

VITERBI DECODING CONSIDERATIONS

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Viterbi/Trellis Decoders

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WE SAW THAT TO AVOID HAVING A LARGE PATH MEMORY (HOLDING THE TRELLIS INFORMATION) WE HAVE FIXED LENGTH HISTORY OF 4 OR 5 TIMES THE CONSTRAINT LENGTH.

THE AMOUNT OF PATH MEMORY REQUIRED IS

$$U = h 2^{K-1}; \quad h = 4K - \alpha K - SK$$

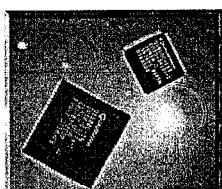
U - REQUIRED PATH MEMORY
h - LENGTH OF BIT PATH HISTORY PER STATE
K - CONSTRAINT LENGTH.

SINCE THE COMPLEXITY OF VITERBI DECODING IS DIRECTLY PROPORTIONAL TO THE NUMBER OF STATES IN THE TRELLIS, THE DECODER BECOME IMPRACTICAL FOR $K \geq 10$.

CHIPSETS FOR VITERBI DECODING ARE AVAILABLE FROM A NUMBER OF SEMICONDUCTOR MANUFACTURERS

- SEE FOLLOWING TWO PAGES

Q1900 Viterbi/Trellis Decoder



Forward Error Correction (FEC) improves the bit error rate (BER) performance of power-limited and/or bandwidth-limited channels by adding structured redundancy to the transmitted data. The type of additive noise experienced on the channel determines the class of FEC used on the channel. Tree codes are used for channels with Additive White Gaussian Noise (AWGN) and block codes are used for channels with additive burst noise. The Q1900 is based on a $k=7$ Viterbi decoder tree code, optimizing performance over channels with AWGN. The Q1900 supports encoding and decoding for Viterbi and Trellis Modes of operation. The Viterbi Mode is typically used for systems that are power-limited but not bandwidth-limited. The standard modulation types are Binary Phase Shift Keying (BPSK) and Quadrature Phase Shift Keying (QPSK). Trellis Mode is typically used for systems that are both power-limited and bandwidth-limited. The standard modulation types are 8-PSK and 16-PSK.

The encoders are both based on a $k=7$ convolutional encoder and the decoders are both based on a $k=7$ Viterbi decoder.

The Viterbi Mode supports four code rates: 1/3, 1/2, 3/4 and 7/8. Additional code rates can be supported with external circuitry. The Viterbi Mode also supports built-in phase synchronization for standard BPSK, QPSK, and Offset Quadrature Phase Shift Keying (OQPSK) modulation techniques. Either 1 bit hard-decision or 3 bit soft-decision input data is supported. The Viterbi Mode also includes two powerful built-in techniques for monitoring synchronization status as well as performing channel BER measurements.

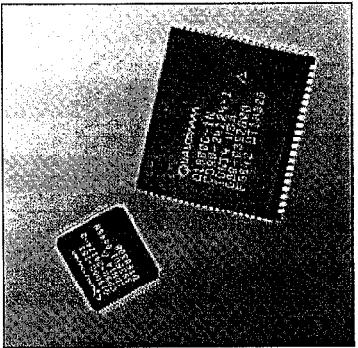
The Trellis Mode supports two code rates: 2/3 for 8-PSK and 3/4 for 16-PSK. The Trellis Mode also supports built-in phase synchronization for 8-PSK and 16-PSK. The Viterbi and Trellis Modes include a processor interface to facilitate control and status monitoring functions while keeping device pinout to a minimum.

The Q1900 is packaged in an 84-pin PLCC package or a 100-pin VTQFP package and is implemented in fully static CMOS logic to reduce power consumption. It also uses fully parallel circuit architecture to negate the requirement for a higher speed computation clock.

The Q1900 is well suited for many commercial satellite communication networks, including INMARSAT and INTELSAT. The low-cost and high performance of the Q1900 make it ideal for FEC requirements in systems such as direct broadcast satellites (DBS), microwave point-to-point data links, very small aperture terminals (VSAT), digital modems, digital video transmission systems, high-speed data modems and military and NASA communication systems.

