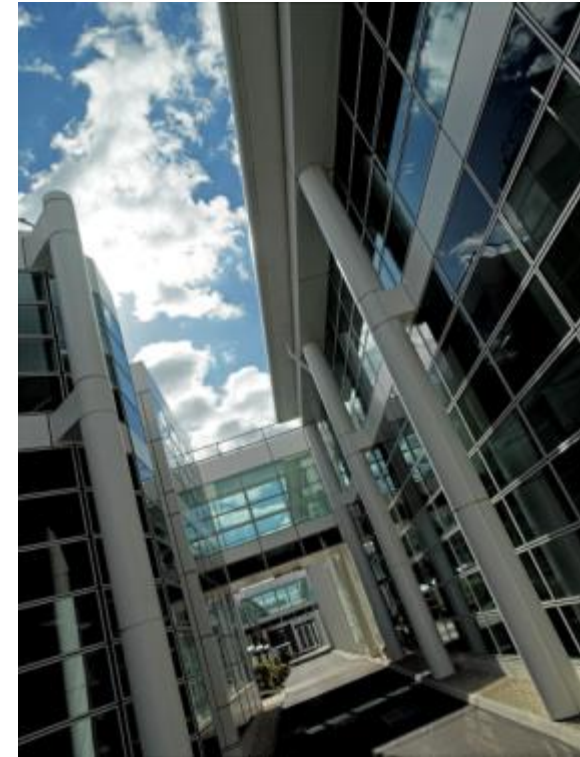




About NPL ...

The UK's national standards laboratory

- Founded in **1900**
- World leading **National Measurement Institute**
- ~750 staff; 550+ specialists in Measurement Science plus 200 visiting researchers pa
- State-of-the-art laboratory facilities
- 388 Laboratories (35,746 sq. metres)
- The heart of the UK's **National Measurement System** to support business and society
- Experts in **Knowledge Transfer**



What do we do

- Develop & disseminate UK's measurement standards, ensure they are internationally accepted
- Multidisciplinary R&D and technical services for public and private sector
- Knowledge transfer and advice between industry, government and academia
- Promotion of science and engineering



