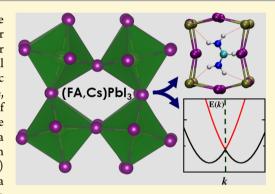


Mixed A-Cation Perovskites for Solar Cells: Atomic-Scale Insights Into Structural Distortion, Hydrogen Bonding, and Electronic **Properties**

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Supporting Information

ABSTRACT: Hybrid lead halide perovskites containing a mixture of A-site cations such as the formamidinium (CH(NH2)2, FA) and the smaller cesium (Cs⁺) cations have attracted considerable interest due to their improved stability and solar cell performance. However, the structural changes at the atomic scale and modifications to the optoelectronic properties of these mixed cation perovskites are not fully understood. Here, we investigate the $FA_{1-x}Cs_xPbI_3$ ($x \le 0.25$) system using a combination of static and dynamic ab initio computational methods. We find that the incorporation of Cs+ cations into the parent FAPbI3 structure induces a chemical pressure or lattice strain effect through Cs/FA ion size mismatch resulting in structural distortion and stronger FA-iodide (N-H···I) hydrogen bonding interactions. The dynamic tilting of PbI₆ octahedra and the rotational motion of FA cations are also suppressed, which leads to



symmetry-breaking of the lattice. Such symmetry-breaking distortions of the Pb/I lattice give rise to a Rashba-type effect, which spin-splits the frontier electronic bands making the band gap indirect. Our results suggest that the direct-indirect band gap transition may be a factor in the reduced charge-carrier recombination rate in these mixed cation perovskites.

1. INTRODUCTION

Lead halide perovskite solar cells have shown a remarkable rise in power conversion efficiency from 3.8% to over 22% in less than a decade. 1-9 Along with their solution-processed fabrication, they possess many suitable properties for solar absorbers, including long charge-carrier lifetimes, a tunable band gap by cation or halide substitution, and compatibility with a wide range of charge collecting layers.

Despite their promising properties, a number of challenges need to be overcome before perovskite-based solar cell devices can be commercialized. Long-term stability at ambient conditions is one of the most important issues. $^{10-14}$ Compositional engineering has recently emerged as a potential approach to deliver higher stability without sacrificing power efficiency. 15-32

Lead halide perovskites typically have the composition APbX₃ with the A-site occupied by a monovalent organic or inorganic cation (e.g., methylammonium CH₃NH₃⁺ (MA⁺), formamidinium $CH(NH_2)_2^+$ (FA⁺), or cesium Cs^+) and the Xsite by a halide anion (I⁻, Br⁻, or Cl⁻). The PbX₃ component forms a framework cage of corner-sharing octahedra (shown in Figure 1) with the A-site cation (termed A-cation hereafter) at the center of each cage. Among compositional engineering approaches, the mixing of different sized A-cations has shown promise in producing longer lived solar cells. 17-22,24-28,33 In particular, partial substitution (of up to 25%) of FA cations by

the much smaller Cs cations in FAPbI₃ stabilizes the perovskite phase against phase transitions and chemical degradation. ^{18,20,21,28,33,34} These mixed FA/Cs perovskites also exhibit improved optoelectronic properties, such as a tuned band gap,¹⁸ enhanced charge-carrier mobility²⁰ and recombination lifetime,²⁰ and reduced energetic disordering.¹⁸ As the static and dynamical structures influence these properties, it has been suggested that A-cation mixing modifies the internal interactions between the octahedral inorganic framework and organic cations. Despite a number of experimental reports and intriguing proposals, an in-depth atomistic understanding of these improvements is currently unclear.

We have carried out a range of recent studies on hybrid halide perovskites including work on ion transport, degradation, and defect passivation. 14,35-42 Here, we extend our previous work by investigating the structural distortions and interatomic interactions between the organic cations and inorganic framework of $FA_{1-x}Cs_xPbI_3$ ($x \le 0.25$). Insights into the atomic-scale dynamical processes of the PbI framework and the organic cations are also provided by ab initio molecular dynamics simulations. The impact of A-cation mixing on the photovoltaic behavior and possible Rashba-type effects has

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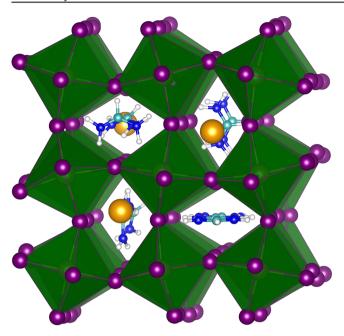


Figure 1. Schematic structure of a mixed A-cation metal halide perovskite. The A cations, FA⁺ and Cs⁺, occupy the inorganic cavity formed by corner-sharing PbI₆ octahedra (green). Key: iodine, purple; hydrogen, white; carbon, cyan; nitrogen, blue; cesium, orange.

been investigated by exploring electronic properties of these perovskites.

