ADAPTIVITY IN CLINICAL TRIAL DESIGNS:

OLD AND NEW

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Adaptivity

- emerges; e.g., scores in a linear rank test, logrank vs Gehan test Adaptive choice of test statistic as information on assumptions
- Adaptive allocation to achieve balance within strata

Adaptive allocation to assign fewer patients to an inferior treatment

- Adaptivity to accruing information on nuisance parameters
- Adaptivity to accruing information on safety/secondary endpoints
- Adaptivity to adjust power based on accruing information on primary endpoints
- Adaptivity to to drop arms in a multi-arm study based on accruing information on primary endpoints
- And more

Outline of Presentation

1. Interim monitoring of clinical trials

Adapting to observed data

- 2. Distribution theory, the role of "information"
- 3. Error-spending tests

Adapting to unpredictable information Adapting to nuisance parameters

4. Most efficient group sequential tests

Adapting optimally to observed data

- 5. More recent adaptive proposals
- 6. Example of inefficiency in an adaptive designs
- 7. Conclusions

1. Interim monitoring of clinical trials

ethics, administration (accrual, compliance) and economics It is standard practice to monitor progress of clinical trials for reasons of

Special methods are needed since multiple looks at accumulating data can lead to over-interpretation of interim results

clinical trials in the 1950s. Methods developed in manufacturing production were first transposed to

occasions whereas it is only practical to analyse a clinical trial on a small number of Traditional sequential methods assumed continuous monitoring of data,

the 1970s. The major step forward was the advent of *Group Sequential* methods in

Pocock's repeated significance test (1977)

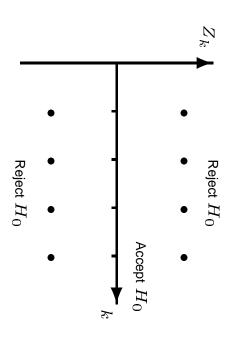
To test H_0 : heta=0 vs heta
eq 0, where heta represents the treatment difference

Use standardised test statistics Z_k , $k=1,\ldots,K$.

Stop to reject H_0 at analysis $\,k\,$ if $\,|Z_k|>c,$

if H_0 has not been rejected by analysis K, stop and accept $H_0.$

Choose c to give overall type I error rate = α .



Types of hypothesis testing problems

Two-sided test:

testing H_0 : $\theta = 0$ against $\theta \neq 0$.

One-sided test:

testing H_0 : $\theta \leq 0$ against $\theta > 0$.

Equivalence tests:

as treatment B, within a margin $\,\delta$ (non-inferiority). one-sided — to show treatment A is as good

are equal within an accepted tolerance two-sided — to show two treatment formulations

Types of early stopping

- 1. Stopping to reject H_0 : No treatment difference
- Allows rapid progress from a positive outcome
- Avoids exposing further patients to the inferior treatment
- Appropriate if no further checks are needed on safety or long-term effects.
- 2. Stopping to accept H_0 : No treatment difference
- Stopping "for futility" or "abandoning a lost cause"
- Saves time and effort when a study is unlikely to lead to a positive conclusion.

One-sided tests

To look for superiority of a new treatment, test

$$H_0$$
: $\theta \le 0$ against $\theta > 0$.

find out whether $\theta = 0$ or $\theta < 0$. If the new treatment if not effective, it is not appropriate to keep sampling to

Specify type I error rate and power

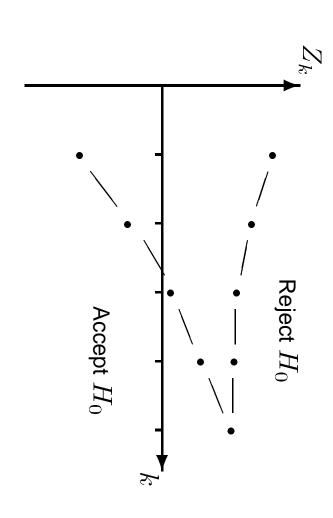
$$Pr\{ ext{Reject } H_0 \, | \, \theta = 0 \} = \alpha,$$

$$Pr\{ ext{Reject } H_0 \, | \, \theta = \delta \} = 1 - \beta.$$

and at effect sizes in between. A sequential test can reduce expected sample size under $\theta=0,~\theta=\delta,$

One-sided tests

A typical boundary one-sided testing boundary:



 $E({\sf Sample\ size})$ can be around 50 to 70% of the fixed sample size

adapting to data, stopping when a decision is possible.