Q1900

VITERBI/TRELLIS DECODER



RECEIVED
SEQUENCE:
11 0001 00
01 1100 11
10 0110 01
00 1101 10
11 0001 00
01 1100 11
10 0110 01
00 1101 10

FEATURES

- Viterbi Mode Rates $\frac{1}{2}$, $\frac{3}{4}$ and $\frac{7}{8}$
- Trellis Mode Rates $\frac{2}{3}$ and $\frac{5}{6}$
- Full Duplex Encode and Decode in Both Viterbi and Trellis Modes
- Large Coding Gains at E_b/N_0 of 10^5
 - 5.5 dB for Rate $\frac{1}{2}$ Viterbi Decoding
 - 5.2 dB for Rate $\frac{2}{3}$ Viterbi Decoding
 - 3.2 dB for Rate $\frac{2}{3}$ Trellis Decoding
 - 3.1 dB for Rate $\frac{3}{4}$ Trellis Decoding
- Automatic Phase Synchronization for BPSK and QPSK in Viterbi Mode and for 8-PSK and 16-PSK in Trellis Mode
- Data Rates up to 30 Mbps for Viterbi Mode and 90 Mbps (16-PSK) for Trellis Mode
- 3-Bit Soft Decision or 1-Bit Hard Decision Decoder Inputs for Viterbi Mode
- Viterbi Mode On-chip Channel Bit Error Rate (BER) Monitor
- Easy Implementation of Additional Code Rates
- Processor Interface Simplifies Control and Status
- Low-power CMOS Implementation
- Viterbi Mode Compatible with INTELSAT-308 and INTELSAT-309
- Standard 84-Pin PLCC or 100-Pin VQFP Package

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Forward Error Correction, Convolutional Coding, Data Book, 86-24128-1, A, 8658
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PERFORMANCE OF CONVOLUTION CODES

AN ERROR WILL OCCUR IN THE DECODING PROCESS WHEN THE SELECTED PATH DIFFERS FROM THE EXPECTED PATH.

LET'S LOOK AT OUR RATE $\frac{1}{2}$ K=3 CODE AGAIN. IF WE ASSUME THAT ALL PATHS ARE EQUALLY LIKELY, WE CAN LOOK AT THE CODE PERFORMANCE BY GENERATING A ZERO SEQUENCE AND THEN ADDING ERRORS

SUPPOSE M = 00000 ...