2. METHODS

Ab initio simulations were performed within the framework of density functional theory (DFT) as implemented in the Vienna Ab Initio Simulation Package (VASP)^{43,44} using the Perdew–Burke–Ernzerhof functional for solids (PBEsol) within the generalized gradient approximation (GGA). 45,46 The projected augmented wave (PAW)⁴⁷ method and a plane-wave cutoff energy of 500 eV were employed for all the calculations. To simulate the impact of Cs incorporation with experimental concentrations of up to 25%, sufficiently large 4 × 4 × 4 supercell (64 A-cations) of the parent FAPbI₂ was chosen. We stress the necessity of a large structural supercell to model the experimental compositions for mixed Acations. The extensive configuration space of cation distributions makes the ab initio computational investigations extremely challenging. Geometry relaxation was performed with k-point sampling at the Γ point, and the interatomic forces were relaxed with the convergence criteria of 0.01 eV Å⁻¹. A 3 × 3 × 3 Γ-centered Monkhorst-Pack sampling mesh with a Gaussian smearing of 0.01 eV was used for the electronic structure evaluation. To introduce a spin-orbit coupling (SOC) correction, geometry optimized 2 × 2 × 2 supercells of selective systems were considered. A 5 \times 5 \times 5 Γ -centered mesh was considered for the SOC-corrected electronic structure calculations.

To consider various possible conformations of FA^+ cations in $FAPbI_3$, the structural optimizations were initiated from up to 40 randomly generated geometries. We find that different orientations of the FA^+ cations result in small changes in total ground-state energy

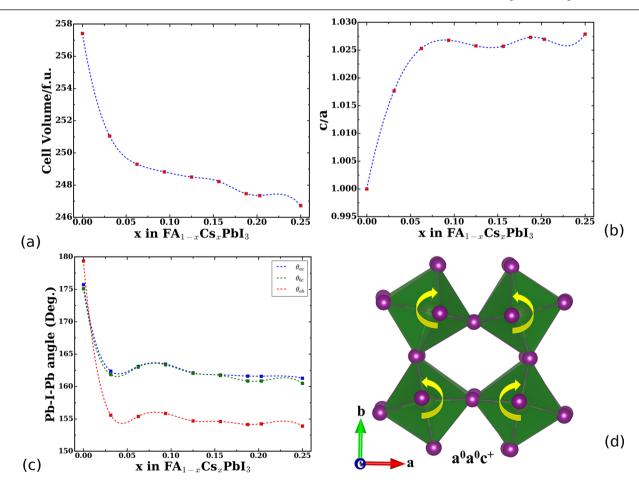


Figure 2. Structural distortion in $FA_{1-x}Cs_xPbI_3$. (a) Cell volume per formula unit, (b) c/a ratio, and (c) average Pb-I-Pb angle in three planes. (d) Tilting of PbI_6 octahedra with mutual in-phase rotation, i.e., $a^0a^0c^+$ in Glazer's notation for $FA_{0.85}Cs_{0.15}PbI_3$. Yellow arrows indicate the direction of rigid rotation of the octahedra.

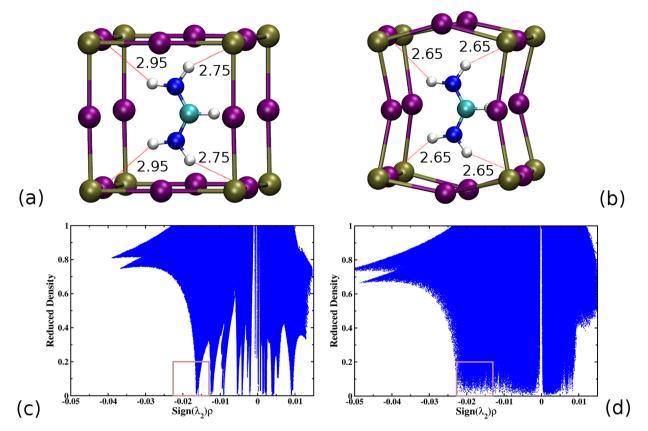


Figure 3. Enhanced hydrogen bonding with A-cation mixing. Schematic structures of H_N ···I hydrogen bonds (red dashed lines) in (a) FAPbI₃ and (b) FA_{0.85}Cs_{0.15}PbI₃ with average bond lengths in Angstrom (Å). Reduced density gradient (s) plot as a function of Sign(λ_2) ρ for (c) FAPbI₃ and (d) FA_{0.85}Cs_{0.15}PbI₃. The brown boxes denote the range $-0.022 < \rho < -0.012$ where the hydrogen bonding mediated troughs are markedly different between FAPbI₃ and FA_{0.85}Cs_{0.15}PbI₃.

and lattice parameters. By exploring the configurational space for the mixed A-cation system $FA_{0.85}Cs_{0.15}PbI_3$, the highly dispersed Cs cation arrangements produced the lowest energy geometries, and such a cation distribution has been considered in this study (see Supporting Information (SI) for further details).

