## Liquidean distance

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## Groundwater network

- A map of Nitrate
  Vulnerable Zones is made
  using ordinary Kriging.
- Currently, covariance
  structure is assumed to
  depend only on distance
  between points.



## Water quality estimation



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# First approach

#### DISTANCE

- For a given set of coordinates  $X = \{\bar{z}, \bar{A}, \bar{R}\}$ where  $\bar{z}$  is the location,  $\bar{A}$  is a vector indicating the corresponding aquifer, and  $\bar{R}$  indicates the rock types present.
- We define the distance

$$d_X = \sqrt{(1 - \alpha - \beta)d_z^2 + \alpha d_A^2 + \beta d_R^2}.$$

so the covariance of our model is

$$\Sigma_{ij} = \sigma^2 \exp\left(\frac{-d_{Xij}^2}{\tau}\right)$$

## First approach $X = \{E, N, A_1, A_2, A_3, A_4, R\}$





## What we tried

#### NEXT STEP

- Prediction and performance
- Estimate all parameters (α, β, scale and variance)
  e.g. using MCMC
- See if the fun covariance matrix works better

## First approach

SPECIAL CASE: DECOUPLED AQUIFERS

- Infinite distance between boreholes in different aquifers  $\rightarrow$  zero correlation
- Block diagonal matrix
- Geodistance contribution within aquifers based in rock types

#### DIFFUSION MODEL



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#### TIME DEPENDENT CORRELATION







TIME DEPENDENT CORRELATION

- Correlation in  $\Delta t$  if
  - direct correlation in  $\Delta t$
  - difference of path to most recent common ancestor is  $\Delta t$
- Amount of correlation
  - transported mass
  - decay in time/distance
  - path physical properties



#### Bath, Bath and North East Somerset at scale 1:300,000

Other maps 🕑 Data search 🕑 Text only version 🕑