Surface Energies Control the Self-Organization of Oriented In$_2$O$_3$ Nanostructures on Cubic Zirconia

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ABSTRACT

Highly aligned one-dimensional (1D) nanorods of the transparent conducting oxide In$_2$O$_3$ have been grown on (110)-oriented Y-stabilized ZrO$_2$ substrates, whereas growth on (100) and (111) substrates leads respectively to blocklike 3D islands and continuous films. It is shown that the striking influence of substrate orientation on the growth morphology is controlled by differences in energies between the low index surfaces of In$_2$O$_3$ and that spontaneous self-organization is driven by minimization of surface energies.

KEYWORDS

Transparent conducting oxides, In$_2$O$_3$, self-organization, nanostructures

Transparent conducting oxides (TCOs) are key materials when it is necessary to combine optical transparency in the visible region with a high electrical conductivity. In$_2$O$_3$ doped with Sn (widely, but somewhat misleadingly, known as indium tin oxide or ITO) is one of the most important TCOs due to its intrinsically facile dopability, high conductivity, excellent transparency, and easy processability. Despite the fact that ITO finds widespread application in liquid crystal displays, solar cells and other optoelectronic devices, the basic physical properties of the material have been the subject of ongoing controversy. For example, it was only in 2008 that it was established that In$_2$O$_3$ has a direct, but dipole forbidden, bandgap of around 2.8 eV, almost 1 eV lower than the widely quoted value of 3.75 eV which marks the onset of fully allowed optical transitions. Revision of the value for the bandgap led in turn to the realization that electron accumulation may be observed on In$_2$O$_3$ surfaces with low bulk doping levels. The renewed interest in the bulk and surface physics of In$_2$O$_3$ has encouraged attempts to grow high quality single crystal thin films of In$_2$O$_3$ both for detailed fundamental investigations and for electronic device applications. There has also been an interest ongoing over many years in preparation of nanostructured In$_2$O$_3$ using solution techniques based on sol–gel or solvothermal processing, chemical vapor deposition, and electron beam evaporation. Nanostructured In$_2$O$_3$ has potential applications in gas sensing, field emission devices, and transparent electronics. A general limitation of the earlier approaches, however, is that they provide no control over the orientation of the structures formed. In the current work, we demonstrate that growth of In$_2$O$_3$ by high-temperature oxygen plasma-assisted molecular beam epitaxy (MBE) opens the possibility of rational design of highly oriented nanostructured films. Self-organization arising from lattice mismatch during heteroepitaxial growth provides a well-established approach to the preparation of “quantum dots” in conventional semiconductor systems such as Ge on Si and InAs on GaAs; the morphology of the dots is determined by an interplay between elastic strain and surface energies. Much less effort has been devoted to the controlled self-assembly of oxide nanostructures during epitaxial growth. Oxides and other polar materials are however of particular interest because in general there are very large differences between the energies of different low-index surfaces. This provides a means to control the aspect ratio and orientation of nanostructured material. Specifically, we explore the influence of substrate orientation in the epitaxial growth of In$_2$O$_3$ on Y-stabilized cubic ZrO$_2$ (YSZ).

In$_2$O$_3$ adopts a body-centered cubic bixbyite structure with space group $Ia\overline{3}$ and lattice parameter $a = 1.01170$ nm. The structure may be regarded as a $2 \times 2 \times 2$ superstructure of fluorite, with ordered removal of O from one-fourth of the anion sites. YSZ adopts a fluorite structure belonging to the space group $Fm\overline{3}m$ with lattice parameter $a = 0.51423$ nm at the 17% Y doping level of the substrates used in the current work. Thus, there is a mismatch of only 1.6% between $2a$ for Y-doped ZrO$_2$ (1.02846 nm) and $a$ for In$_2$O$_3$. Moreover, the