SI Units



kilogram

Mass



metre

Length



second

Time



ampere

Electric Current



kelvin

Temperature



candela

Luminous Intensity



mole

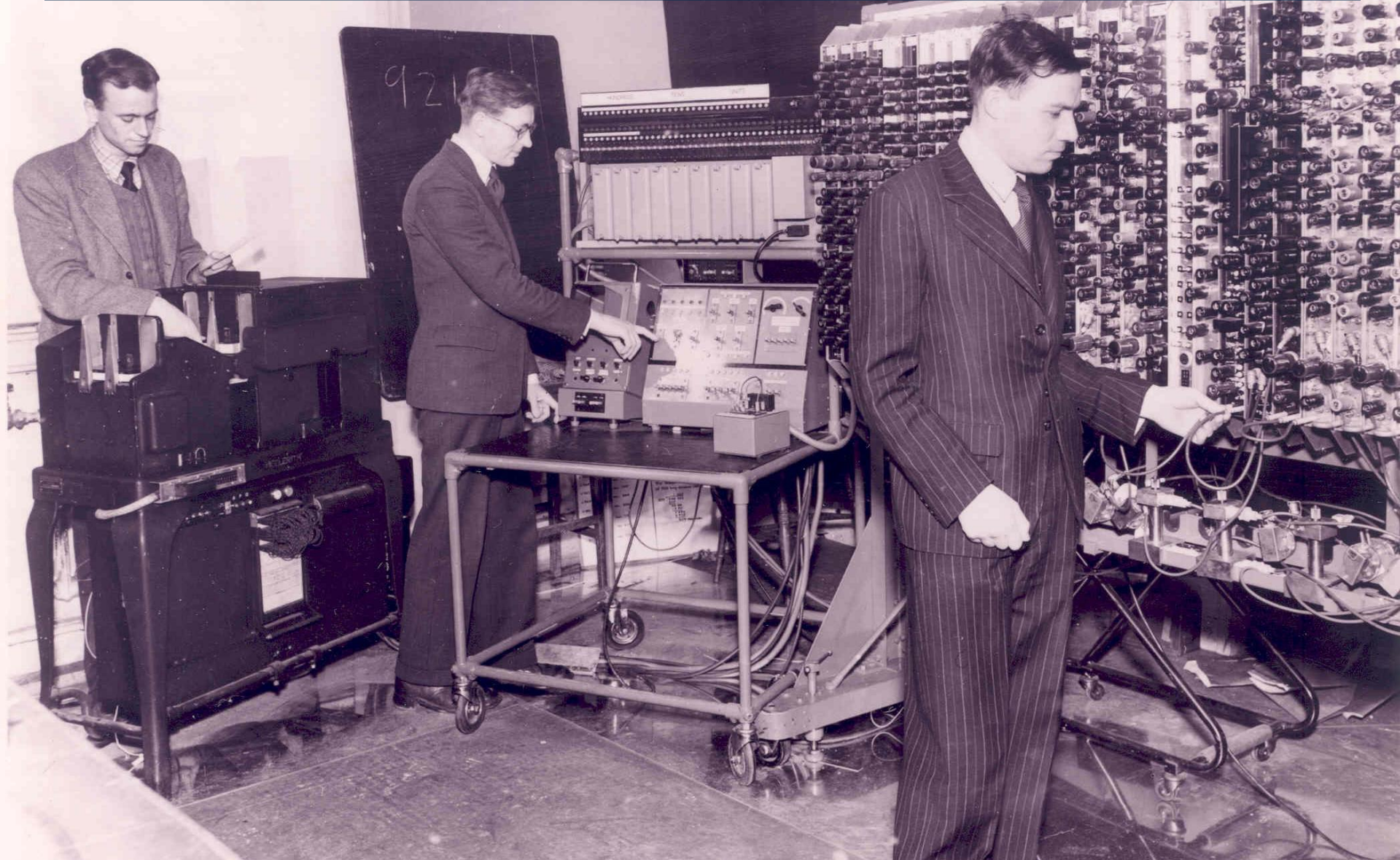
Amount of Substance

NPL's Calibration Services

- Mass
- Neutrons
- Photometry
- Radioactivity
- Radiometry
- RF & microwave
- Spectrophotometry
- Thermal
- Time & frequency
- Optical power and frequency
- Laser measurements
- Force & pressure
- Infra-red radiation
- Ultrasonics
- Gas standards
- Ionising radiations
- Acoustics
- DC & LF
- Fibre optics



World's first Automatic Computing Engine (ACE) 1946

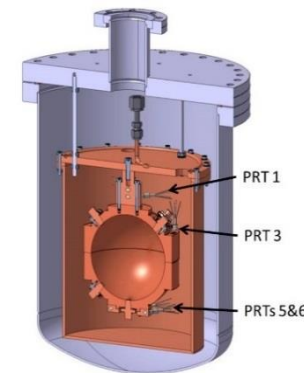
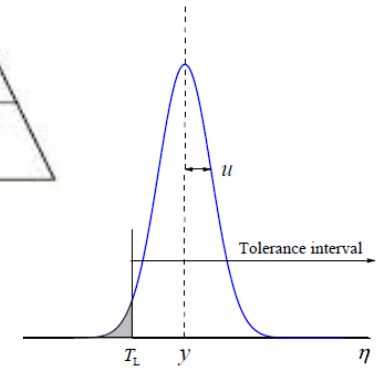


Packet-switching developed at NPL 1966



Data science

- Ensuring measurements are traceable to standard units
- Ensuring inferences, predictions and decisions are quality-assured
- Measurements made inside the laboratory
“theory-heavy, data-light”
- Measurements made outside the laboratory
“theory-light, data-heavy”