To investigate finite temperature effects, we also performed *ab initio* molecular dynamics simulations at 300 K using the CP2K package. The QUICKSTEP formalism, an analytical dual-space pseudopotentials, the GGA of the PBEsol form, and dispersion corrections as prescribed by Grimme (DFT-D3) were used. Equilibrium dynamics were maintained in the NPT ensemble using a Nose-Hoover thermostat and a barostat as formulated by Martyna et al. With a time step of 1 fs, each simulation covered a period of 40 ps, with the equilibration spanning the first 5 ps.

3. RESULTS AND DISCUSSION

3.1. Structural Distortion of the Perovskite Lattice.

Simulations of the perovskite structures indicate that the lattice volume of $FA_{1-x}Cs_xPbI_3~(x\leq0.25)$ reduces with increasing Cs^+ content (Figure 2a), which is in agreement with X-ray diffraction studies. 21,33 The reduction of the unit cell volume in these mixed A-cation perovskites indicates chemical pressure effects, which relate to the internal structural contraction induced by the ion size mismatch between FA^+ (2.53 Å) and much smaller Cs^+ (1.67 Å). 53 Because of the soft mechanical nature of hybrid perovskites (with a bulk modulus <18 $GPa^{54,55}$), such effects can be tuned by mixing the large and small sized A-cations in controlled proportions. These structural perturbations are expected to have prominent effects on their phase transitions, 56 solubility of ions in solid solutions, 18 and optoelectronic properties. 54

By substituting small sized Cs^+ cations in place of FA^+ , the parent cubic lattice contracts anisotropically and lowers the crystal symmetry to a tetragonal phase. The a and b lattice parameters contract, whereas the c lattice parameter elongates, increasing the c/a ratio by 2.8% (Figure 2b). This structural change leads to symmetry-reducing tetragonal distortion in the $FA_{1-x}Cs_xPbI_3$ lattice upon A-cation mixing.

The main source of the anisotropic volume contraction could be either the reduced internal volume of the PbI₆ octahedra with compressed Pb–I bonds and/or the octahedral tilting of corner-sharing PbI₆. To investigate both possibilities, we analyze (1) the average PbI₆ octahedral volume and the Pb–I bond distances, which indicate the distortion inside the octahedra, and (2) Pb–I–Pb angles, which represent the magnitude of the octahedral tilting. We find that the average PbI₆ volume and Pb–I bond lengths (Figure S3 a,b) remain unchanged upon A-cation mixing. Thus, A-cation mixing keeps the internal structure of PbI₆ octahedra unaltered. Interestingly, this contrasts with the tin-based system FA_{1-x}Cs_xSnI₃, where the Sn–I bond contracts with Cs⁺ incorporation. 33

Our results indicate that the average Pb-I-Pb angles decrease along with the lattice contraction of $FA_{1-x}Cs_xPbI_3$ (shown in Figure 2c). Specifically, with increasing Cs^+ concentration, the Pb-I-Pb bond angles are more strongly reduced in the ab-plane (θ_{ab}) than in the other planes (θ_{bc} and θ_{ac}), indicating rotation of PbI₆ octahedra about the c-axis. As shown in Figure 2d, adjacent PbI₆ octahedra tilt in the same direction, that is, "in-phase" about the c-axis.³³ Using Glazer

notation,⁵⁷ such one-tilt rotations of octahedra are denoted $a^0a^0c^+$.

Therefore, as a consequence of the FA/Cs ion size mismatch, the cell volume contracts by tilting the PbI₆ octahedra. In a similar manner, applying low hydrostatic pressure (<5 GPa) has also been found to induce similar octahedral tilting based distortions and phase transitions in other hybrid perovskites including MAPbI₃ and FAPbI₃. ^{58–60} Tilting of corner-sharing octahedra is a relatively low-energy process ^{58,59,61} in these hybrid lead perovskites, and consequently, it becomes the source of structural distortion under weak perturbations such as cation substitution and mild external pressure.

3.2. Effect of H-Bonding. Lattice distortions can also modify the hydrogen bonding interactions between FA⁺ cations and the PbI framework as discussed in our previous study. By analyzing the H_N ···I bonds in FAPbI₃, we find the shortest distances are 2.75 and 2.95 Å (see Figure 3a). In contrast, on incorporation of Cs, as in FA_{0.85}Cs_{0.15}PbI₃, all four H_N ···I hydrogen bonds become much stronger due to the structural distortions (Figure 3b). As shown in Figure 3b, all the H_N ···I distances are now ~2.65 Å, which are shorter than that in the parent FAPbI₃.