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cation arrays within the two materials are very similar, minimizing the chemical mismatch at the interface. We demonstrate the spontaneous formation of highly directional one-dimensional (1D) nanorods during high-temperature epitaxial growth of In$_2$O$_3$ on (110)-oriented Y-stabilized cubic ZrO$_2$ (YSZ). By contrast, growth on (100) surfaces leads to truncated square pyramidal islands. There is a growing consensus that (111)-oriented substrates are optimal for growth of high quality continuous thin films at relatively low temperature (T ≤ 700 °C).° We confirm here that atomically flat mesa or continuous thin films develop on (111)-oriented substrates even under high-temperature conditions. On the basis of ab initio quantum chemical simulations, it is shown that the different growth modes and the striking azimuthal orientation of the rods and pyramids on (110) and (100) surfaces are determined by large differences in the energies of the three low index surfaces.

**Experimental Section.** The In$_2$O$_3$ thin films were grown on (100)-, (110)-, and (111)-oriented 1 cm × 1 cm Y-stabilized ZrO$_2$ substrates in an ultrahigh vacuum oxide MBE system (SVT, U.S.A.) with a base pressure of 5 × 10$^{-10}$ mbar. This incorporated a hot lip indium Knudsen cell and a radio frequency (RF) plasma oxygen atom source operated at 200 mW RF power with an oxygen background pressure of 3 × 10$^{-5}$ mB. Substrates were heated radiatively using a graphite filament. The nominal growth rate was 0.035 nm s$^{-1}$, calibrated using the thickness from HRTEM measurements and AFM images. The Y-ZrO$_2$ substrates were cleaned by exposure to the oxygen atom beam at a nominal substrate temperature of 900 °C. We explored a wide range of growth conditions in terms of film thickness and growth temperature, which ranged between 550 and 1000 °C. Most of the data reported here relate to a deposition time of 3000 s that corresponds to a film thickness of 100 nm assuming a layer growth mode. In situ LEED was carried out in an analysis chamber connected to the growth chamber. AFM images were recorded ex situ with a Digital Instruments Multimode SPM instrument. This was operated in contact mode with a “J” scanner having a lateral range of approximately 100 µm and a vertical range of 6 µm. Silicon nitride probes (Nascatec GmbH model NST NCHFR) with a thin coating of gold to act as a mirror for the laser beam were used. Calibration of the AFM was accomplished by scanning a 10 mm pitch 200 nm 3D reference from Digital instruments. Digital Nanoscope software (version 5.1.2) was used to analyze and process the AFM topographic images. All the images were treated with the “flatten” command and are presented using one of the standard color palettes of the Nanoscope software. Specimens for cross-sectional TEM were prepared by cutting and mechanical grinding down to 5–10 µm, followed by thinning to electron transparency by Ar ion beam milling using a Gatan 691 Precision Ion Polishing System (PIPS). It proved very difficult to obtain sections with a uniform thickness across the ZrO$_2$/In$_2$O$_3$ interfaces because the epilayer etched at a much higher rate than the substrate. Cross-sectional TEM images were collected using a JEOL3000F microscope operating at 300 keV. Digital Micrograph image software was used to process the TEM images. Bragg filtering was applied to the TEM images to remove some of the background noise and contrast adjustment was applied uniformly across the images where necessary to enhance the display quality.

The bulk and surface electronic structure and total energies were calculated using density functional theory within the generalized gradient approximation (PBE) as implemented in the VASP package. The plane-wave kinetic energy threshold (500 eV) and k-point density (4 × 4 × 4) were both well-converged for the bulk system. Starting from the relaxed bulk bixbyite lattice (a = 1.030 nm), 2D surface models were constructed using a periodic arrangement of slabs, separated with a 2 nm vacuum region. Convergence of y with respect to slab thickness resulted in models containing 32, 32, and 48 formula units for the (100), (110), and (111) surfaces, respectively. In all cases, the top two ionic layers were allowed to relax, while all other layers were held at their bulk lattice positions. Simulated annealing was performed to assess the stability of the resulting structures at 750 K and no further relaxations or reconstructions were found to occur.