2. Joint distribution of parameter estimates

Let θ_k be the estimate of the parameter of interest, θ , based on data at analysis k.

The information for $\,\theta\,$ at analysis $\,k\,$ is

$$\mathcal{I}_k \; = \; rac{1}{ ext{Var}(\widehat{ heta}_k)} \,, \quad k = 1, \dots, K.$$

Canonical joint distribution of $\ \widehat{ heta}_1,\dots,\widehat{ heta}_K$

normal, In very many situations, $\widehat{ heta}_1,\dots,\widehat{ heta}_K$ are approximately multivariate

$$\widehat{\theta}_k \sim N(\theta, \{\mathcal{I}_k\}^{-1}), \quad k = 1, \dots, K,$$

and

$$\operatorname{Cov}(\widehat{\theta}_{k_1},\widehat{\theta}_{k_2}) = \operatorname{Var}(\widehat{\theta}_{k_2}) = \{\mathcal{I}_{k_2}\}^{-1} \quad \text{for } k_1 < k_2.$$

Canonical joint distribution of z-statistics

In a test of H_0 : $\theta=0$, the standardised statistic at analysis k is

$$Z_k = \frac{\widehat{ heta}_k}{\sqrt{ ext{Var}(\widehat{ heta}_k)}} = \widehat{ heta}_k \sqrt{\mathcal{I}_k}.$$

For this,

 (Z_1,\ldots,Z_K) is multivariate normal,

$$Z_k \sim N(\theta \sqrt{I_k}, 1), \quad k = 1, \dots, K,$$

$$\operatorname{\mathsf{Cov}}(Z_{k_1}, Z_{k_2}) = \sqrt{\mathcal{I}_{k_1}/\mathcal{I}_{k_2}} \quad \text{for } k_1 < k_2.$$

Canonical joint distribution of score statistics

The score statistics $S_k=Z_k\sqrt{\mathcal{I}_k}$, are also multivariate normal with

$$S_k \sim N(\theta \mathcal{I}_k, \mathcal{I}_k), \quad k = 1, \dots, K.$$

The score statistics possess the "independent increments" property,

$$Cov(S_k - S_{k-1}, S_{k'} - S_{k'-1}) = 0$$
 for $k \neq k'$.

with drift heta observed at times $\mathcal{I}_1, \dots, \mathcal{I}_K$. It can be helpful to know the score statistics behave as Brownian motion

Sequential distribution theory

demonstrated directly for: The preceding results for the joint distribution of $\, heta_1,\dots, heta_K\,$ can be

 θ a single normal mean,

 $\theta = \mu_A - \mu_B$, the effect size in a comparison of two normal means.

The results also apply when $\, heta\,$ is a parameter in:

a general normal linear,

a general model fitted by maximum likelihood (large sample theory).

adjustment for covariates if required So, we have the theory to support general comparisons, including

Survival data

The canonical joint distributions also arise for:

parameter estimates in Cox's proportional hazards regression model

survival curves a sequence of log-rank statistics (score statistics) for comparing two

— and to z-statistics formed from these.

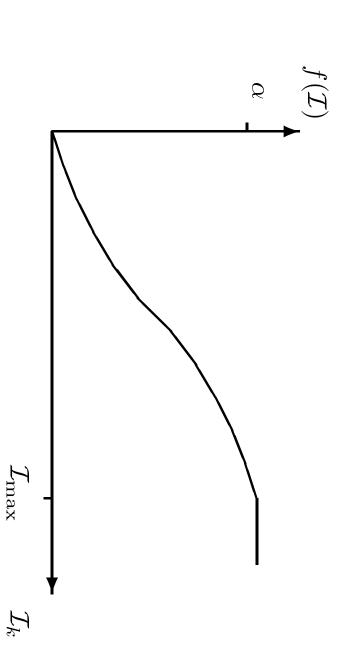
number of failures seen. For survival data, observed information is roughly proportional to the

and unevenly spaced information levels Special types of group sequential test are needed to handle unpredictable

3. Error spending tests

type I error probability as a function of observed information. Lan & DeMets (Biometrika, 1983) presented two-sided tests which "spend"

spent up to the current analysis The error spending function, $f(\mathcal{I})$, gives the type I error probability to be