Promoting confidence in (the use of) data

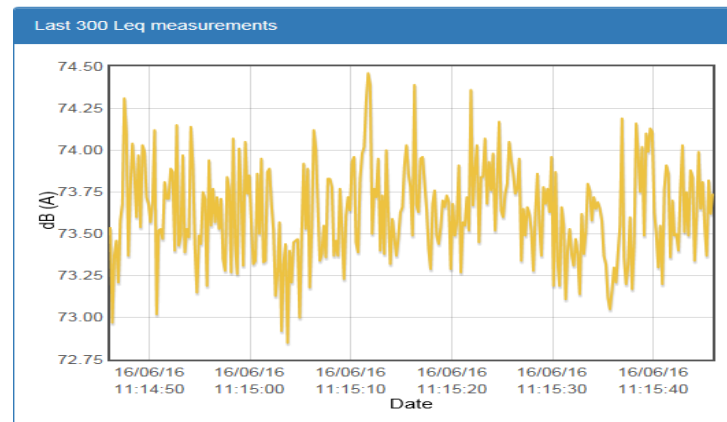
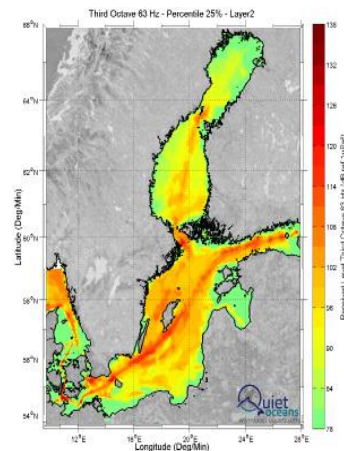
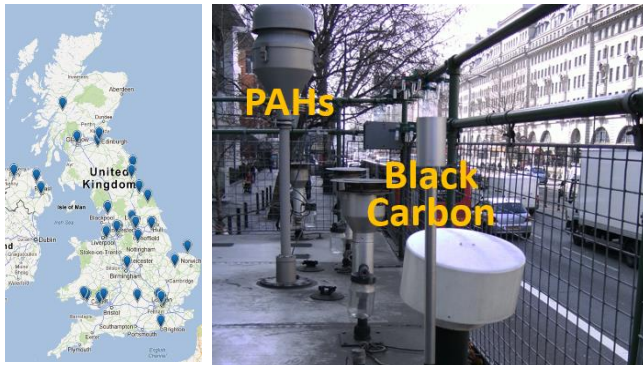
- Measuring and transmitting data
 - Integrity** and security of data
 - Providing legitimate access to data and information
 - Detecting faults, corruption, malicious interventions
- Storage and retrieval of data
 - Provenance** of data
 - Metadata: when, where, how it was captured
 - Cleaning and curating data
- Data analytics
 - Extracting knowledge from data
 - Uncertainty** quantification, with contributions from data, models, algorithms, computation, training sets, software, etc.

Sensor networks

- Collection of (often) many low-cost sensors making discrete measurements (in space, time and frequency) of quantities that vary continuously (in space, time and frequency)
- Can operate at different scales (factory, neighbourhood, city, region, global)
- Source of large volumes of data
- Want to use data to make predictions and decisions, for source identification and attribution, all supported by statements of uncertainty