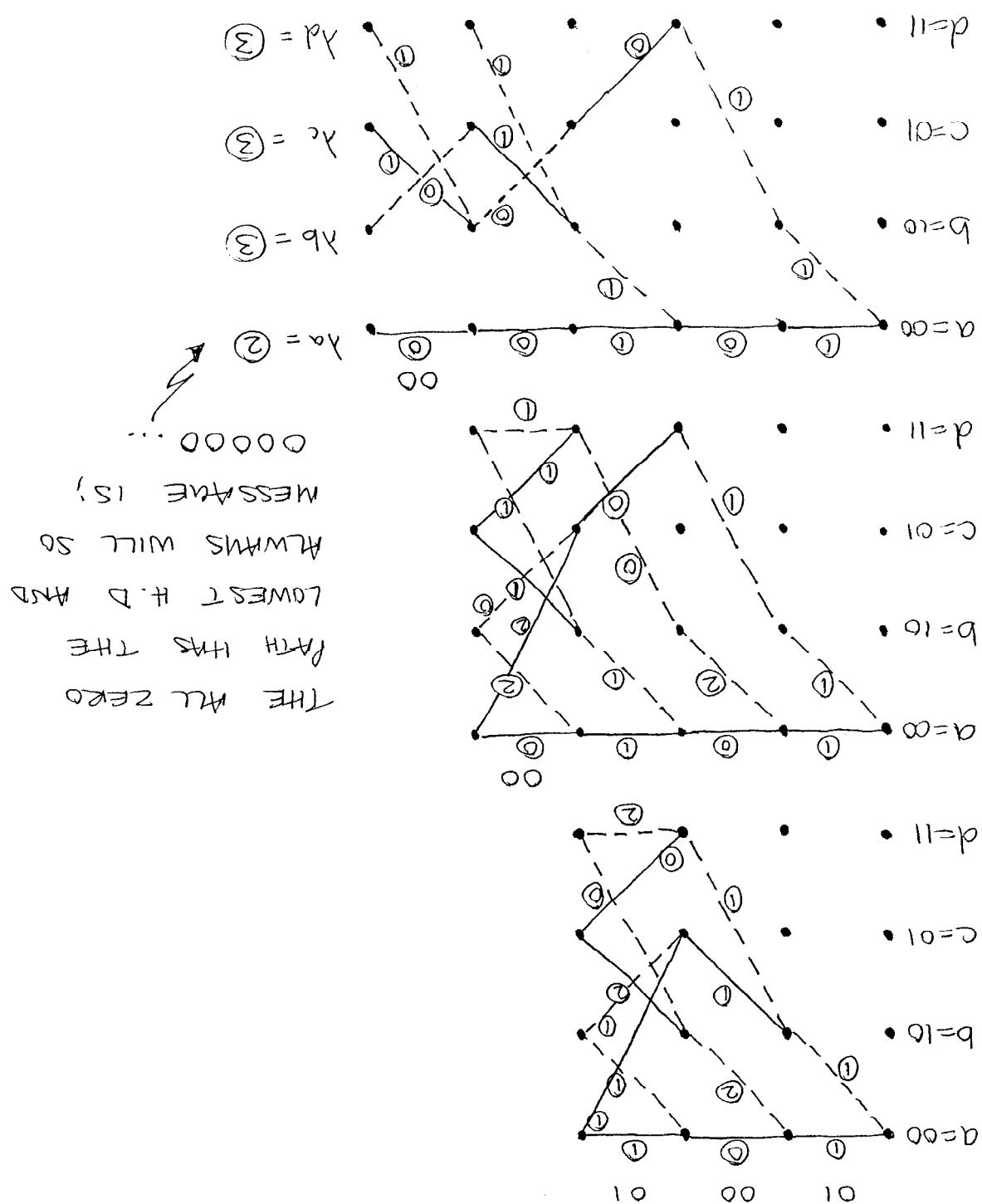
CASE 1: RECEIVED SEQUENCE : 01 00 01 00 ...
TWO ERRORS

CASE 2: RECEIVED SEQUENCE : 11 0001 00 ...
(SEE PAGES 5 AND 6) THREE ERRORS

CONCLUSION : A TRIPLE ERROR IS UNCORRECTABLE BY VITERBI DECODING WHEN APPLIED TO ONE RATE $\frac{1}{2}$ K=3 CONVOLUTION CODE

UNLESS THE TRIPLE ERROR IS SPREAD OUT OF A TIME SPAN GREATER THAN A CONSTRAINT LENGTH - IN WHICH CASE IT IS MOST LIKELY CORRECTABLE.