Maximum information design

- Specify the error spending function $f(\mathcal{I})$
- cumulative type I error probability $f(\mathcal{I}_k)$. For each $\,k=1,2,\ldots$, set the boundary at analysis $\,k\,$ to give
- Accept H_0 if $\mathcal{I}_{ ext{max}}$ is reached without rejecting H_0 .

sequence over-runs the target $\mathcal{I}_{\mathrm{max}}$, or if the study ends without reaching reaching this target. See slides 20 and 21 or Chapter 7 of Jennison & Turnbull (2000). Precise rules are available to protect the type I error rate if the information

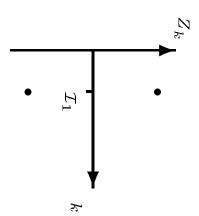
Implementing error spending tests

Analysis 1:

Observed information \mathcal{I}_1 .

Reject H_0 if $\left|Z_1\right|>c_1$ where

$$Pr_{\theta=0}\{|Z_1|>c_1\}=f(\mathcal{I}_1).$$

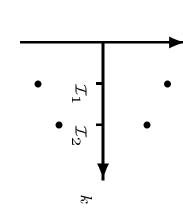


Analysis 2:

Cumulative information \mathcal{I}_2 .

Reject H_0 if $|Z_2|>c_2$ where

$$Pr_{\theta=0}\{|Z_1|< c_1, |Z_2|> c_2\}=f(\mathcal{I}_2)-f(\mathcal{I}_1).$$

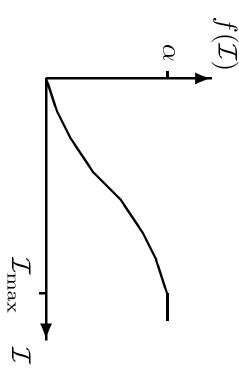


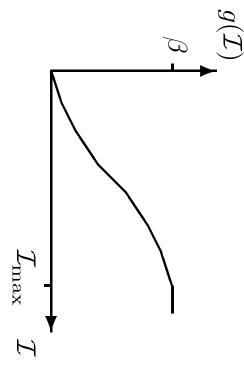
etc.

Adapting to unpredictable information

One-sided error spending tests

Define $f(\mathcal{I})$ and $g(\mathcal{I})$ for spending type I and type II error probabilities.





At analysis k, set boundary values $(a_k,\,b_k)$ so that

$$Pr_{ heta=0}\left\{ \mathsf{Reject}\ H_0 \ \mathsf{by} \ \mathsf{analysis}\ k
ight\} \ = \ f(\mathcal{I}_k),$$

$$Pr_{\theta=\delta}\left\{ \mathsf{Accept}\ H_0 \ \mathsf{by} \ \mathsf{analysis}\ k
ight\} \ = \ g(\mathcal{I}_k).$$

Power family of error spending tests: $f(\mathcal{I})$ and $g(\mathcal{I}) \propto (\mathcal{I}/\mathcal{I}_{\max})^{
ho}$.

Implementing one-sided error spending tests

- 1. Computation of (a_k, b_k) does **not** depend on future information levels, $\mathcal{I}_{k+1}, \mathcal{I}_{k+2}, \ldots$
- 2. A "maximum information design" continues until a boundary is crossed or an analysis with $\mathcal{I}_k \geq \mathcal{I}_{ ext{max}}$ is reached.
- 3. The value of $\mathcal{I}_{ ext{max}}$ is chosen so that boundaries converge at the final analysis under a typical sequence of information levels, e.g.,

$$\mathcal{I}_k = (k/K)\mathcal{I}_{\max}, \quad k = 1, \dots, K.$$

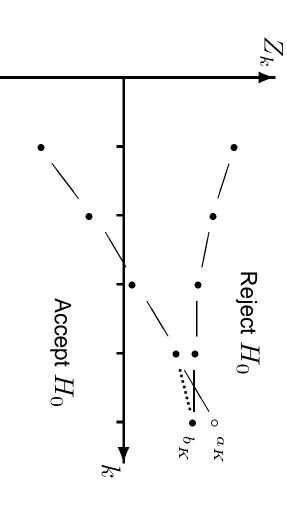
For type I error rate α and power $1-\beta$ at $\theta=\delta$,

$$\mathcal{I}_{\max} = R \frac{(z_{\alpha} + z_{\beta})^2}{\delta^2},$$

where R is the "inflation factor" for this design.