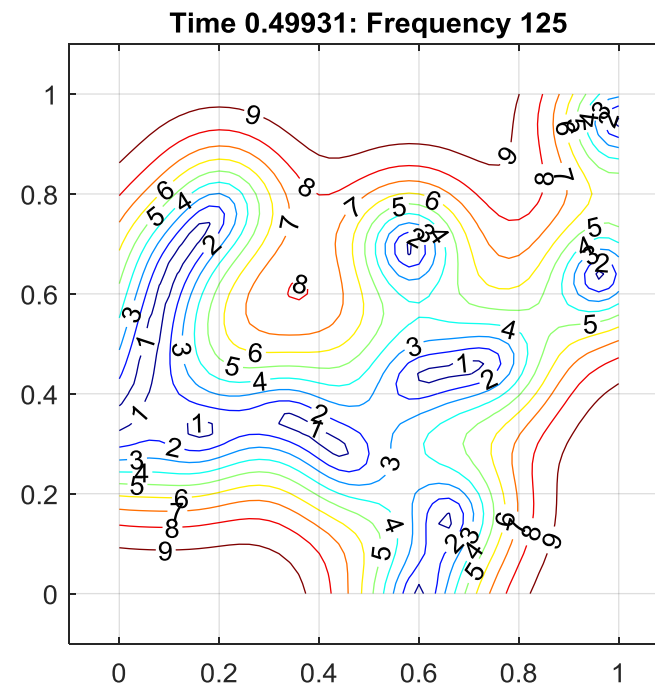
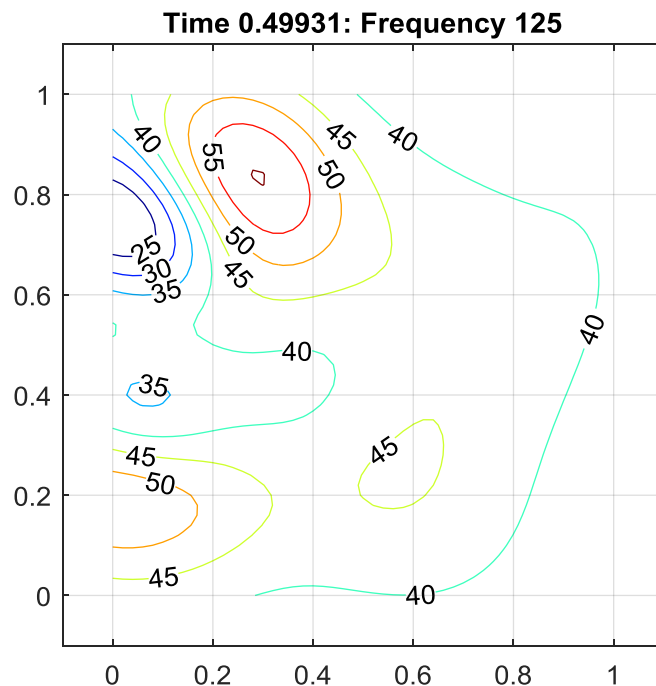
Examples

- Underwater acoustic noise in oceans
- Air quality and airborne noise in urban environments
- Radiometric measurements from satellites for EO



Prediction problem

- Create spatial-temporal-frequency maps of both estimates and uncertainties for measured quantities
- Can we exploit the co-location of sensor networks operating with different modalities (measuring different quantities that are dependent)?



Prediction problem

- GPs a useful tool but can be difficult to apply when the size of the training set exceeds a few thousand
(Example of airborne acoustic network provided 500,000 measured values per day for many weeks)
- Given training set (X, y) , a GP with covariance function $k(x_1, x_2)$, and noise variance σ_n^2 :

$$y_* = K(X_*, X)[K(X, X) + \sigma_n^2 I]^{-1}y,$$

$$\text{cov}(y_*) = K(X_*, X_*) - K(X_*, X)[K(X, X) + \sigma_n^2 I]^{-1}K(X, X_*)$$

(Requires solution of large symmetric systems of equations)

Prediction problem

- Learning about parameters of covariance function and σ_n^2 by maximising log-likelihood:

$$\log p(y|X) \propto -\frac{1}{2} y^T [K(X, X) + \sigma_n^2 I]^{-1} y - \frac{1}{2} \log |K(X, X) + \sigma_n^2 I|$$

