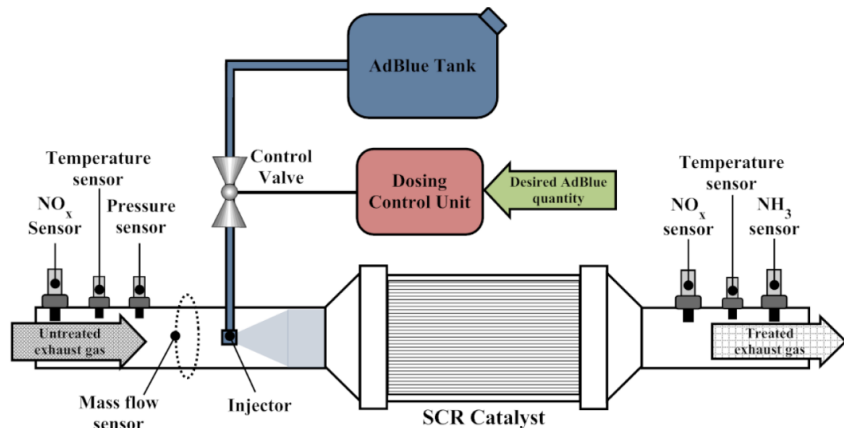


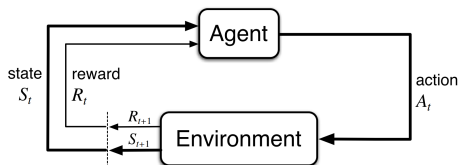
# Selective Catalytic Reduction with Reinforcement Learning

June 12, 2019

# The Current Process



# Reinforcement Learning



**Figure:** The agent-environment interaction in a Markov decision process [Sutton, R.S., Barto, A.G. *Reinforcement Learning: An Introduction* (1998)]

# Reinforcement Learning

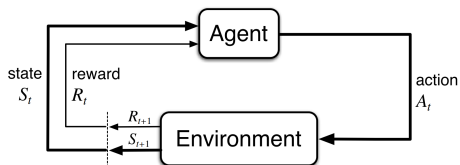


Figure: The agent-environment interaction in a Markov decision process [Sutton, R.S., Barto, A.G. *Reinforcement Learning: An Introduction* (1998)]

## Value & Q-Value Function

$$V^\pi(S) = \mathbb{E}_\pi \left[ \sum_{i=0}^T \gamma^i R_{t+i} \mid S = S_t \right]$$

$$Q(S_t, A_t) = R_t(S_t, A_t) + \gamma \max_{A_{t+1}} Q(S_{t+1}, A_{t+1})$$

# Reinforcement Learning

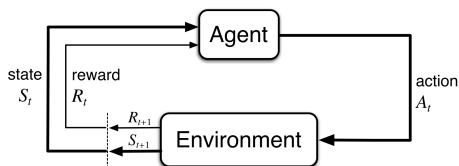


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# Reinforcement Learning

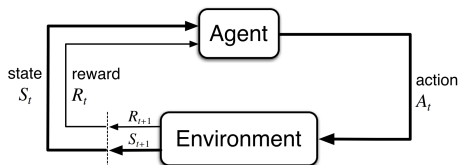


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# Reinforcement Learning

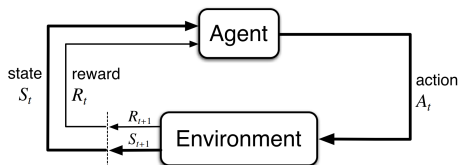


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Simplistic Reward Scheme:

$$R_t = \sum_{j=t}^{T+t} -\text{AdBlue}_j - c_1(\text{NH}_3)_j - c_2(\text{NO}_x)_j \quad \text{or} \quad R_t = \dots?$$

# Simpler Toy Problem

$$\frac{d}{dt}c_{NO,k} = \frac{n}{V_c \cdot \varepsilon_g} \cdot \frac{\dot{m}_{EG} \cdot R}{p_{EG} \cdot M_{EG}} (T_{EG,k-1} \cdot c_{NO,k-1} - T_{c,k} \cdot c_{NO,k}) + a_R (-4 \cdot r_{std,k} - 2 \cdot r_{fst,k} - r_{NO,g,k})$$

$$\frac{d}{dt}c_{NO_2,k} = \frac{n}{V_c \cdot \varepsilon_g} \cdot \frac{\dot{m}_{EG} \cdot R}{p_{EG} \cdot M_{EG}} (T_{EG,k-1} \cdot c_{NO_2,k-1} - T_{c,k} \cdot c_{NO_2,k}) + a_R (-2 \cdot r_{fst,k} - 6 \cdot r_{stw,k} + r_{NO,g,k})$$

$$\frac{d}{dt}c_{NH_3,k} = \frac{n}{V_c \cdot \varepsilon_g} \cdot \frac{\dot{m}_{EG} \cdot R}{p_{EG} \cdot M_{EG}} (T_{EG,k-1} \cdot c_{NH_3,k-1} - T_{c,k} \cdot c_{NH_3,k}) + a_R (-r_{ad,k} + r_{de,k} - 4 \cdot r_{ox,g,k})$$

⇒ ?

$$\frac{d}{dt}c_{CO_2,k} = \frac{n}{V_c \cdot \varepsilon_g} \cdot \frac{\dot{m}_{EG} \cdot R}{p_{EG} \cdot M_{EG}} (T_{EG,k-1} \cdot c_{CO_2,k-1} - T_{c,k} \cdot c_{CO_2,k}) + a_R (-0.5 \cdot r_{NO,g,k})$$

$$\frac{d}{dt}\theta_{NH_3,k} = \frac{1}{\Theta_{NH_3}} (r_{ad,k} - r_{de,k} - 4 \cdot r_{std,k} - 4 \cdot r_{fst,k} - 8 \cdot r_{stw,k} - 4 \cdot r_{ox,k})$$

$$\frac{d}{dt}T_{c,k} = \frac{n}{m_c \cdot c_{p,c}} \left( \dot{m}_{EG} \cdot c_{p,EG} \cdot (T_{EG,k-1} - T_{c,k}) + \alpha_c \cdot a_c \cdot (T_{Amb} - T_{c,k}) \right)$$