Over-running

If $\mathcal{I}_K > \mathcal{I}_{ ext{max}}$, solving for a_K and b_K is liable to give $a_K > b_K$.

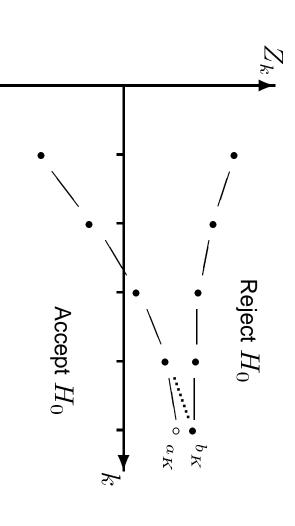


So, reduce a_K to b_K — and gain extra power. Keeping b_K as calculated guarantees type I error probability of exactly α .

deviate from the equally spaced values (say) used in choosing $\mathcal{I}_{max}.$ Over-running may also occur if $\mathcal{I}_K = \mathcal{I}_{ ext{max}}$ but the information levels

Under-running

 b_K is liable to give $a_K < b_K$. If a final information level $\mathcal{I}_K < \mathcal{I}_{\max}$ is imposed, solving for a_K and



Again, with b_K as calculated, the type I error probability is exactly lpha.

This time, increase a_K to b_K — attained power will be just below $1-\beta$.

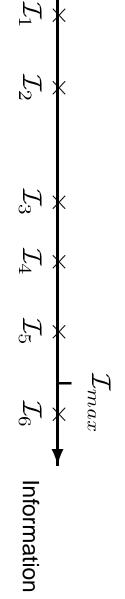
Error-spending designs and nuisance parameters

(1) Survival data, log-rank statistics

Information depends on the number of observed failures,

$$\mathcal{I}_k ~pprox ~rac{1}{4}$$
 {Number of failures by analysis k } .

With fixed dates for analyses, continue until information reaches \mathcal{I}_{\max} .



extend the patient accrual period. If the overall failure rate is low or censoring is high, one may decide to

they should **not** be influenced by the estimated treatment effect. Changes affecting $\{\mathcal{I}_1,\mathcal{I}_2,\dots\}$ can be based on observed information;

Error-spending designs and nuisance parameters

(2) Normal responses with unknown variance

and power $1-\beta$ at $\theta=\delta$ requires information In a two treatment comparison, a fixed sample test with type I error rate $\, lpha \,$

$$\mathcal{I}_f = \frac{(z_\alpha + z_\beta)^2}{\delta^2}$$

information $\mathcal{I}_{\max} = R \mathcal{I}_f$. A group sequential design with inflation factor $\,R\,$ needs maximum

to provide this level of information depends on the unknown variance σ^2 . The maximum required information is fixed — but the sample size needed

Adapting to nuisance parameters

Adjusting sample size as variance is estimated

The information from n_A observations on treatment A and n_B on B is

$$\mathcal{I} = \left\{ \left(\frac{1}{n_A} + \frac{1}{n_B} \right) \sigma^2 \right\}^{-1}.$$

equal to an initial estimate, σ_0^2 . Initially: Set maximum sample sizes to give information $\mathcal{I}_{ ext{max}}$ if σ^2 is

As updated estimates of σ^2 are obtained: Adjust future group sizes so the final analysis has

$$\left\{ \left(\frac{1}{n_A} + \frac{1}{n_B} \right) \hat{\sigma}^2 \right\}^{-1} = \mathcal{I}_{\text{max}}.$$

N.B., state \mathcal{I}_{max} in the protocol, not initial targets for n_A and n_B .

At interim analyses, apply the error spending boundary based on observed (estimated) information

4. Optimal group sequential tests

benchmark for judging efficiency of designs with other desirable features. "Optimal" designs may be used directly — or they can serve as a

Optimising a group sequential test:

Formulate the testing problem:

fix type I error rate α and power $1-\beta$ at $\theta=\delta$,

fix number of analyses, K,

fix maximum sample size (information), if desired.

one particular θ or averaged over several θ s. Find the design which minimises average sample size (information) at

Derivation of optimal group sequential tests

costs for a wrong decision. Write a program to solve this Bayes problem by Create a Bayes decision problem with a prior on θ , sampling costs and backwards induction (dynamic programming).