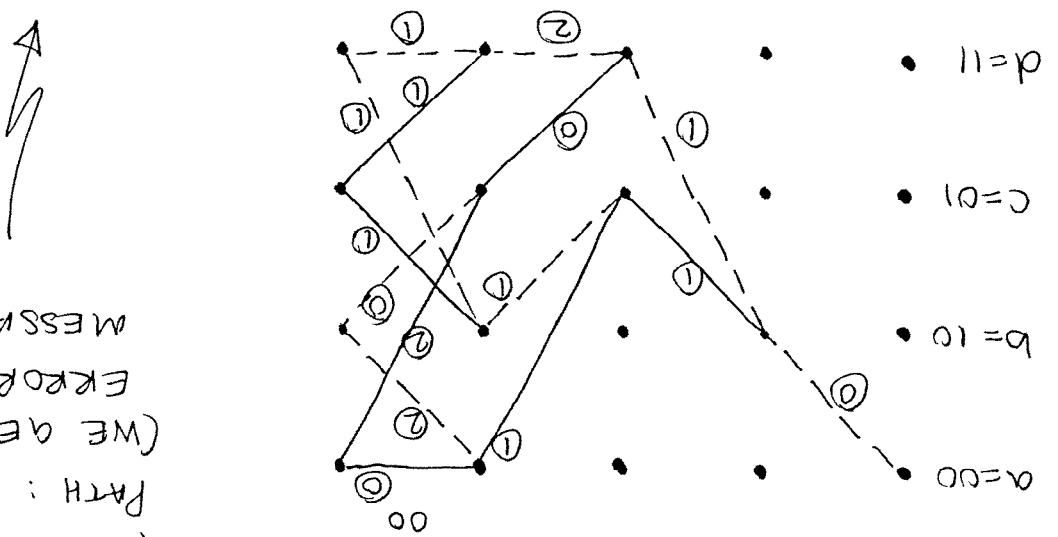
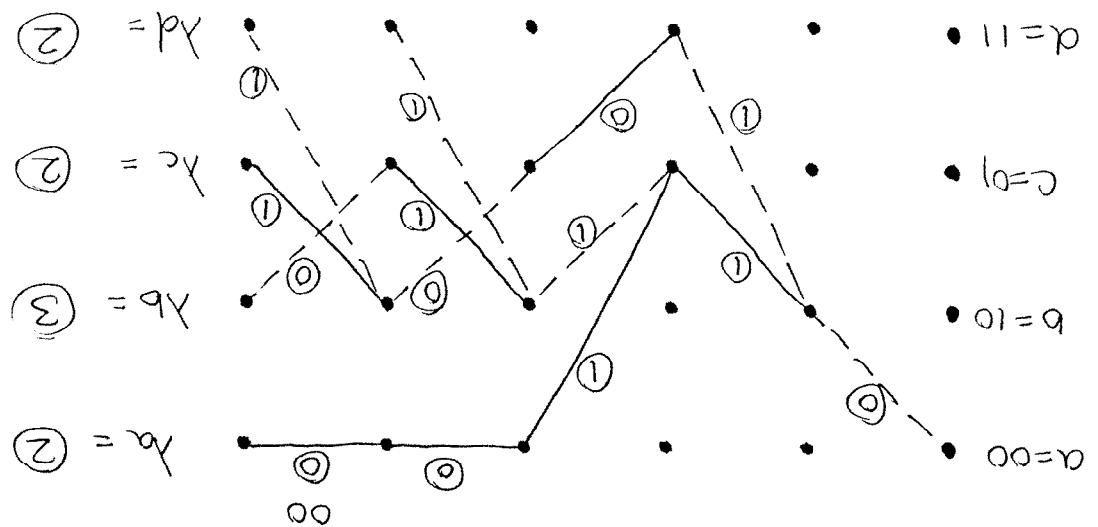
(4)



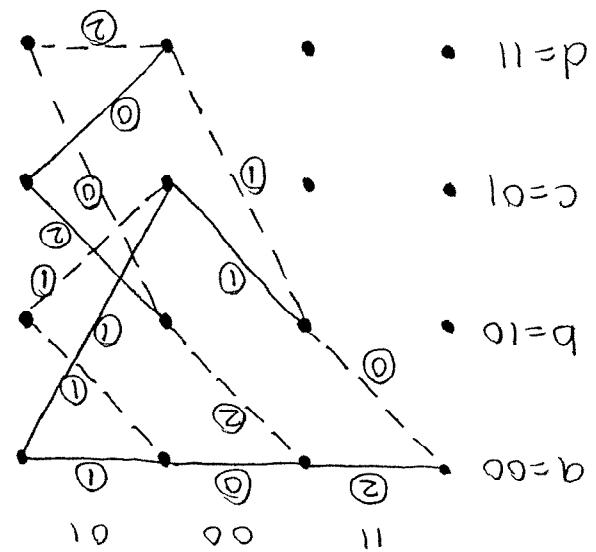
RECEIVED SEQUENCE: 01 00 01 00 ...