Figure 1 shows θ–2θ X-ray diffraction (XRD) profiles of In$_2$O$_3$ films with a nominal thickness of 100 nm grown on (a) (100)- and (b) (110)-oriented Y-stabilized cubic zirconia wafers. The insets show corresponding LEED patterns measured in situ in the MBE growth system.
films show no evidence of spot splitting.\textsuperscript{13} the 3-fold symmetric LEED patterns from (111)-oriented indicative of extensive faceting at the surface. By contrast splitting that varies strongly with beam energy. This is ever, the patterns show evidence of streaking and spot expected the patterns from (100) and (110) surfaces show oriented films measured in situ in the MBE system. As electron diffraction (LEED) patterns from the differently baseline noise. The insets in Figure 1 show low-energy

reflections with substrate (220) reflection. Within the space group \( l a \bar{5} (h k 0) \) \( h = k \) are systematically absent unless \( h = 2n \), so that the (110) and (330) epilayer peaks are not observed but the (220) peak is observable just above the baseline noise. The insets in Figure 1 show low-energy electron diffraction (LEED) patterns from the differently oriented films measured in situ in the MBE system. As expected the patterns from (100) and (110) surfaces show 4-fold and 2-fold rotational symmetries, respectively. However, the patterns show evidence of streaking and spot splitting that varies strongly with beam energy. This is indicative of extensive faceting at the surface. By contrast the 3-fold symmetric LEED patterns from (111)-oriented films show no evidence of spot splitting.\textsuperscript{13}

High-resolution transmission electron microscopy (HR-TEM) images such as those shown in Figure 2 confirm the excellent crystalline order in the films grown on the three differently oriented substrates and also demonstrate the formation in each case of sharp interfaces between the substrate and the epilayer. However, very pronounced morphological differences between films grown on the different low index substrates are apparent on a longer length scale. The differences are most obvious in large area atomic force microscopy (AFM) images, such as those shown in Figure 3. The (100)-oriented epilayer grown at 750 °C (Figure 3a) is seen to consist of an array of square or rectangular islands with lateral dimensions typically of the order of 100 nm and with edges all aligned parallel to the [011] directions of the substrate. Elongation of the islands takes place along both [011] and [011] directions. The (110) epilayer (Figure 3b) shows a similar island structure but in this case the islands are all rectangular and oriented with edges along [110] and [001] directions. The elongation is exclusively along the [110] direction. By contrast the (111) epilayer consists of larger loosely connected mesa (shown in Figure 3c) with dimensions up to about 5 \( \mu \)m, dissected occasionally by deep troughs which extend down to the substrate. These mesa have a distinctive serrated “autumn leaf” morphology and flat surfaces on which it is possible to resolve atomic scale steps with a height of 0.29 nm. This distance is equal to \( a/2\sqrt{3} \) where \( a \) is the cubic lattice parameter of \( \text{In}_2\text{O}_3 \) and corresponds to the separation between successive cation containing planes within the bixbyte structure. The morphological differences between (100) and (110) surfaces become even more pronounced for samples grown at 900 °C, as shown in Figure 3d,e. Here the islands on the (100) surface have developed a more uniform square shape. The typical edge size of the islands is now about 1 \( \mu \)m, which is around a factor of 10 bigger than for films grown at 750 °C. The island size is dependent on the surface coverage (Supporting Information). However, the islands always remain aligned with edges parallel to (110) directions and have sloping side facets inclined at 54.7° to the surface plane, evident in both AFM images and cross sectional TEM. The characteristic angle and the azimuthal orientation allow us to identify the side facets as being of \{111\} origin. As shown in Figure 3e, on the (110) surface the anisotropy between [110] and [001] directions becomes much more apparent and the islands have assumed a “rodlike” appearance with typical lengths between 2 and 5 \( \mu \)m along the [110] direction but with widths of around only 100 nm along the [001] direction. In contrast to films grown on (100) and (110) substrates, those grown on (111) substrates showed very little change on increasing the growth temperature from 750 to 900 °C (Figure 3f). The spontaneous development of highly oriented nanorods on (110) surfaces prompted us to explore growth at yet higher temperatures. Panels g–i in Figure 3 show AFM images of a layer grown with a lower nominal coverage (50 nm) than in Figure 3e at 1000 °C. The rods are now further elongated with lengths in excess of 20 \( \mu \)m and a width restricted to about 100 nm, to give an aspect ratio of over 200. As with the square islands on (100) surfaces, the rods have sloping side facets and the predominant facets parallel to the [110] direction are of \{111\} nature.