frequentist properties: type I error rate α and power $1-\beta$ at $\theta=\delta$. Search for a set of costs such that the Bayes test has the desired

optimisation problem — the key is that the unconstrained Bayes problem can be solved accurately and quickly. This is essentially a Lagrangian method for solving a constrained

Example of properties of optimal tests

equal group sizes, minimising $\{E_0(\mathcal{I})+E_\delta(\mathcal{I})\}/2$. One-sided tests, $\, \alpha = \beta = 0.05, \, K \,$ analyses, $\mathcal{I}_{max} = R \, \mathcal{I}_{fix}$,

Minimum values of $\{E_0(\mathcal{I})+E_\delta(\mathcal{I})\}/2$, as a percentage of \mathcal{I}_{fix}

20	10	Ŋ	N	K	
67.6	69.1	72.2	80.9	1.01	
60.5	62.1	65.2	74.5	1.05	
57.4	59.0	62.2	72.8	<u>-</u>	
54.6	56.3	59.8	73.2	R	
53.3	55.2	59.0	75.3	1.3	
52.0 at R =1.6	54.3 at R =1.6	58.7 at R =1.4	72.7 at R =1.15	$egin{aligned} extit{Minimum} \ ext{over} \ R \end{aligned}$	

Note: $E(\mathcal{I})\searrow$ as $K\nearrow$ but with diminishing returns,

 $E(\mathcal{I}) \searrow \text{ as } R \nearrow \text{ up to a point.}$

Assessing families of group sequential tests

One-sided tests:

Pampallona & Tsiatis

each Δ implies an "inflation factor" R such that $\mathcal{I}_{max} = R \, \mathcal{I}_{fix}.$ Parametric family indexed by Δ , boundaries for S_k involve \mathcal{I}_k^Δ ,

Error spending, ρ -family

Error spent is proportional to $\mathcal{I}_k^{\
ho},\
ho$ determines the inflation factor R.

Error spending, γ -family (Hwang et al, 1994)

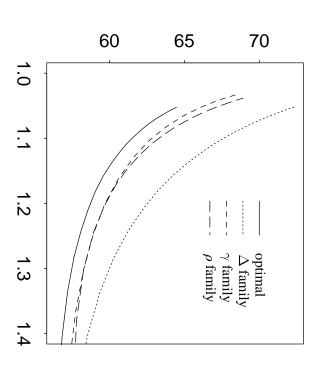
Error spent is proportional to

$$\frac{1 - e^{-\gamma \mathcal{I}_k/\mathcal{I}_{max}}}{1 - e^{-\gamma}}.$$

Families of tests

Tests with K=10, $\alpha=0.05$, $1-\beta=0.9$.

 $\{E_0(\mathcal{I})+E_\delta(\mathcal{I})\}/2~$ as a percentage of \mathcal{I}_{fix}



tests are sub-optimal. Both error spending families are highly efficient but Pampallona & Tsiatis

R

Adapting optimally to observed data

Squeezing a little extra efficiency

Schmitz (1993) proposed group sequential tests in which group sizes are chosen adaptively:

Initially, fix \mathcal{I}_1 ,

observe
$$S_1 \sim N(\theta \mathcal{I}_1, \mathcal{I}_1)$$
,

then choose \mathcal{I}_2 as a function of S_1 , observe S_2 where

$$S_2 - S_1 \sim N(\theta(\mathcal{I}_2 - \mathcal{I}_1), (\mathcal{I}_2 - \mathcal{I}_1)),$$

and so forth.

error rate and power. Specify sampling rule and stopping rule to achieve desired overall type I

and power $1-\beta=0.9$ at $\theta=\delta$. To test H_0 : $\theta=0$ versus H_1 : $\theta>0$ with type I error rate $\alpha=0.025$

Aim for low values of

$$\int E_{\theta}(N)f(\theta)\,d\theta,$$

where $f(\theta)$ is the density of a $N(\delta, \, \delta^2/4)$ distribution.

Constraints:

Maximum sample information =1.2 imes fixed sample information.

Maximum number of analyses = K.

Again, optimal designs can be found by solving related Bayes decision problems

Optimal average ${\cal E}({\cal I})$ as a percentage of the fixed sample information.