TWO ERRORS

(S)



IF WE CHOOSE α
 PATH : 10000 ...
 WE GET ONE
 ERROR IN THE
 MESSAGE)



RECEIVED SEQUENCE : 11 00 01 00 00

THESE ERRORS

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FREE DISTANCE

RECALL THAT WE SAID EARLIER THAT AN ERROR OCCURS WHEN THE SELECTED PATH DIFFERS FROM THE CORRECT ONE.

THE MOST IMPORTANT MEASURE OF A CONVOLUTIONAL CODE'S ABILITY TO CORRECT ERRORS IS THE FREE DISTANCE d_f

FROM THE FREE DISTANCE, THE ERROR CORRECTING CAPABILITY IS GIVEN BY:

$$t = \left\lfloor \frac{d_f - 1}{2} \right\rfloor$$

No correctable errors

d_f IS THE MINIMUM HAMMING DISTANCE BETWEEN ANY TWO CODEWORDS IN THE CODE, THAT BETWEEN ANY TWO PARTS IN THE TRELLIS.

WE CAN ESTIMATE THE FREE DISTANCE (SOMETIMES CALLED THE MINIMUM FREE DISTANCE) BY FINDING THE MINIMUM DISTANCE BETWEEN THE ALL-ZERO PATH (GENERATED FROM AN ALL-ZERO INPUT SEQUENCE) AND EACH OF THE OTHER CODEWORD SEQUENCES.
[SINCE THE CODE IS LINEAR, WE CAN DO]
[THIS WITHOUT LOSS OF GENERALITY]

(1)

HOW TO FIND d_f

* ASSUMING THAT THE ALL-ZEROS SEQUENCE WAS SENT, THE ONLY PATHS THAT MATTER ARE THOSE THAT START WITH STATE s_0 AND ENDS AT STATE s_f WITHOUT RETURNING TO STATE s_0 IN BETWEEN.

* AN ERROR WILL OCCUR WHENEVER THE DISTANCE OF ANY OTHER PATH THAT MERGES WITH STATE s_0 AT TIME t_i HAS A HAMMING DISTANCE LESS THAN THAT OF THE ALL-ZEROS PATH.

* GIVEN THE ALL-ZEROS TRANSMISSION, AN ERROR OCCURS WHEN THE ALL ZEROS PATH DOES NOT SURVIVE

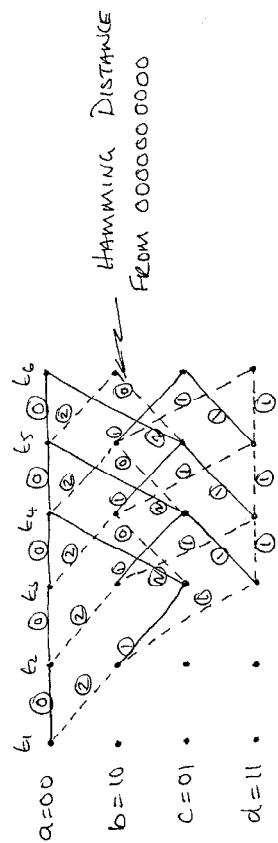
TO FIND d_f :

- DRAW THE DECODE TRELLOUS UNBELLING EACH BRANCH WITH THE HAMMING DISTANCE FROM THE ALL-ZERO PATH

- EXHAUSTIVELY SEARCH ALL PATHS FROM ALL ZEROS PATH AND BACK.
- THE MINIMUM HAMMING DISTANCE IS THE MIN FREE DISTANCE, d_f .

(2)

For example, consider our rate $\frac{1}{2}$, $K=3$ case (9)