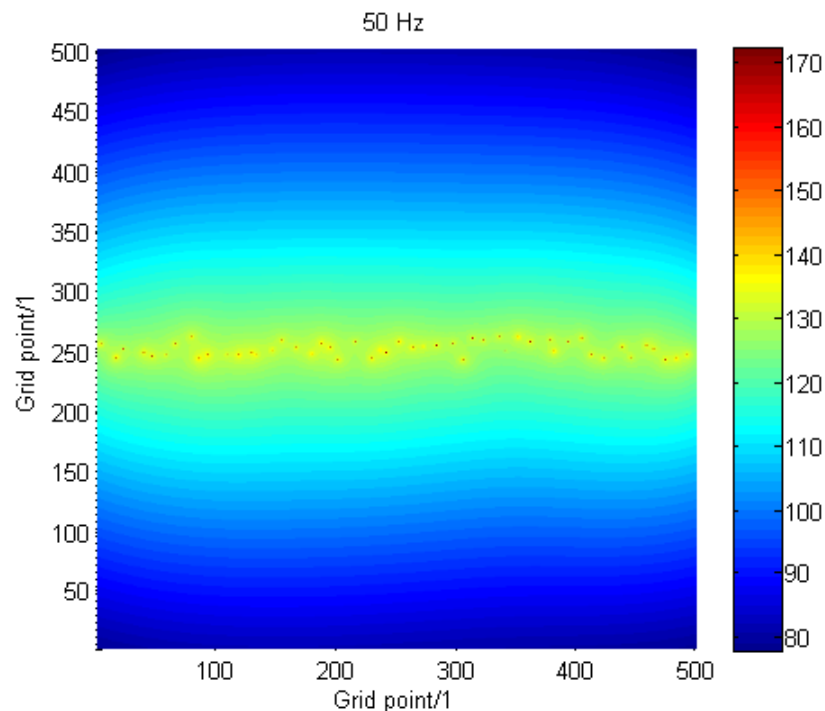
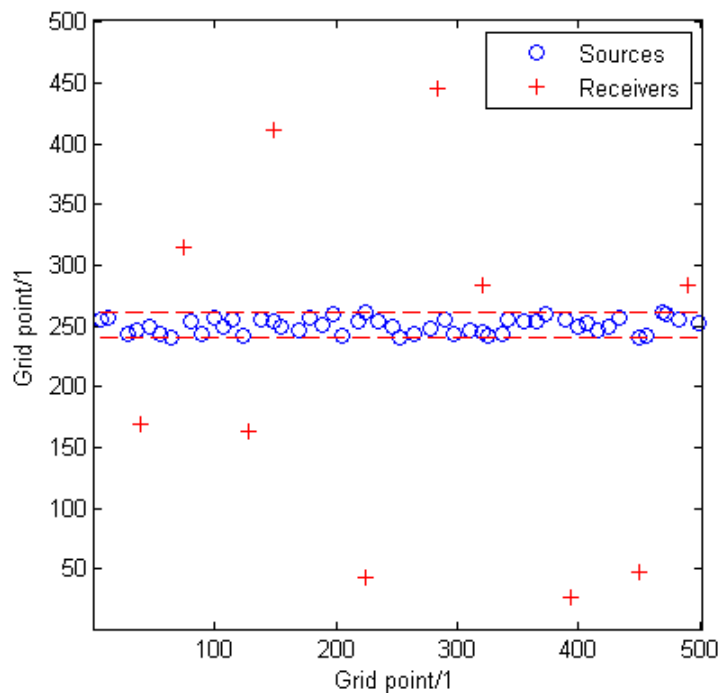
(Evaluation also requires eigenvalues of large symmetric matrix)

- Exploit structure of data (gridded) and structure of covariance function (separable) to decompose matrices as tensor matrix products ... then, e.g., combine with iterative methods to solve equations

(Copes with large problems but computations are slow)

Source identification and tracking problem

- Add knowledge that the measured quantity depends on a small number of sources and a model for how the quantity varies with distance from a source
(For an acoustic problem, this could be a model of propagation loss)



Source identification and tracking problem

- For a single time instant, vector s represents source factors at possible source locations (within shipping lane)
- Find solution $s \geq 0$ to minimize

$$\|As - y\|_2^2 + \tau \|s\|_1$$

First term matches model to sensor observations y : highly under-determined system: maybe ~ 100 observations but $\sim 10,000$ unknowns