To evaluate the strength of hydrogen bonding in FA_{1-x}Cs_xPbI₃, we perform an analysis based on the noncovalent interactions (NCI) index formulated by Johnson et al. 62,63 This analysis uses the electron density and its spatial derivatives to identify the noncovalent bonds in materials including the hybrid perovskites.^{64,65} We analyze the reduced electron density gradient, s, as a function of Sign(λ_2) ρ , where ρ and λ_2 are the electron density and the second eigenvalue of the electron density Hessian (second derivative) matrix, respectively (Figure 3c,d).⁶³ From this analysis, the appearance of troughs and singularities in $s(\rho)$ indicate the presence of noncovalent interactions. The sign of λ_2 denotes the type of interaction: for λ_2 < 0, the interaction is attractive (such as hydrogen bonding), whereas in the case of $\lambda_2 > 0$ it is repulsive (steric crowding). The interaction strength is determined by the density ρ ; the higher the absolute value of ρ the stronger is the interaction.

As shown in Figure 3c,d, a greater number of troughs appear in the range $-0.022 < \rho < -0.012$ for $FA_{0.85}Cs_{0.15}PbI_3$ than for FAPbI₃. The troughs also move to a higher negative value of ρ in the mixed A-cation lattice (Figure 3c,d). As the highlighted range of ρ in Figure 3c,d indicates the degree of hydrogen bonding, ⁶³ these plots show a strengthening of this noncovalent bonding interaction in the mixed A-cation perovskite. Because of the structural distortion, H_N atoms of the FA cations become spatially constrained and closer to the iodide anions, enhancing the strength of H_N ···I hydrogen bonding interactions.

The stronger hydrogen bonding between molecular cations and the Pb/I lattice increases the internal energy of the perovskite phase. This is confirmed by the calculation of a favorable Helmholtz free energy of mixing for FA_{0.85}Cs_{0.15}PbI₃ of the order of 92 meV/formula unit at 300 K. In addition, we have examined the enthalply of decomposition of both FAPbI₃ and FA_{0.85}Cs_{0.15}PbI₃ to PbI₂, FAI, and CsI and derived an exothermic value of –20 meV/formula unit and endothermic value of 135 meV/formula unit, respectively. We also find much weaker hydrogen bonding in the nonperovskite hexagonal phase of FAPbI₃ due to long H_N···I distances, with no significant change in hexagonal FA_{1-x}Cs_xPbI₃. This, in

turn, correlates with the experimentally observed enhanced stability of the perovskite phase against the hexagonal phase for these mixed-cation halide perovskites ^{18,24,66} (see SI for details).

Hence, increased hydrogen bond strength helps to stabilize the structure and contributes to the greater thermal stability of the mixed A-cation perovskites. Similar phase stability induced by hydrogen bonding has also been observed for the low-temperature orthorhombic structure of MAPbI₃. ^{11,67–70} From computational work on MAPbI₃, Bristowe and Cheetham ⁶⁴ suggest that tuning the degree of hydrogen bonding can also be used as an additional control parameter to optimize perovskite solar cell properties.

3.3. Dynamics of Inorganic Framework and Molecular A-Cations. A-cation mixing also affects the dynamic interactions and motion of the inorganic Pb/I cage and the organic cations. ^{36,71} We therefore performed *ab initio* molecular dynamics simulations of the parent FAPbI₃ and mixed A-cation system FA_{0.85}Cs_{0.15}PbI₃ at 300 K. First, considering the inorganic framework, we plot two-dimensional (2D) volumetric maps of a representative PbI frame in the *ab*-plane (Figure 4a,b). The 2D volumetric map represents the

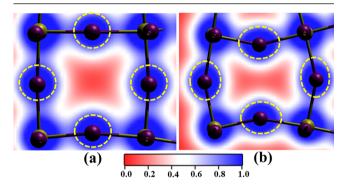


Figure 4. Dynamics of the inorganic framework in parent and mixed-cation perovskites. The volumetric plots of I and Pb atoms in a representative PbI-plane of (a) FAPbI $_3$ and (b) FA $_{0.88}$ Cs $_{0.15}$ PbI $_3$. This plot represents the number density of atoms in space over the simulation time. The scale is in arbitrary units, with blue and red indicating high and low number density, respectively. The ball—stick model of the inorganic framework shows the time-averaged positions of Pb and I atoms. The yellow dashed circles/ovals highlight the positions of iodine atoms over the simulation.

probability of atoms occupying positions in space over the time scale of the simulation. In Figure 4a, the iodine atoms of the parent FAPbI $_3$ show a symmetric distribution around the lattice sites, which are iodine lattice sites of the high-symmetry cubic structure. Thus, the time-averaged trajectories demonstrate an almost perfect cubic phase of FAPbI $_3$ (Figure 4a). In contrast, the 2D volumetric map for FA $_{0.85}$ Cs $_{0.15}$ PbI $_3$ (Figure 4b) shows significant spatial distribution of iodine atoms away from the cubic lattice sites. The time-averaged structure consequently clearly indicates the distorted low-symmetry lattice for FA $_{1-x}$ Cs $_x$ PbI $_3$.