PATH	Hamming Dist	# Errors (correctable)	R	K	df	Max Coding Gain (dB)
$\textcircled{a} \rightarrow \textcircled{b} \rightarrow \textcircled{c} \rightarrow \textcircled{a}$	5	2				
$\textcircled{a} \rightarrow \textcircled{b} \rightarrow \textcircled{b} \rightarrow \textcircled{c} \rightarrow \textcircled{a}$	6	2	$\frac{1}{2}$	3	5	3.98
$\textcircled{a} \rightarrow \textcircled{b} \rightarrow \textcircled{c} \rightarrow \textcircled{b} \rightarrow \textcircled{c} \rightarrow \textcircled{a}$	6	2	$\frac{1}{2}$	9	12	6.02
$\textcircled{a} \rightarrow \textcircled{b} \rightarrow \textcircled{c} \rightarrow \textcircled{b} \rightarrow \textcircled{c} \rightarrow \textcircled{b}$	7	3	$\frac{1}{3}$	3	8	7.78
$\textcircled{a} \rightarrow \textcircled{b} \rightarrow \textcircled{b} \rightarrow \textcircled{b} \rightarrow \textcircled{c} \rightarrow \textcircled{a}$	7	3	$\frac{1}{3}$	6	13	4.26
$\textcircled{a} \rightarrow \textcircled{b} \rightarrow \textcircled{b} \rightarrow \textcircled{b} \rightarrow \textcircled{b} \rightarrow \textcircled{a}$	8	4	$\frac{1}{3}$	9	18	6.37
HENCE $df = 5$						7.78

Conclusion: The larger df, the better the code performance. To increase df we need to increase K, and optimize the shift register connections. The exact design of convolutional codes is beyond the scope of this course - it can be found in books if you're interested.

(10)

CODING GAIN FOR A CONVOLUTIONAL CODE

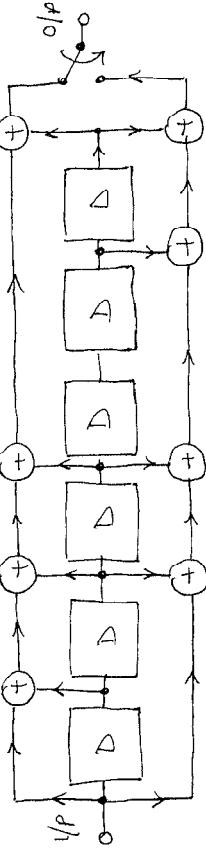
The coding gain increases with K, however it cannot increase indefinitely, the upper bound can be shown to be:

$$\text{Coding Gain (dB)} \leq 10 \log_{10}[R df]$$

where R is the code rate

PATH	Hamming Dist	# Errors (correctable)	R	K	df	Max Coding Gain (dB)
$\textcircled{a} \rightarrow \textcircled{b} \rightarrow \textcircled{c} \rightarrow \textcircled{a}$	5	2				
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$\textcircled{a} \rightarrow \textcircled{b} \rightarrow \textcircled{b} \rightarrow \textcircled{b} \rightarrow \textcircled{c} \rightarrow \textcircled{a}$	7	3	$\frac{1}{3}$	6	13	4.26
$\textcircled{a} \rightarrow \textcircled{b} \rightarrow \textcircled{b} \rightarrow \textcircled{b} \rightarrow \textcircled{b} \rightarrow \textcircled{a}$	8	4	$\frac{1}{3}$	9	18	6.37
HENCE $df = 5$						7.78