Second term regularises solution by forcing sparsity

Parameter τ used to control balance between “fitting” data and level of sparsity

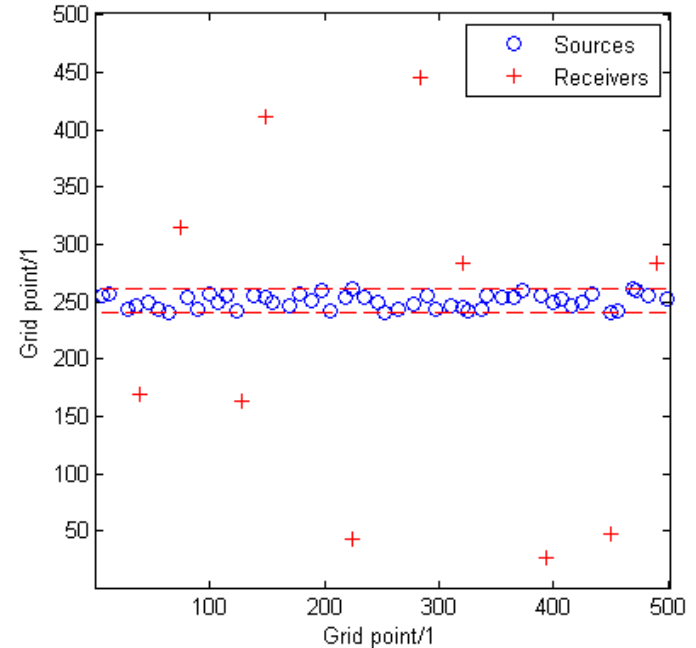
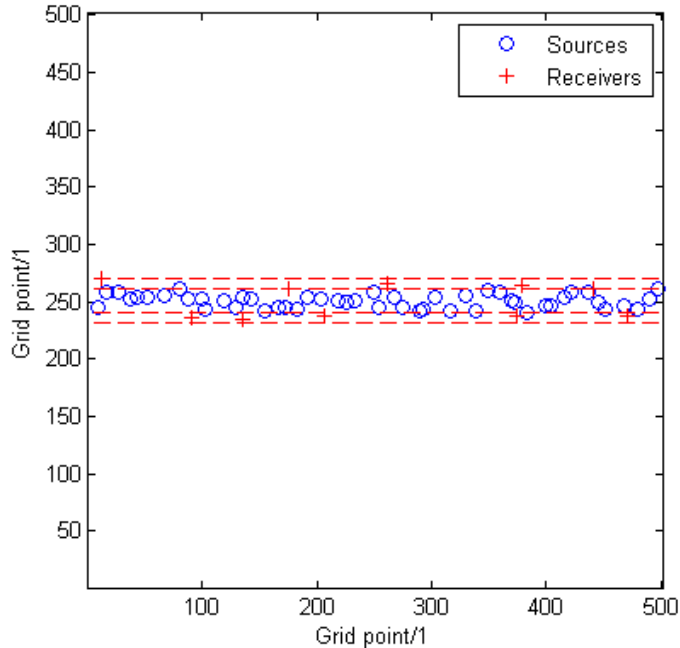
Columns of design matrix A are highly coherent, which limits the “spatial resolution” to which the source locations can be estimated

Source identification and tracking problem

- Account for additional knowledge that locations of some of the sources are known (from GPS transponder data), but not their source levels
- Use knowledge of the precision of the sensors to provide uncertainty evaluation
(LASSO \longrightarrow Bayesian LASSO?)
- Use data recorded at consecutive times to track sources
(The sources can be expected to move along continuous paths ... initially straight-lines ... and to have a constant source level)
(“Real-time” solution in the form of a “filter”?)

Design problem

- To deploy a sensor network, need to decide
 - Number of sensors
 - Locations of sensors
 - “Quality of sensors”: short-term (noise characteristics) and long-term (drift characteristics)



Design problem

- Optimise a measure of information (gain)
 - E.g., trace of covariance matrix for predictions made at a number of spatial locations
- But balanced against constraints
 - On cost (dependent on number and quality of sensors)
 - On where the sensors may be located (e.g., shipping lane is inaccessible)
- May also be a design specification
 - Requirement to make a prediction that meets a target uncertainty

- **Real airborne acoustic sensor network data**
(~15 sensors measuring at ~30 frequencies every minute for seven days — some data is missing — possibility of providing data for much longer period)
- **Simulated underwater acoustic sensor network data**
(Investigating possibility of accessing real data measured in the Baltic Sea — but a propagation loss function would be needed)
- **Air quality sensor network data**
(Possibility of accessing data from networks run by NPL — some low resolution [daily] ozone concentration data recorded over a number of years at a number of sites across the UK is available)



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