At room temperature, the iodide anions in FAPbI₃ oscillate about equilibrium positions in a regular cubic lattice with maximum displacements inside and outside of a cage due to periodic rotation of the octahedra about the pseudocubic axis.³⁶ As reported in recent inelastic X-ray scattering experiments and DFT-based computations, the energy barrier for octahedral tilting is only a few meV in these mechanically

soft perovskites, and consequently, these oscillations are thermally active at room temperature. However, our work shows that in $FA_{0.85}Cs_{0.15}PbI_3$ the iodide ions become constrained and oscillate through a smaller angle, with respect to their equilibrium positions either outside or inside of a PbI cage, suppressing low-energy vibrational modes. This constraining of the lattice inhibits the periodic rotational motion of PbI₆ octahedra about the *c*-axis at 300 K, locking the octahedra across the whole structure in a tilted geometry. The suppressed octahedral tilting motion in $FA_{1-x}Cs_xPbI_3$ causes a static octahedral distortion, which has recently been identified by X-ray diffraction studies of Prasanna et al.³³

The molecular FA⁺ cations also change their dynamic behavior upon Cs⁺ incorporation. As illustrated in Figure 5a,

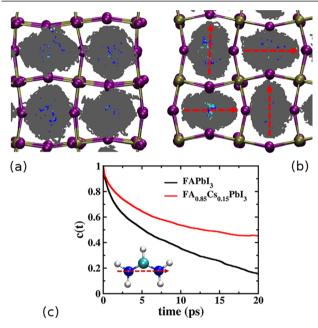


Figure 5. Dynamics of the FA $^+$ cation in parent and mixed-cation perovskites. The distribution of FA $^+$ cations in (a) FAPbI $_3$ and (b) FA $_{0.85}$ Cs $_{0.15}$ PbI $_3$ over the simulation time. The ball—stick model of the inorganic framework is the averaged position of Pb and I atoms over that time scale. Key: hydrogen, gray; carbon, cyan; nitrogen, blue. (c) Vector autocorrelation function of the FA $^+$ cation showing the probability of the cation remaining in its initial orientation over time. The molecular vectors of the FA $^+$ ion in b and the inset of c are represented by red dashed arrows.

the mobile FA cations in the parent FAPbI₃ explore full conformational space inside the inorganic cage showing no preferential orientation during the molecular dynamics simulation at 300 K. This disordered cation dynamics are in excellent agreement with quasi-elastic neutron scattering experiments, which also find a low barrier for reorientational motion inside the cage. 12,72 In contrast, for FA_{0.85}Cs_{0.15}PbI₃ the FA+ cations exhibit constrained reorientational dynamics in which the N-N molecular axis preferentially aligns along the high-symmetry directions, [100] and [010] (Figure 5b). Furthermore, neighboring FA cations in the ab-crystal plane remain mutually perpendicular, orienting themselves along the elongated direction of the distorted cages (Figure 5b and Figure S4). Thus, the ordering of FA⁺ cations is clearly influenced by the tetragonal distortion caused by the symmetry-lowering tilting of PbI₆ octahedra.

To further analyze the rotational motion of the FA⁺ cations, we focus on the reorientation of the N–N molecular axis of the CH(NH₂)⁺₂ cation (inset of Figure 5c) to capture the tumbling or "jump-like" rotation. To obtain a quantitative description of this motion, we evaluate the vector autocorrelation function c(t) of the N–N molecular axis from equilibrium trajectories. This function calculates the probability that the orientation of FA⁺ cations remains directionally self-correlated over time. The faster the rotational correlation is lost, the faster the c(t) decays with time.

As shown in Figure 5c, the autocorrelation function for tumbling rotation of FA⁺ cations in FAPbI₃ decays much faster than that of FA_{0.85}Cs_{0.15}PbI₃. Notably, due to cation—lattice interactions, the FA⁺ shows heterogeneous behavior in its dynamics in which the organic cation is inside the inorganic cage. We have therefore employed a stretched exponential fit to these autocorrelation functions to calculate the rotational relaxation time (see SI for details). We derive relaxation times for FA⁺ reorientation of 8.8 and 28.2 ps (with exponent values $\beta = 0.64$ and 0.48) in FAPbI₃ and FA_{0.85}Cs_{0.15}PbI₃, respectively. The significant difference in relaxation times clearly indicates the restricted rotational dynamics of FA⁺ cations at ambient conditions upon Cs⁺ incorporation. Our simulated rotational relaxation time for FA⁺ cations in FAPbI₃ matches well with a recent solid-state NMR study of Fabini et al.⁷⁴