NASA STANDARD RATE $\frac{1}{2}$, $K=7$ CODER



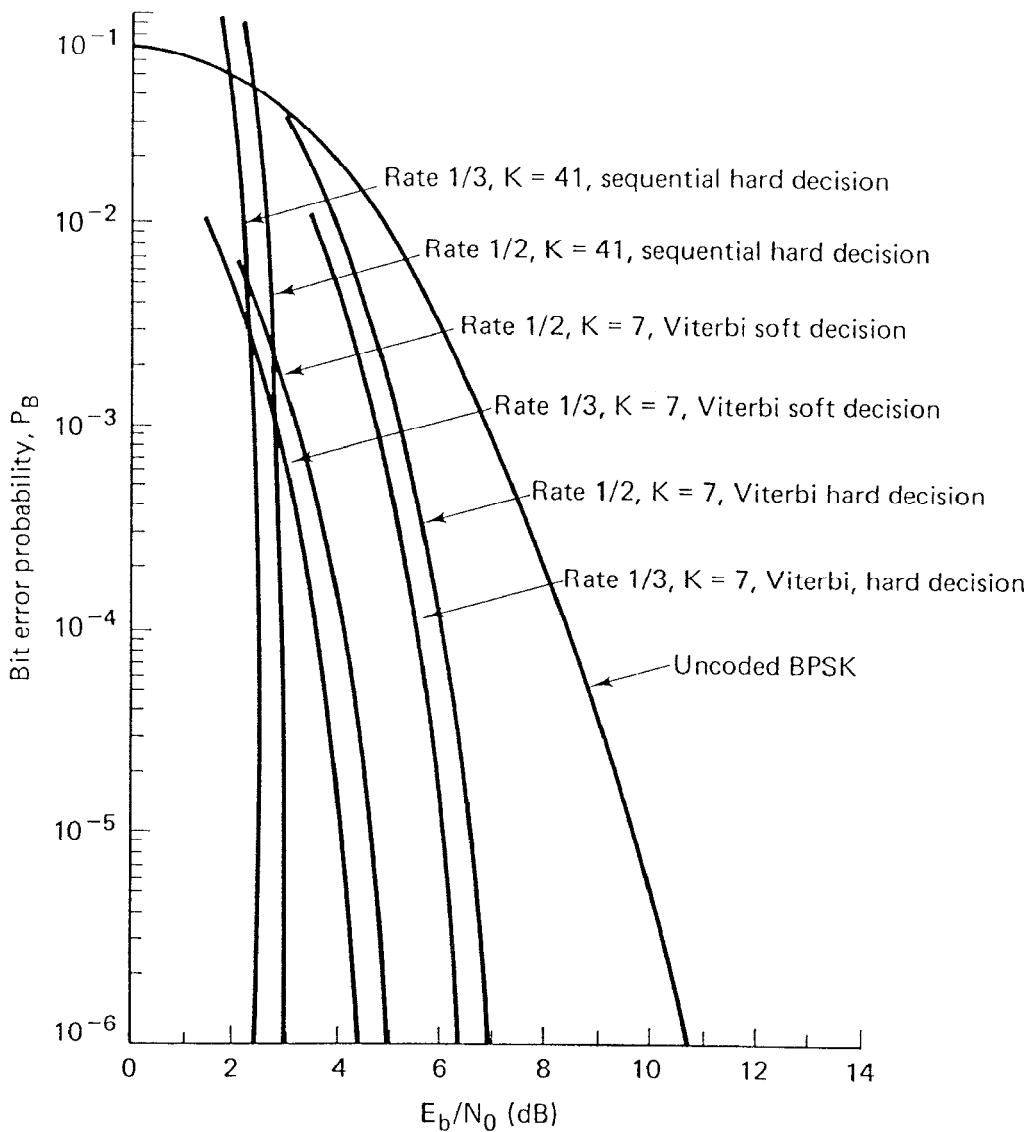
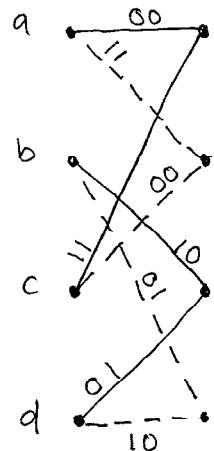


Figure 6.21 Bit error performance for various Viterbi and sequential decoding schemes using coherent BPSK over an AWGN channel. (Reprinted with permission from J. K. Omura and B. K. Levitt, "Coded Error Probability Evaluation for Antijam Communication Systems," *IEEE Trans. Commun.*, vol. COM30, no. 5, May 1982, Fig. 4, p. 900. © 1982 IEEE.)

TAKEN FROM SKLAR

	t_1	00	t_2	11	t_3	11	t_4	
$a = 00$	
$b = 10$	
$c = 01$	
$d = 11$	
			↓		01	t_5		
$a = 00$	
$b = 10$	
$c = 01$	
$d = 11$	
			↓					
$a = 00$		$\lambda_a =$
$b = 10$		$\lambda_b =$
$c = 01$		$\lambda_c =$
$d = 11$		$\lambda_d =$



MESSAGE SEQUENCE :