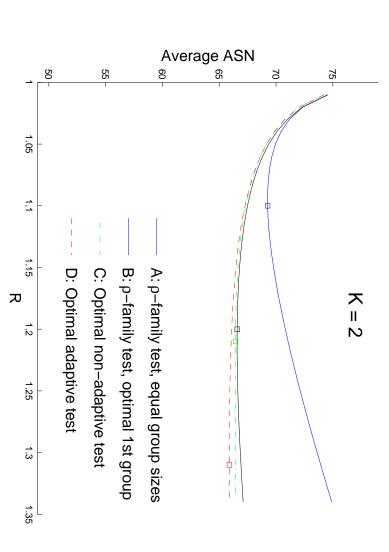
10	∞	o	4	ω	2		K		
55.9	56.6	58.0	61.2	64.8	72.5	(Schmitz)	design	adaptive	Optimal
57.2	58.0	59.4	62.4	65.6	73.2	group sizes	optimised	non-adaptive,	Optimal
57.5	58.3	59.8	62.7	66.1	74.8	sizes	equal group	non-adaptive,	Optimal

efficiency gains are slight. Varying group sizes adaptively makes for a complex procedure and the

Adapting super-optimally to observed data

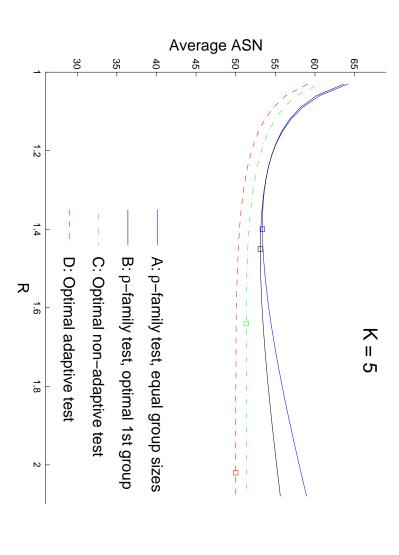
power $1-\beta=0.8$ at $\theta=\delta$, and K=2 analyses. Tests of H_0 : $\theta=0$ versus H_1 : $\theta>0$ with type I error rate $\alpha=0.025$,

Designs minimise average ASN $\{E_{\theta=0}(\mathcal{I})+E_{\theta=\delta}(\mathcal{I})+E_{\theta=2\delta}(\mathcal{I})\}/3$.



power $1-\beta=0.8$ at $\theta=\delta$, and K=5 analyses. Tests of H_0 : $\theta=0$ versus H_1 : $\theta>0$ with type I error rate $\alpha=0.025$,

Designs minimise average ASN $\{E_{\theta=0}(\mathcal{I})+E_{\theta=\delta}(\mathcal{I})+E_{\theta=2\delta}(\mathcal{I})\}/3$.



5. Recent adaptive methods

"Adaptivity" \neq "Flexibility"

- very much like "Schmitz" designs. Hunsberger (1995), Li et al. (2002), Hartung and Knapp (2003) are interim data is pre-determined: particular designs of Proschan and Pre-planned extensions. The way the design changes in response to
- stages: Bauer (1989), Bauer & Köhne (1994). Partially pre-planned. The time of the first interim analysis is pre-specified, as is the method for combining results from different
- any re-design: Fisher (1998), Cui et al. (1999), Denne (2001) or Müller different stages is implicit in the original design and carried over into Re-design may be unplanned. The method of combining results from & Schäfer (2001).

Bauer (1989) and Bauer & Köhne (1994) ...

... proposed mid-course design changes to one or more of

Treatment definition

Choice of primary response variable

Sample size:

in order to maintain power under an estimated nuisance parameter

to change power in response to external information

— to change power for internal reasons

a) secondary endpoint, e.g., safety

b) primary endpoint, i.e., $\hat{\theta}$.

Bauer & Köhne's two-stage scheme

Each part yields a one-sided P-value and these are combined. Investigators decide at the design stage to split the trial into two parts.

Run part 1 as planned. This gives

$$P_1 \sim U(0, 1)$$
 under H_0 .

- Make design changes.
- Run part 2 with these changes, giving

$$P_2 \, \sim \, U(0,\,1) \quad {
m under}\, H_0,$$

conditionally on $\,P_1\,$ and other part 1 information.

Combine P_1 and P_2 by Fisher's combination test:

$$-\log(P_1\,P_2)\,\sim\,rac{1}{2}\,\chi_4^2$$
 under $H_0.$

B & K: Major design changes before part 2

drug development process, such as: With major changes, the two parts are rather like separate studies in a

Phase IIb

Compare several doses and select the best.