The morphology of growth in mismatched epitaxial systems depends on a complex interplay between the kinetics of
nucleation and surface diffusion and the minimization of surface and interface energies and elastic strain. The very pronounced changes with substrate temperature indicate that at low temperatures kinetic factors must be important and it is not clear that even at the highest temperatures that growth morphology is determined by purely thermodynamic factors. Nonetheless, many aspects of the experimental observations can be rationalized by considering the energies of the low-index surfaces of In$_2$O$_3$ computed using ab initio total energy calculations. The surface energy ($\gamma$) is defined as the energy per unit area required for forming the surface relative to the bulk and is calculated according to:

$$\gamma = \frac{(U_{\text{slab}} - U_{\text{bulk}})}{2A}$$

where $U_{\text{slab}}$ is the total energy of the 2D surface slab with a 2 nm vacuum region and $U_{\text{bulk}}$ is the energy of the corresponding number of bulk In$_2$O$_3$ formula units; $A$ represents the surface area which is created on each side of the slab and is repeated periodically. The (100), (110), and (111) surfaces were modeled using $a \times a$, $a \times a\sqrt{2}$, and $a\sqrt{2} \times a\sqrt{2}$ expansions, respectively.

Side view ball and stick models of the three bixbyite surfaces are shown in Figure 4 along with corresponding views of the low-index fluorite surfaces. The computed relaxed surface energies and associated relaxation energies are given at the bottom of the figure. The (100) surface of fluorite is a classic example of a “Type III” ionic surface within the Tasker classification and contains alternating cation and anion planes. These give rise to a surface dipole and cause the surface energy to diverge to infinity for sufficiently thick slabs. The polar surface may be stabilized in a simple manner through microfaceting, that is, by transferring half the ions in the outermost ionic layer to the other side of the slab, which allows for distinct cation- or anion-terminated surfaces. By contrast, the (110) surface of
fluorite is a stable “Type I” surface containing charge neutral ionic layers. Finally the (111) surface is “Type II” and contains repeating quadrupolar grouping of anionic and cationic layers. The bixbyite surfaces of In$_2$O$_3$ are very similar in appearance to those of the parent fluorite structure, although there is minor rumpling within the cation layers due to the relaxations in atomic positions associated with the intrinsic vacant oxygen sites within the structure and the (110) surface is no longer rigorously “Type II”. The bulk-terminated surface energies follow a sequence $\gamma_{(100)}^{\text{In}} > \gamma_{(100)}^{\text{O}} > \gamma_{(110)} > \gamma_{(111)}$, although the difference between (111) and (110) surfaces is rather small. However, the relaxation energy for the (111) surface is significantly bigger than for the (110) surface so that the relaxed surface energy for the (111) surface is about 0.18 J/m$^2$ lower than the (110) surface energy. Cleavage of the (111) surface breaks a single long In–O bond (0.24 nm) separating the charge neutral In$_2$O$_3$ units; efficient relaxation is then achieved primarily through a concerted contraction of the (111) In–O bond in the subsurface layers by ca. 9%. The order of surface energies is the same as found for oxides with the fluorite structure such as UO$_2^{28}$ and our substrate material cubic Y-stabilized ZrO$_2$. Thus for 24% Y-doped ZrO$_2$, Ballabio et al. found relaxed surface energies $\gamma_{(100)}^{\text{In}} = 1.75$ J/m$^2$, $\gamma_{(110)} = 1.44$ J/m$^2$, and $\gamma_{(111)} = 1.04$ J/m$^2$. Note however that the order of surface energies for In$_2$O$_3$ is different from that proposed by Hao et al. who suggested a sequence $\gamma_{(110)} > \gamma_{(100)} > \gamma_{(111)}$ on the basis of the morphologies In$_2$O$_3$ nanocrystals prepared by vapor transport.\textsuperscript{31}