In summary, the lattice contraction and tetragonal distortion of the inorganic framework causes the spatial confinement of FA $^+$ cations, reducing the molecular tumbling dynamics at 300 K. Such restrained dynamics further increases the probability of the $H_{\rm N}$ atoms of ${\rm CH(NH_2)_2^+}$ to reside closer to the electronegative iodide anions, enhancing the lattice–molecule interactions through stronger N–H···I hydrogen-bonding. Since these effects reinforce each other, the reorientational modes of cation dynamics become restricted, causing partial immobilization of FA cations along [100] or [010] crystal axes at room temperature. Recently, the suppression of cation dynamics and formation of an orientational glassy phase have been observed by neutron scattering studies of ${\rm MA_{1-x}Cs_xPbBr_3}$ perovskites. 71

3.4. Effect on Electronic Properties. We now consider the electronic properties of FA_{1-r}Cs_rPbI₃ in relation to its photovoltaic behavior. As shown in Figure 6a, the band gap exhibits a blue-shift with increased Cs content from 1.52 eV (x= 0.06) to 1.59 eV (x = 0.25). Inclusion of spin-orbital coupling in the simulations strongly underestimates the band gap of FA_{1-x}Cs_xPbI₃ (Table S1), although the trend of variation with Cs concentration remains unchanged. This variation and increase in band gap values are in agreement with recent experimental absorption studies. 18,21,33 We note that due to the use of the semilocal exchange-correlation functional (PBEsol) the absolute band gap values have not been captured fully. The requirement for large simulation cell sizes prohibits us from applying a quasi-particle self-consistent GW approach with spin-orbit coupling corrections.⁷⁵ Nevertheless, as demonstrated in earlier studies, 76,77 we can still analyze the key trends in electronic properties and the impact of A-cation composition.

Along with the band gap, the relative energies and chemical bonding character of the band edges directly affect charge separation, influencing their efficiency as perovskite solar cell devices. Applying the band-alignment scheme (see SI for details), the valence band maxima (VBM) downshift in energy

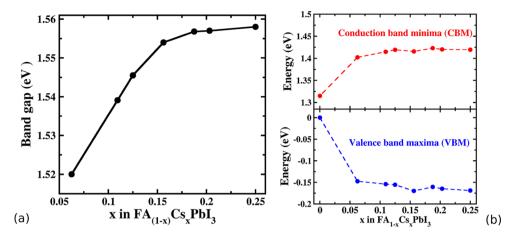


Figure 6. Electronic properties of $FA_{1-x}Cs_xPbI_3$ versus Cs concentration (x). (a) Variation in the band gap. (b) Variation in energy of conduction band minima (upper panel) and valence band maxima (lower panel). All energies are scaled to the VBM of FAPbI₃.

by 170 meV with increased Cs concentration, as shown in Figure 6(b). At the same time, the conduction band minima (CBM) shift upward in energy by a smaller amount of 100 meV. Overall, this leads to a blue-shift in the band gap, which is consistent with experimental absorption studies.³³ Note that inclusion of spin—orbit coupling does not change the overall trend in shifts of the band edges. We recognize that models based on band alignment have approximations. Nevertheless, the change in the band edges can tune the band offset between perovskite and charge transport layers, which may facilitate charge-carrier separation and transfer.⁷⁹

To investigate the atomistic origin of the shift in energy level positions, we performed a detailed investigation of the chemical bonding nature of the CBM (Figure 7a,b) and VBM (Figure 7c,d). The charge density contours in Figure 7c,d show that the VBM originates from the antibonding overlap of Pb 6s and I 5p* orbitals, consistent with previous reports. Furthermore, the site-projected density of states (pDOS, see Figure S5) indicate the covalent bonding nature of the VBM, in which 6s orbitals of Pb and 5p orbitals of I contribute ~30–35% and ~65–70%, respectively.

For cubic FAPbI₃, where the Pb–I–Pb alignment is almost linear, the antibonding orbital overlap in the VBM state remains significant (Figure 7c). With A-cation mixing, the inphase PbI₆ octahedral tilting causes symmetry-lowering lattice distortion where the Pb–I–Pb bond angles deviate from 180° so that the I atoms are displaced out of the linear bonding geometry (see Figure 7d). This distortion reduces the energetically unfavorable antibonding overlap between Pb 6s and I 5p* orbitals, causing a decrease in the energy of the VBM of FA_{1–x}Cs_xPbI₃. Similar modification of the VBM across the structural phase transition of FA_{1–x}Cs_xPbI₃ has been reported from experimental spectroscopy studies.³³

In contrast to the VBM, the CBM is dominated by Pb 6p nonbonding orbital contributions as shown in Figure 7b,d (see pDOS Figure S5). The localized nature of the electronic charge density indicates predominantly ionic character. Despite the nonbonding character, as shown in Figure 6b (upper panel), the CBM energy level is also influenced by Acation mixing in these hybrid perovskites. The charge density contours of the CBM in FAPbI₃ and in the high Cs content system FA_{0.75}Cs_{0.25}PbI₃ (Figure 7a, b) show that A-cation mixing enhances the contribution of 5p-I orbitals to the conduction band, inducing partial covalent character. The