Use a rapidly available endpoint (e.g., tumour response).

Phase III

Compare selected dose against control.

Use a long-term endpoint (e.g., survival).

the two stages with a pre-specified rule Applying Fisher's combination test for P_1 and P_2 gives a meta-analysis of

Note: Each stage has its own null hypothesis and the overall H_0 is **the**

intersection of these.

B & K: Minor design changes before stage 2

the original plan. With only minor changes, the form of responses in stage 2 stays close to

Bauer & Köhne's method provides a way to handle this.

Or, an error spending test could be used:

information levels, which can be handled in an error spending design. Slight departures from the original design will perturb the observed

spending test with a maximum information design. statistic can be embedded in a Brownian motion, one can use an error patients admitted before and after the change. As long as the overall score After a change of treatment definition, one can stratify with respect to

B & K: Nuisance parameters

Example. Normal response with unknown variance, σ^2 .

sample size depends on σ^2 . Aiming for type I error rate $\, lpha \,$ and power $\, 1 - eta \,$ at $\, heta = \delta \,$, the necessary

requirement assuming variance is equal to s_1^2 , the estimate from stage 1. One can choose the second stage's sample size to meet this power

 P_1 and P_2 from t-tests are independent $U(0,\ 1)$ under H_0 — exactly.

Other methods:

- (a) Many "internal pilot" designs are available.
- (b) Error spending designs can use estimated information (from s^2).
- (c) The two-stage design of Stein (1945) attains both type I error and power precisely!

External factors or internal, secondary information

Bauer and Köhne design

than $\theta = \delta$ ($\delta < \delta$). endpoint, investigators wish to achieve power $1-\beta$ at $\theta=\delta$ rather At an interim stage suppose, for reasons not concerning the primary

be increased, e.g., to give conditional power $1-\beta$ at $\theta=\delta$. If this happens after part 1 of a B & K design, the part 2 sample size can

If no re-design was planned

possible within a fixed sample study or a group sequential design by Recent work shows similar re-design, maintaining the type I error rate, is

preserving conditional type I error probability under $\theta=0$

see Denne (2001) or Müller & Schäfer (2001).

Responding to $\, heta_{ ext{,}}$ an estimate of the primary endpoint

Motivation may be:

- to rescue an under-powered study,
- a "wait and see" approach to choosing a study's power requirement,
- trying to be efficient.

power under $\theta = \theta$. Many methods have been proposed to do this, often by fixing conditional

available If re-design is unplanned, the conditional type I error rate approach is

It is good to be able to rescue a poorly designed study.

stopping on θ — and optimal GSTs do this optimally! But, group sequential tests already base the decision for early

The variance spending method

L. Fisher (1998), Cui et al. (1999), ...

normal method (Mosteller and Bush, 1954): For a study with two parts, combine $\,P_1\,$ and $\,P_2\,$ by the weighted inverse

$$Z_1 = \Phi^{-1}(1 - P_1),$$

$$Z_2 = \Phi^{-1}(1 - P_2),$$

combined in the overall statistic

$$Z = w_1 Z_1 + w_2 Z_2$$

where w_1 and w_2 are pre-specified with $w_1^2 + w_2^2 = 1$.

Then $Z\sim N(0,1)$ under $H_0.$

Variance spending method — normal observations

Suppose observations are independent, normally distributed

statistic if The overall statistic $Z=w_1Z_1+w_2Z_2$ is the usual efficient test

$$w_i \propto \sqrt{\mathsf{sample}\;\mathsf{size}\;\mathsf{in}\;\mathsf{stage}\;i}, \quad i=1$$

But, after flexible, adaptive re-design this is typically not the case.

In one standard scenario:

 $heta_1$ at stage 1 is smaller than hoped for,

second stage sample size is increased to enhance power under

$$\theta = \widehat{\theta}_1$$
,

stage counterparts hence, second stage observations receive lower weight than their first

6. Example of inefficiency in an adaptive design

Example. A Cui, Hung & Wang (1999) style example.

Scenario.