The present results establish unambiguously that the surface energies of In$_2$O$_3$ have a direct influence on the morphology of single crystal thin films. Continuous or near continuous epilayers that are atomically flat on the micrometer length range can be grown under a wide range of conditions on (111)-oriented substrates because the (111) surface energy for In$_2$O$_3$ is the lowest among the three low index surfaces and $\gamma_{\text{In}_2\text{O}_3(111)} < \gamma_{\text{ZrO}_2(111)}$. By contrast on (100) and (110) surfaces an island growth mode is preferred. The thermodynamically favored (111) termination is found to occur through spontaneous development of sloping side facets on the islands. Although this increases the surface area of side facets by a factor of cosec $\theta$ (where $\theta$ is the contact angle with the surface), this is energetically favorable because higher energy {110} or {100} edge walls are replaced by lower energy {111} facets. In addition there is a reduction in the surface energy associated with the island top and with the bare substrate at the minimal expense of increasing the overall contribution of the interface energy.

The propensity for the sloping side facets of the islands to have {111} orientation in turn determines the azimuthal orientation of the square islands found on (100) substrates and the elongation of islands along the [110] direction to give rodlike structures on (110)-oriented substrates. This is illustrated in Figure 5 that shows that {111} side facets can form on (100) islands provided the island edges align along the [110] directions; alignment with edges parallel to (100) directions would be associated with higher energy {110} side facets. Similarly on (110) surfaces, elongation of islands to give rodlike structures with the long axis along the [110] direction allows for the development of extended {111} side facets whereas elongation along the [001] direction would demand formation of extended sloping {100} facets. A
detailed treatment of the orientation dependence of the surface energy of the square islands found on (100) surfaces is given as Supporting Information; it is found that an energy of order $3.8 \times 10^{-13}$ J is required to rotate an island of the sort shown in Figure 3d through 45°. Furthermore, it is shown that the formation of nanorod islands with a very high aspect ratio between length $l$ and width $w$ is driven by minimization of the surface energy, provided that the interfacial energy $\gamma(110)$ is small.

In summary, we have been able to rationalize both the distinct growth modes found for In$_2$O$_3$ on differently oriented Y-stabilized zirconia surfaces and the propensity for development of islands with $\{111\}$ facets on (100) and (110) surfaces in terms of relaxed surface energies. The growth of highly oriented nanorods on (110) substrates is of particular note given the growing recent interest in field effect transistors based on nanowires. However, most established techniques for preparation of oxide nanowires or nanobelts lead to a tangled mass of interpenetrating structures, which is in contrast to the perfectly aligned rods prepared in the present work. The use of an anisotropic (110) substrate as in the present work ensures that the rods align spontaneously in one direction. This is in contrast to very recent work where Gd-doped CeO$_2$ nanorods were grown on the (100) surface of cubic LaAlO$_3$. Here the formation of (110)-oriented rodlike structures is driven by anisotropy in the mismatch between the square surface cell of the substrate and the rectangular surface cell of the epilayer. However, rods grow in two orthogonal directions unless the substrate is deliberately scratched to promote uniaxial growth. We can conclude that the use of slightly mismatched (110)-oriented substrates of cubic or tetragonal materials will provide a general approach to the epitaxial growth of oxide nanostructures with uniaxial orientation.

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Supporting Information Available. (S1) Control of the In$_2$O$_3$ island size on (100) surfaces; (S2) analysis of island orientation on (100) surfaces; (S3) aspect ratio of nanorods on (110)-oriented substrates. This material is available free of charge via the Internet at http://pubs.acs.org.

REFERENCES AND NOTES