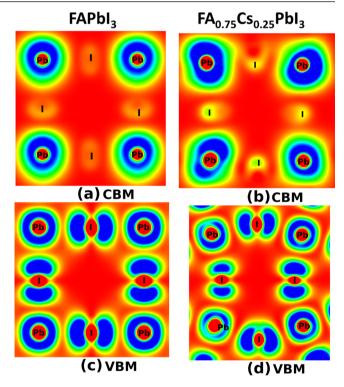


Figure 7. Electronic charge density contours. The conduction band minima (CBM) of (a) FAPbI₃ and (b) FA $_{0.75}$ Cs $_{0.25}$ PbI₃. The valence band maxima (VBM) of (c) FAPbI₃ and (d) FA $_{0.75}$ Cs $_{0.25}$ PbI₃. The CBM and VBM are dominated by the contributions from 6s orbitals of Pb and 5p orbitals of I. Color scale: red is defined as 0 and blue as 0.00015 eÅ $^{-3}$.

pDOS for the conduction band edge of $FA_{1-x}Cs_xPbI_3$ ($0 \le x \le 0.25$, Figure S6) also demonstrate the increased participation of 5p-I orbitals in this band with A-cation mixing. Such a variation in conduction band position with structural distortion is in line with previous computational studies on inorganic and hybrid lead halide perovskites. 64,76,77

Because of the pseudo-Jahn—Teller effect, the symmetry-lowering distortion in the inorganic framework of APbI $_3$ perovskites increases the covalency of the Pb—I bond. ⁸⁰ The increased covalent nature in the largely ionic CBM shifts the band to higher energy as shown in Figure 6b. Thus, A-cation mixing affects the VBM and CBM in opposing ways, leading to

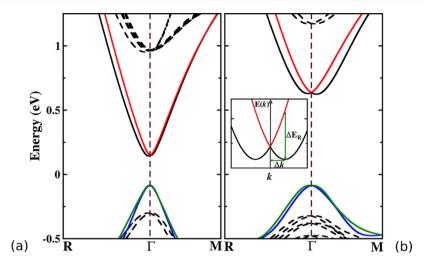


Figure 8. Rashba-type effect in mixed A-cation perovskites. The PBEsol-SOC electronic band structures of (a) FAPbI₃ and (b) FA_{0.75}Cs_{0.25}PbI₃. The Rashba-Dresselhaus splitting of the CBM in the $M \to \Gamma$ and $R \to \Gamma$ directions for FA_{0.75}Cs_{0.25}PbI₃ is prominent. Inset of b shows the zoomed section of the split conduction bands. The spin-split valence bands are shown in green and blue solid lines. The conduction bands are represented by black and red solid lines. All other bands are represented by dashed black lines.

an increase in the band gap. Recent X-ray and ultraviolet photoelectron spectroscopy experiments have also found a similar change in the energy levels in these mixed FA/Cs perovskites.³³

As noted in previous studies, single A-cation perovskites such as MAPbI₃ can exhibit a Rashba-type effect where the spin degeneracies of the conduction and valence bands are lifted, which can also lead to an indirect band gap. ^{81–85} We now consider the structural distortions from FA/Cs ion size mismatch on possibly activating a Rashba-type spin-splitting ^{86,87} of the CBM and VBM, resulting in substantial modifications of the band edges of FA_{1–x}Cs_xPbI₃. ^{77,88} It is known that in the presence of heavy nuclei with high spin-orbit coupling constants, the Rashba-type effect spin-splits the band edges of materials which lack the local or extended inversion symmetry in their structure. To examine this effect, we have calculated band structures for FAPbI₃ and FA_{0.75}Cs_{0.25}PbI₃ as shown in Figure 8.

Along both the M \rightarrow Γ and R \rightarrow Γ directions, the k-dependent spin-splitting of the conduction band shifts the band extrema from the high symmetry Γ -point for the mixed A-cation perovskite lattice. The momentum offset, Δk , is the difference between the Γ -point and shifted band-extrema in k-space. For $FA_{0.75}Cs_{0.25}PbI_3$, Δk in the M \rightarrow Γ and R \rightarrow Γ high symmetry directions are 0.025 and 0.018 Å⁻¹, respectively. Δk for such splitting in its valence band is much lower with a value of only 0.001 Å⁻¹ along both directions. The differing extents of Δk in the frontier bands create an indirect band gap for $FA_{0.75}Cs_{0.25}PbI_3$ (see Table S1).