We wish to design a test with type I error probability lpha=0.025.

and worth detecting (cf the example cited by Cui et al). However, effect sizes as low as about $heta \geq \delta^{**} = 15$ are clinically relevant Investigators are optimistic the effect, $\, heta$, could be as high as $\,\delta^*=20.$

We suppose this requires a sample size $n_f = 100$. First, consider a fixed sample study attaining power 0.9 at $\, \theta = \delta^* = 20 \, . \,$

observations, but the data are examined after the first 50 responses to see if there is a need to "adapt". An adaptive design starts out as a fixed sample test with $\,n_f=100\,$

Cui et al. adaptive design

Denote the estimated effect based on the first 50 observations by $heta_1$.

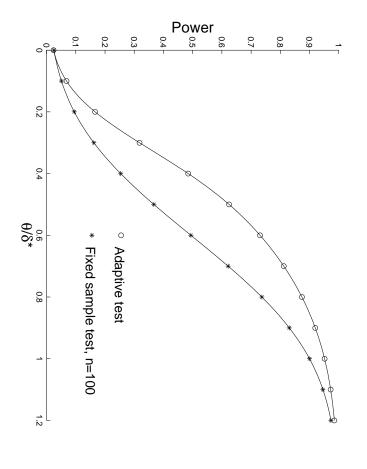
If $\widehat{ heta}_1 < 0.2\,\delta^* = 4$, stop the trial for futility, accepting H_0 .

type I error rate given $\, heta_1$ — thereby maintaining overall type I error rate $\,lpha_1$ Otherwise, re-design the remainder of the trial, preserving the conditional

 $\theta = \theta_1$. Choose the remaining sample size to give conditional power 0.9 if in fact

decrease in sample size is allowed and we keep the total sample size to at most 550 Then, truncate this additional sample size to the interval (50, 500), so no

Power of the Cui et al. adaptive test



achieving power 0.85 at $\, \theta = \delta^{**} = 15 \,$ (i.e., $\, \theta/\delta^* = 0.75$). The adaptive test improves on the power of the fixed sample test,

If continuing past the first stage, total sample size ranges from 100 to 550.

A conventional group sequential test

attain power 0.9 when $\theta=14$. Similar overall power can be obtained by a non-adaptive GST designed to

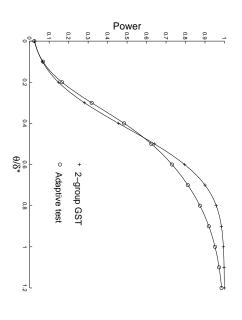
We have compared a power family, error spending test with $\,
ho=1$:

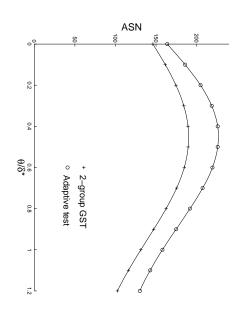
type I error rate is $\alpha = 0.025$,

after 225 gives a test meeting the requirement of power 0.9 at $\, heta=14.$ taking the first analysis after 68 observations and the second analysis

compared to 550. power and ASN. It also has a much lower maximum sample size — 225 This test dominates the Cui et al. adaptive design with respect to both

Cui et al. adaptive test vs non-adaptive GST





size. lower average sample size function, and a much smaller maximum sample The advantages of the conventional GST are clear. It has higher power, a

proposed in the literature. We have found similar inefficiency in many more of the adaptive designs

Conditional power and overall power

under way so overall power is irrelevant once data have been observed. It might be argued that only conditional power is important once a study is

However:

Overall power integrates over conditional properties in just the right way.

rule and sampling rule (even an adaptive one) are chosen It is overall power that is available at the design stage, when a stopping

given the variability of this estimate, the true effect size could well be zero. to very large sample sizes when the estimated effect size is low — and, As the example shows, "chasing conditional power" can be a trap leading

average sample size of each study. performance is determined by overall properties, i.e., the power and To a pharmaceutical company conducting many trials, long term

7. Conclusions

Error Spending tests using Information Monitoring can adapt to

- unpredictable information levels,
- nuisance parameters,
- observed data, i.e., efficient stopping rules.

to external developments or internal evidence from secondary endpoints. Methods preserving conditional type I error allow re-design in response

Recently proposed adaptive methods can

facilitate re-sizing for nuisance parameters,

support re-sizing to rescue an under-powered study,

allow an on-going approach to study design.

But, they will not improve on the efficiency of "standard" Group Sequential Tests — and they can be substantially inferior.

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