Fundamentally, the Rashba-type splitting is directly related to the strength of the spin—orbit coupling of elements. Hence, the conduction band, which is dominated by contributions from heavy Pb atoms (Figure 7a,b), splits more than the valence band in which the lighter I atoms largely contribute (Figure 7c,d). For FAPbI₃, however, the extent of spin-splitting in the conduction band along $M \to \Gamma$ and $R \to \Gamma$ directions (Figure 8a) is significantly lower than that in $FA_{0.75}Cs_{0.25}PbI_3$ (Figure 8b); in these two directions, Δk values for the conduction band in FAPbI₃ are only 0.002 and 0.003 Å⁻¹, respectively. Thus, considering static structures, the presence of greater symmetry-breaking distortion in mixed A-cation

perovskites results in higher Rashba-type spin-splitting than that in $FAPbI_3$.

The strength of the Rashba-type effect can be represented by the parameter $\alpha = E_R/2\Delta k$, where E_R is the amplitude of the band splitting in a particular direction (see the inset of Figure 8c). In FA_{0.75}Cs_{0.25}PbI₃, the estimated α values in the M \rightarrow Γ and R \rightarrow Γ directions are 0.96 and 0.88 eV Å, respectively, which are of the same order as those reported by previous computational studies of related FA-iodide perovskites. ⁸⁹

Interestingly, several experimental reports based on time-correlated single-photon counting measurements have demonstrated an increased carrier lifetime for $FA_{1-x}Cs_xPb-(I_{0.6}Br_{0.4})_3$ ($x \le 0.25$). Better crystallinity and removal of nonperovskite phases by A-cation mixing have been argued as the primary causes for the improved photovoltaic properties. Our results suggest that changes in the static and dynamic interactions between the organic cation and inorganic Pb/I components in these mixed FA/Cs perovskites can also play an important role in the charge-carrier recombination.

As shown in Figure 8, structural distortions induce the Rashba-type spin-splitting of the band edges resulting in an indirect band gap in $FA_{0.75}Cs_{0.25}PbI_3. \ As a consequence of the$ indirect nature of the band gap in these distorted perovskites, photogenerated carriers occupy the band extrema with different k-points in reciprocal space. This, in turn, may reduce the possibility of radiative electron-hole recombination, which is otherwise active in direct band gap semiconductors. In the radiative limit, an indirect band gap can affect the recombination rate for materials with low chargecarrier mobilities and smaller absorption coefficients for indirect over direct optical transitions. 90 Because of other complex factors such as defect densities and transitions from defect states, assessing the exact influence of an indirect band gap on nonradiative recombination rates is not straightforward and requires further in-depth study.

We have shown that structural distortion from FA/Cs ion size mismatch makes these mixed A-cation structures less dynamic and induces static symmetry-breaking. Hence, we suggest that under certain conditions static Rashba-type spin splitting can be a significant factor for charge-carrier recombination processes in these mixed A-cation perovskites.

It should be noted that our finding of a static band-splitting mechanism is different from the recently demonstrated dynamical Rashba effect in MAPbI₃, which appears from dynamical local symmetry-breaking at finite temperatures. We recognize that other influences on recombination have been considered in the much-studied MAPbI₃ including carrier trapping, polaronic screening, and an inverse absorption process. Nevertheless, Rashba-type effects on the optoelectronic properties warrant further experimental studies as discussed by Stranks and Plochocka. Such effects have also rendered hybrid perovskites as promising materials for spintronic applications. 88,94

4. CONCLUSIONS

The changes in structural and optoelectronic properties of mixed A-site cation perovskite halides are not fully understood at the atomic scale. We have investigated the mixed cation system FA_{1-r}Cs_rPbI₃ using a combination of static and dynamic ab initio simulations with the following key features emerging: (a) Incorporation of Cs⁺ cations into the parent FAPbI₃ compound induces significant structural distortion through ion size mismatch between the formamidinium ion $(CH(NH_2)_2^+, FA^+)$ and the much smaller cesium ion (Cs^+) . This results in octahedral tilting and stronger N-H···I hydrogen bonding between the organic FA cation and iodide ions (within the inorganic cages), which help to stabilize the structure and promote greater thermal stability. (b) We find that the dynamic tilting of PbI₆ octahedra and rotational motion of FA-cations are significantly inhibited in the mixed cation structure, which leads to static symmetry-breaking of the lattice. (c) The band gap can be tuned by compositional cation substitution. The calculated band gap is found to widen with increasing Cs content in FA1-xCsxPbI3 as observed experimentally. The alignment of frontier energy levels are also altered by the structural distortions. The symmetry-breaking distortions of the Pb/I lattice give rise to a Rashba-type effect, which spin-splits the frontier electronic bands making the band gap indirect. Our results suggest that the direct to indirect band gap transition may be a factor in the reduced rate of charge-carrier recombination in mixed A-cation perovskites.

These findings warrant further investigation and, indeed, one of the aims of our work is to stimulate new experimental studies in this area.

ASSOCIATED CONTENT

S Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.chemmater.8b01851.

Detailed methods, phase stability, octahedral tilting, hydrogen bonding analysis, and reorientation relaxation time (PDF)

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Notes

The authors declare no competing financial interest.

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